

- Identical things of another type, r identical things of the third type, and n different things
- Number of divisors of N
- Divisions and distributions
 - Distinct objectives
 - Distribution of identical objectives
- Application of Multinomial Expansion
 - Different cases of multinomial theorem
- Exponent Of a Prime Number n!.
- Principles of inclusion and exclusion
 - Derangement
 - Distribution of n different objects into r distinct boxes if in each box at least 1 object is placed

PERMUTATION & COMBINATION

Factorial:

A handy Notation: $n! = n \cdot (n - 1) \cdot (n - 2) \dots 3 \cdot 2 \cdot 1$; $n! = n \cdot (n - 1)!$ Where $n \in \mathbb{N}$



1. $0! = 1! = 1$
2. Factorials are not defined for negative integers.
3. $n!$ is also denoted by
4. $(2n)! = 2^n \cdot n! [1 \cdot 3 \cdot 5 \cdot 7 \dots (2n - 1)]$
5. Prime Factorization of (n): If (p) is a prime number and (n) is a positive integer, then The exponent of (p) in (n) is denoted by $(E_p(n))$ and is given by

$$E_p(n!) = \left[\frac{n}{p} \right] + \left[\frac{n}{p^2} \right] + \left[\frac{n}{p^3} \right] + \dots + \left[\frac{n}{p^k} \right]$$

Where $p^k \leq n < p^{k+1}$ and $[x]$ denotes the integral part of x.

If we express the powers of each prime contained in any number (n) individually, then

(n) can be represented as $n = 2^{\alpha_1} \cdot 3^{\alpha_2} \cdot 5^{\alpha_3} \cdot 7^{\alpha_4}$

Where α_i are whole numbers.