




## Multiplication on Number Line



Let us consider 3 packets, each consisting of 4 doughnuts.

|   |  |
|---|--|
| Total number of doughnuts = $4 + 4 + 4 = 12$  |  |
| We can also write:                            |  |
| Total number of doughnuts = $3 \times 4 = 12$ |  |

Therefore, we can say that multiplication is repeated addition.

### i) Closure Property:



$a, b$  Whole numbers  $\Rightarrow a \times b$ , Whole number

If  $a$  and  $b$  are two whole numbers, then  $a \times b$  is always a whole number.

| $a$ | $b$ | $a \times b$         | Whole number |
|-----|-----|----------------------|--------------|
| 9   | 7   | $9 \times 7 = 63$    | Yes          |
| 5   | 11  | $5 \times 11 = 55$   | Yes          |
| 10  | 27  | $10 \times 27 = 270$ | Yes          |



Whole number



When we multiply two whole numbers, the product is also a whole number.

**ii) Commutative Property:**



$$a, b \text{ Whole numbers} \Rightarrow a \times b = b \times a$$

If  $a$  and  $b$  are two whole numbers, then  $a \times b = b \times a$

| a | b   | $a \times b$         | $b \times a$         | Is $a \times b = b \times a$ ? |
|---|-----|----------------------|----------------------|--------------------------------|
| 1 | 7   | $1 \times 7 = 7$     | $7 \times 1 = 7$     | Yes                            |
| 8 | 11  | $8 \times 11 = 88$   | $11 \times 8 = 88$   | Yes                            |
| 3 | 100 | $3 \times 100 = 300$ | $100 \times 3 = 300$ | Yes                            |

The value of the product does not change even when the order of multiplication is changed.

**iii) Associative Property:**



$$a, b \text{ and } c \text{ Whole numbers} \Rightarrow (a \times b) \times c = a \times (b \times c)$$

If  $a$ ,  $b$  and  $c$  are any three whole numbers, then  $(a \times b) \times c = a \times (b \times c)$



| a | b | c  | $(a \times b) \times c$        | $a \times (b \times c)$        | Is $(a \times b) \times c = a \times (b \times c)$ ? |
|---|---|----|--------------------------------|--------------------------------|--|
| 1 | 7 | 5  | $(1 \times 7) \times 5 = 35$   | $1 \times (7 \times 5) = 35$   | Yes  |
| 5 | 6 | 10 | $(5 \times 6) \times 10 = 300$ | $5 \times (6 \times 10) = 300$ | Yes  |
| 8 | 2 | 5  | $(8 \times 2) \times 5 = 80$   | $8 \times (2 \times 5) = 80$   | yes  |

When we multiply three or more whole numbers, the value of the product remains the same even if they are grouped in any manner.

#### iv) Multiplicative Identity Property:

If  $a$  is any whole number, then  $a \times 1 = a = 1 \times a$

| a   | 1 | $a \times 1$         | Is $a \times 1 = a$ ? |
|-----|---|----------------------|-----------------------|
| 1   | 1 | $1 \times 1 = 1$     | Yes                   |
| 15  | 1 | $15 \times 1 = 15$   | Yes                   |
| 196 | 1 | $196 \times 1 = 196$ | Yes                   |

Multiplicative identity is any number which when multiplied by any whole number, then the value remains the same.

So, 1 is the multiplicative identity of whole numbers.

#### v) Distributivity of Multiplication over Addition:



$$a \times (b + c) = a \times b + a \times c$$



If  $a$ ,  $b$  and  $c$  are any three whole numbers, then  $a \times (b + c) = a \times b + a \times c$

| $a$ | $b$ | $c$ | $a \times (b + c)$      | $a \times b + a \times c$      | Is $a \times (b + c) = a \times b + a \times c$ ? |
|-----|-----|-----|-------------------------|--------------------------------|---|
| 2   | 3   | 5   | $2 \times (3 + 5) = 16$ | $2 \times 3 + 2 \times 5 = 16$ | Yes   |
| 1   | 4   | 7   | $1 \times (4 + 7) = 11$ | $1 \times 4 + 1 \times 7 = 11$ | Yes   |
| 3   | 5   | 8   | $3 \times (5 + 8) = 39$ | $3 \times 5 + 3 \times 8 = 39$ | Yes   |

vi) if  $a$  is any whole number other than zero, then  $a \times 0 = 0$



$$a \times 0 = 0$$

$$15 \times 0 = 0; 100 \times 0 = 0$$

**Example:** Find the product by suitable rearrangement:

i)  $4 \times 1768 \times 25$  ii)  $2 \times 166 \times 50$

i)  $4 \times 1768 \times 25$

$$= (4 \times 25) \times 1768 \text{ (by commutative property)}$$

$$= 100 \times 1768 = 176800$$

ii)  $2 \times 166 \times 50$

$$= (2 \times 50) \times 166 \text{ (by commutative property)}$$

$$= 100 \times 166 = 16600$$