

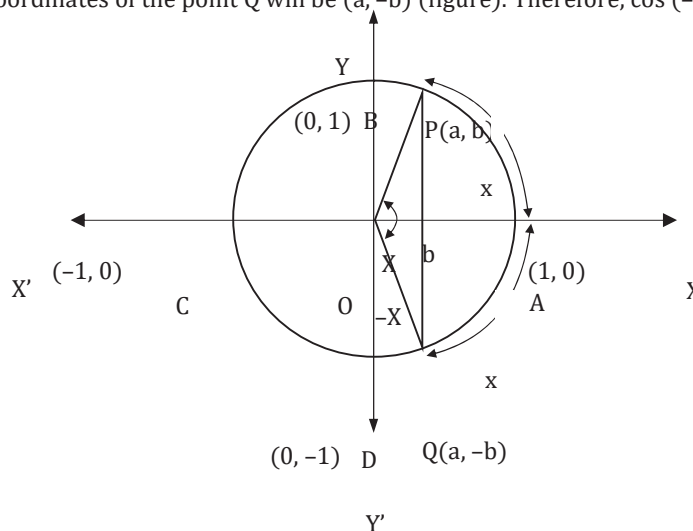
**ANGLES OF TRIGONOMETRY****Angle exceeding  $360^\circ$** **Values of Trigonometric Functions for Some Specific Angles**

( $\theta$ ) in degrees	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$	$120^\circ$	$135^\circ$	$150^\circ$	$180^\circ$	$270^\circ$	$360^\circ$
( $\theta$ ) in radians		$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	$\pi$	$\frac{3\pi}{2}$	$2\pi$
sign $\theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0	-1	0
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{1}{\sqrt{2}}$	$-\frac{\sqrt{3}}{2}$	-1	0	1
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	Not defined	$-\sqrt{3}$	-1	$-\frac{1}{\sqrt{3}}$	0	Not defined	0

The values of cosec  $x$ , sec  $x$  and cot  $x$  can be obtained by taking the reciprocal of the values of sin  $x$ , cos  $x$  and tan  $x$  respectively.

**Sign of The Trigonometric Functions**

Let  $P(a, b)$  be a point on the unit circle with centre at the origin such that  $\angle AOP = x$ . If  $\angle AOQ = -x$ , then the coordinates of the point  $Q$  will be  $(a, -b)$  (figure). Therefore,  $\cos(-x) = \cos x$  and  $\sin(-x) = -\sin x$



Since for every point  $P(a, b)$  on the unit circle,  $-1 \leq a \leq 1$  and  $-1 \leq b \leq 1$  we have  $-1 \leq \cos x \leq 1$  and  $-1 \leq \sin x \leq 1$  for all  $x$ .

In the first quadrant ( $0 < x < \frac{\pi}{2}$ ) both  $a$  and  $b$  are positive. Thus, the value of each of the trigonometric ratios is positive in the first quadrant. In the second quadrant ( $\frac{\pi}{2} < x < \pi$ )  $a$  is negative and  $b$  is positive. Thus, sin  $\theta$  and cosec  $\theta$  will be positive whereas all other trigonometric ratios will be negative in second quadrant.

In the third quadrant ( $\pi < x < \frac{3\pi}{2}$ ), both  $a$  and  $b$  are negative. Thus, tan  $\theta$  and cot  $\theta$  will be positive and all other trigonometric ratios will be negative in third quadrant.

In the fourth quadrant ( $\frac{3\pi}{2} < x < 2\pi$ )  $a$  is positive and  $b$  is negative. Thus, cos  $\theta$  and sec  $\theta$  will be positive while all other trigonometric ratios will be negative in fourth quadrant.

This can be summarized in the table as follows

	$\sin\theta$	$\cos\theta$	$\tan\theta$	$\cot\theta$	$\sec\theta$	$\operatorname{cosec}\theta$
I <sup>st</sup> Quadrant	+	+	+	+	+	+
II <sup>nd</sup> Quadrant	+	–	–	–	–	+
III <sup>rd</sup> Quadrant	–	–	+	+	–	–
IV <sup>th</sup> Quadrant	–	+	–	–	+	–