

## Convex and Concave Quadrilaterals

### 1. Convex Quadrilateral:

A quadrilateral is convex if all its interior angles are less than  $180^\circ$ , and no part of the shape is "pushed inward".

#### Characteristics:

- All interior angles  $< 180^\circ$ .
- Diagonals lie inside the shape.
- No line segment between any two points inside the figure goes outside the figure.

**Common Examples:** Square, Rectangle, Rhombus, Parallelogram, Trapezium

### 2. Concave Quadrilateral:

A quadrilateral is concave if at least one of its interior angles is greater than  $180^\circ$ , and one vertex seems to be pushed inward.

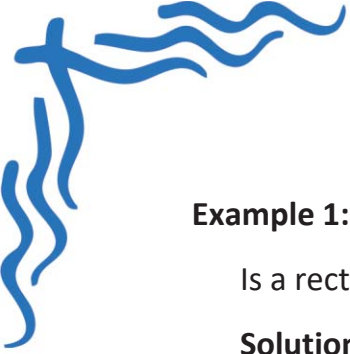
#### Characteristics:

- One angle is  $> 180^\circ$
- One of the diagonals lies outside the figure
- Shape looks "caved in" at one vertex

**Example:** An arrowhead-like shape

### Properties of Convex and Concave Quadrilaterals:

Property	Convex Quadrilateral	Concave Quadrilateral
Interior angles	All $< 180^\circ$	One angle $> 180^\circ$
Diagonals	Both lie inside the shape	One lies outside
Shape	Looks regular or balanced	Has an inward corner
Common examples	Square, Rhombus, Trapezium	Arrowhead-like figures
Sum of interior angles	Always $360^\circ$	Always $360^\circ$

**Example 1:**

Is a rectangle a convex or concave quadrilateral?

**Solution:**

A rectangle has four right angles, each measuring  $90^\circ$ .

Since all interior angles are less than  $180^\circ$ , and both diagonals lie inside the figure, it is a convex quadrilateral.

Answer: Convex quadrilateral

**Example 2:**

A quadrilateral has one of its angles as  $210^\circ$ . Is it convex or concave?

**Solution:**

If one of the angles is greater than  $180^\circ$ , then by definition, the quadrilateral is concave.

Answer: Concave quadrilateral

**Summary Points:**

- **Convex quadrilateral:** All angles  $< 180^\circ$ , diagonals inside, regular shape.
- **Concave quadrilateral:** One angle  $> 180^\circ$ , diagonals may lie outside.
- Sum of all interior angles is always  $360^\circ$  for both types.
- Common convex shapes include square, rectangle, and trapezium.
- Concave shapes look like they are "bent inward" at one corner.