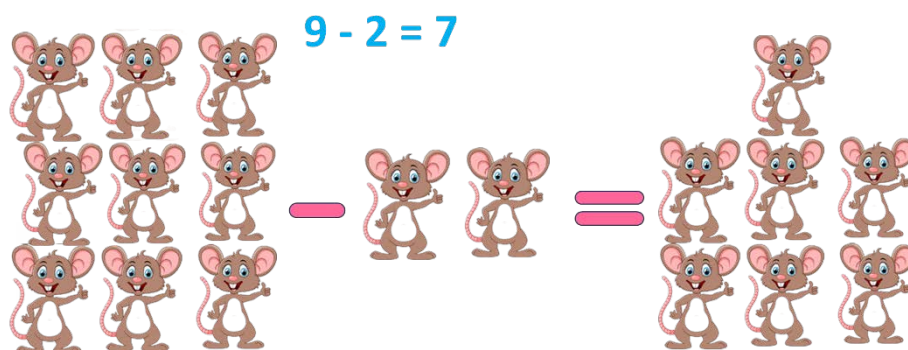
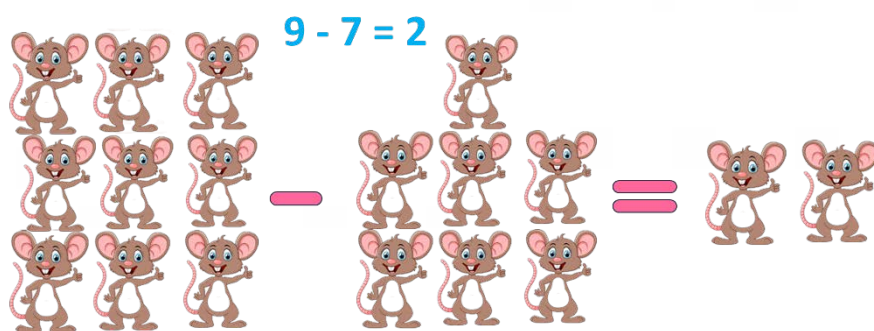
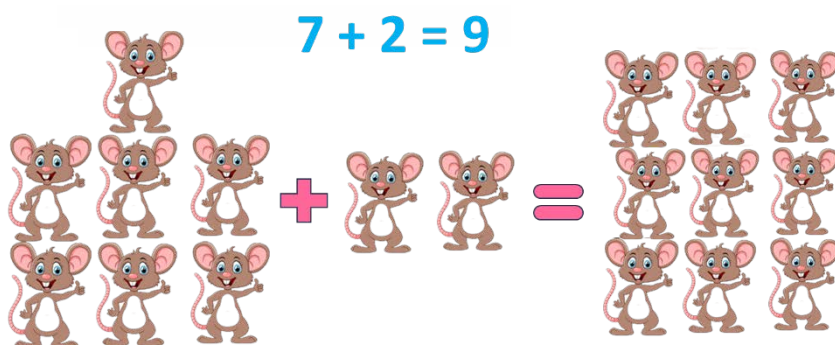


## Subtraction on Number Line



Subtraction is an inverse process of addition.

Example:  $(7 + 2 = 9) \Rightarrow (9 - 7 = 2)$





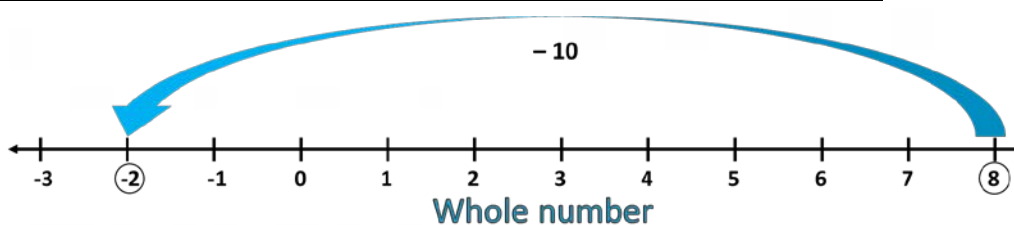
### i) Closure Property:

a, b whole numbers	If $a > b$ or $a = b$ then $a - b$ , Whole number
	If $a < b$ then $a - b$ , not a whole number

If  $a$  and  $b$  are two whole numbers such that  $a > b$  or  $a = b$ , then  $a - b$  is a whole number.

If  $a < b$ , then  $a - b$  is not a whole number.

a	b	$a - b$	Whole number
9	7	$9 - 7 = 2$	Yes
8	10	$8 - 10 = \text{Not a whole number}$	No
10	27	$10 - 27 = \text{Not a whole number}$	No



The whole numbers are not closed under subtraction.

### ii) Commutative Property:



$$a, b \text{ Whole numbers} \Rightarrow a - b \neq b - a$$



If  $a$  and  $b$  are two whole numbers, then  $a - b \neq b - a$

$a$	$b$	$a - b$	$b - a$	Is $a - b = b - a$ ?
11	7	$11 - 7 = 4$	$7 - 11 =$ Not a whole number	No
18	11	$18 - 11 = 7$	$11 - 18 =$ Not a whole number	No
13	25	$13 - 25 =$ Not a whole number	$25 - 13 = 12$	No

iii) Associative Property:



$a, b$  and  $c$  Whole numbers  $\Rightarrow (a - b) - c \neq (a - b) - c$

For any three whole numbers  $a, b$  and  $c$

$(a - b) - c \neq a - (b - c)$

$a$	$b$	$c$	$(a - b) - c$	$a - (b - c)$	Is $(a - b) - c = a - (b - c)$ ?
10	7	5	$(10 - 7) - 5 =$ Not a whole number	$10 - (7 - 5) = 8$	No
5	6	21	$(5 - 6) - 21 =$ Not a whole number	$5 - (6 - 21) = 20$	No
8	25	5	$(8 - 25) - 5 =$ Not a whole number	$8 - (25 - 5) =$ Not a whole number	No



iv) If  $a$  is any whole number other than zero, then  $a - 0 = a$  but  $0 - a$  is not defined.



$a$  is a Whole number  $\Rightarrow a - 0 = a$ ,  $0 - a$  is not defined

$18 - 5 = 13$  but  $5 - 18$  is not defined in whole numbers.

$30 - 12 = 18$  but  $12 - 30$  is not defined in whole numbers

v) If  $a$ ,  $b$  and  $c$  are whole numbers such that  $a - b = c$ , then  $b + c = a$



$a$ ,  $b$  and  $c$  Whole numbers  $\Rightarrow a - b = c$ ,  $b + c = a$

$$a - b = c$$

Transposing  $b$  to RHS

$$a = c + b \text{ or } a = b + c$$

If  $25 - 16 = 9$  then  $25 = 9 + 16$ ,

If  $46 - 8 = 38$  then  $46 = 38 + 8$



**Example:** Consider two whole numbers  $p$  and  $q$  such that  $p$  is greater than  $q$ .

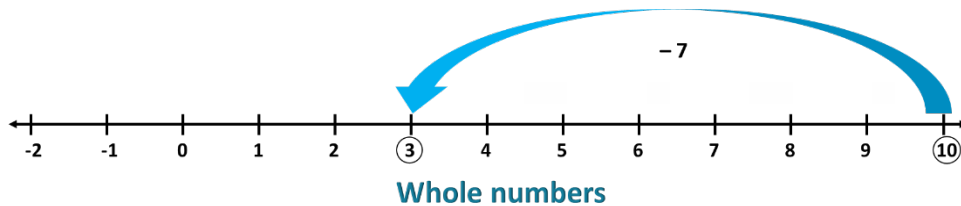
i) Is  $p - q$  a whole number? Is the result always true?

ii) Is  $q - p$  a whole number? Is the result always true?

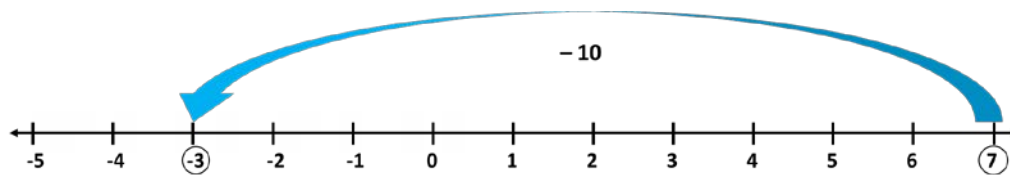
i) Yes,  $p - q$  is a whole number is always true for  $p > q$ .

ii) No,  $q - p$  is not a whole number is always true for  $p > q$ .

Let the value of  $p$  and  $q$  be 10 and 7 respectively.



$p - q = 10 - 7 = 3$ , a whole number



$q - p = 7 - 10$  not a whole number

**Example:** Solve the following,

i)  $367 - 99$

$$= 367 + (-100 + 1)$$

$$= 367 - 100 + 1$$

$$= (367 + 1) - 100$$

$$= 368 - 100 = 268$$