Volume and Surface Area of Solids

Understanding of Volume and Surface Area of Solids

- Solids are three-dimensional objects having length, breadth, and height.
- Volume is the amount of space occupied by a solid and is expressed in cubic units like cm³, m³.
- Surface Area is the total area of the outer surface of a solid and is expressed in square units like cm², m².
- Different solids like cube, cuboid, cylinder, cone, sphere, and hemisphere have different formulas for volume and surface area.

Name of the solid	Figure	Volume	Laterial/Curved Surface Area	l Total Surface Area
Cuboid		lbh	2lh + 2bh or 2h(l+b)	2lh+2bh+ <mark>2lb</mark> or 2(lh+bh+lb)
Cube	a a a	a³	4a ²	4a ² +2a ² or 6a ²
Right circular cylinder	h	$\pi r^2 h$	2πrh	$2\pi rh + 2\pi r^{2}$ or $2\pi r(h+r)$
Right circular cone	h	$\frac{1}{3}\pi r^{2}h$	πrl	$\pi rl + \pi r^{2}$ or $\pi r(l+r)$
Sphere	r	$\frac{4}{3}\pi r^3$	$4\pi r^2$	$4\pi r^2$
Hemisphere	r	$\frac{2}{3}\pi r^3$	$2\pi r^2$	$\frac{2\pi r^2 + \pi r^2}{\sigma r}$

Important Points

- Volume of cube = side³
- Surface area of cube = 6 × side²
- Volume of cuboid = length × breadth × height
- Surface area of cuboid = 2(lb + bh + hl)
- Volume of cylinder = $\pi r^2 h$
- Surface area of cylinder = $2\pi r(h + r)$
- Volume of cone = $\frac{1}{3}\pi r^2 h$
- Surface area of cone = $\pi r(I + r)$ where I is slant height
- Volume of sphere = $\frac{4}{3}\pi r^3$
- Surface area of sphere = $4\pi r^2$

Examples with Solutions

Example: Volume and Surface Area of a Cube

> Find the volume and surface area of a cube of side 4 cm.

Solution: Volume = 4^3 = 64 cm³, Surface Area = 6 × 4^2 = 6 × 16 = 96 cm²

Example: Volume and Surface Area of a Cuboid

Find the volume and surface area of a cuboid of length 5 cm, breadth 3 cm, and height 2 cm.

Solution: Volume = $5 \times 3 \times 2 = 30 \text{ cm}^3$,

Surface Area = $2(5 \times 3 + 3 \times 2 + 2 \times 5)$

$$= 2(15 + 6 + 10)$$

 $= 2(31) = 62 \text{ cm}^2$

Example: Volume and Surface Area of a Cylinder

Find the volume and surface area of a cylinder of radius 3 cm and height 7 cm. Take $\pi = \frac{22}{7}$.

Solution: Volume = $\pi r^2 h = \frac{22}{7} \times 3 \times 3 \times 7 = 198 \text{ cm}^3$,

Surface Area = $2\pi r(h + r) = 2 \times \frac{22}{7} \times 3 \times (7 + 3)$

$$= 2 \times \frac{22}{7} \times 3 \times 10$$
$$= \frac{660}{7} \approx 94.29 \text{ cm}^2$$

Example: Volume and Surface Area of a Cone

> Find the volume and surface area of a cone with radius 4 cm, height 9 cm. Take π = 3.14.

Solution: Slant height I = $\sqrt{4^2 + 9^2}$ = $\sqrt{16 + 81}$ = $\sqrt{97} \approx 9.8 \text{ cm}$ Volume = $\frac{1}{3}\pi r^2 h = \frac{1}{3} \times 3.14 \times 4 \times 4 \times 9$ = $\frac{1}{3} \times 3.14 \times 16 \times 9$ = 150.72 cm³ Surface Area = $\pi r(I + r) = 3.14 \times 4 \times (9.8 + 4)$ = $3.14 \times 4 \times 13.8$ = 173.28 cm²

Example: Volume and Surface Area of a Sphere

> Find the volume and surface area of a sphere of radius 5 cm. Take π = 3.14.

Solution: Volume =
$$\frac{4}{3}\pi r^3$$

= $\frac{4}{3} \times 3.14 \times 5 \times 5 \times 5$
= $\frac{4}{3} \times 3.14 \times 125$
= 523.33 cm³
Surface Area = $4\pi r^2 = 4 \times 3.14 \times 5 \times 5 = 314$ cm²

Summary Points

- Volume measures the space occupied by a solid, expressed in cubic units.
- Surface area measures the total outer area, expressed in square units.
- Different solids have different formulas.
- Always use same units throughout calculation.
- Use correct value of π based on question requirements ($\frac{22}{7}$ or 3.14)