

Chapter 18

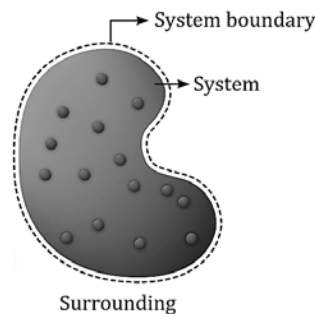
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THERMODYNAMICS SYSTEM AND ITS CHARACTERISTICS

Thermodynamic System

A thermodynamic system is a distinct portion of matter delineated by a definite boundary, within which processes are to be analyzed.



Surroundings

The surroundings encompass all entities that interact with the system.

Boundary

Boundaries demarcate the system from its surroundings. These boundaries can be real or conceptual, as well as rigid or flexible.

Universe

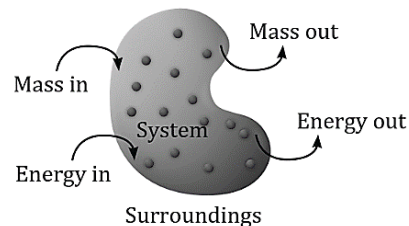
Both the system and its surroundings collectively constitute the universe.

Types of System and its Characteristics

Thermodynamic systems are categorized based on the potential interactions between the system and its surroundings.

Open system

In an open system, both mass and energy are exchangeable between the system and its surroundings.

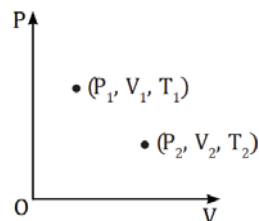


Thermodynamic Coordinate System

In thermodynamics, the typical properties of a system, particularly in gaseous systems, are pressure (P), volume (V), and temperature (T).

These constitute the thermodynamic coordinates, defining the state of a system. With these coordinates, an indicator diagram, such as a P-V graph, can be constructed to represent the system.

Now, consider a system wherein a substance undergoes heating from an initial state characterized by pressure P_1 , volume V_1 , and temperature T_1 , to a final state characterized by pressure P_2 , volume V_2 , and temperature T_2 . Employing the thermodynamic coordinate system, both states can be defined as points on the P-V graph, as depicted in the figure.

**Ideal Gas and Universal Gas constant****Ideal Gas**

Here are some fundamental rules concerning ideal gases:

1. The molecules continuously move in random directions.
2. Molecules exhibit behavior similar to that of rigid spheres.
3. All collisions are elastic.
4. Pressure arises from collisions between molecules and the container walls.

Universal Gas Constant

For an ideal gas,

$$PV = NkT$$

Where, $k = 1.38 \times 10^{-23} \text{ J K}^{-1}$

If a gas contains n moles, $N = nN_A$ (where $N_A = \text{Avogadro's number} = 6.023 \times 10^{23}$)

$$PV = nN_A kT$$

$$PV = nRT$$

Universal gas constant, $R = N_A k$

$$R = 8.314 \text{ J K}^{-1} \text{ mol}$$

Characteristic Gas Constant

From the ideal gas equation,

$$PV = nRT$$

$$PV = \frac{m}{M} RT$$

$$PV = mR_C T$$

Where, $R_C = \frac{R}{M} = \text{Characteristic gas constant}$

Characteristic gas constant of air,

$$R_{C_{\text{air}}} = \frac{8.314}{29}$$

$$R_{C_{\text{air}}} = 0.287 \times 10^3 \text{ J Kg}^{-1} \text{ K}^{-1}$$

Conservation of Energy

Energy cannot be created or destroyed; it can only be transformed from one form to another.

Specific Heat of a Gas**Specific heat at constant volume**

The specific heat at constant volume is the amount of heat needed to increase the temperature of a unit mass of gas by 1°C or 1 K while keeping its volume constant.

$$c_V = \frac{(\Delta Q)_V}{M \Delta T}$$

Molar specific heat at constant volume

The molar specific heat at constant volume refers to the amount of heat needed to increase the temperature of one mole of a gas by 1°C or 1 K while maintaining its volume constant.

$$C_V = M_{\text{molar}} c_V$$

$$C_V = M_{\text{molar}} \left(\frac{(\Delta Q)_V}{M \Delta T} \right)$$

$$C_V = \frac{1}{n} \frac{(\Delta Q)_V}{\Delta T} \left(\text{Since } n = \frac{M}{M_{\text{molar}}} \right)$$

Specific heat at constant pressure

The specific heat at constant pressure is the amount of heat needed to increase the temperature of a unit mass of a gas by 1 °C or 1 K while keeping its pressure constant.

$$c_p = \frac{(\Delta Q)_p}{M \times \Delta T}$$

Molar specific heat at constant pressure

The molar specific heat at constant pressure refers to the amount of heat needed to increase the temperature of one mole of a gas by 1 °C or 1 K while maintaining its pressure constant.

$$C_p = M_{\text{molar}} c_p$$

$$C_p = M_{\text{molar}} \left(\frac{(\Delta Q)_p}{M \times \Delta T} \right)$$

$$C_p = \frac{1}{n} \frac{(\Delta Q)_p}{\Delta T} \quad \left(\text{Since } n = \frac{M}{M_{\text{molar}}} \right)$$

Mayer's formula

The relationship between molar specific heat at constant volume and molar specific heat at constant pressure is termed as Mayer's formula or Mayer's relation.

Mayer's formula establishes the relationship between molar specific heat at constant volume (C_v) and molar specific heat at constant pressure (C_p) as follows:

$$C_p - C_v = R$$

Where, R is the universal gas constant.

Therefore, from Mayer's formula it can be easily be concluded that $C_p > C_v$ since R is a positive quantity.

Specific heat in terms of the degree of freedom

Heat supplied to a gas at constant volume, $\Delta Q_v = nC_v\Delta T$

If f represents the degrees of freedom, then the molar specific heat at constant volume (C_v) is expressed as:

$$C_v = \left(\frac{1}{2}f\right)R$$

Also from Mayer's formula, $C_p - C_v = R$

Therefore,

$$C_p = C_v + R$$

$$C_p = \frac{f}{2}R + R$$

$$C_p = \left(\frac{f}{2} + 1\right)R$$

Adiabatic index (γ)

The adiabatic index is defined as,

$$\gamma = \frac{C_p}{C_v}$$

Also,

$$C_v = \left(\frac{1}{2}f\right)R \text{ and } C_p = \left(\frac{f}{2} + 1\right)R$$

$$\gamma = \frac{C_p}{C_v} = \frac{\left(\frac{f}{2} + 1\right)R}{\left(\frac{1}{2}f\right)R}$$

$$\gamma = \left(1 + \frac{2}{f}\right)$$

Value of γ for different gases

1. For a monatomic gas,

$$f = 3$$

$$\gamma = \frac{5}{3} = 1.6$$

2.

For a diatomic gas,

$$f = 5$$

$$\gamma = \frac{7}{5} = 1.4$$

3.

For a triatomic gas

$$f = 6 \text{ (non linear)}$$

$$\gamma = \frac{4}{3} = 1.33$$