

EXERCISE LEVEL – I

EL- I

- Q.1** In $\int_a^b f(y)dy$, what is called as?
 (A) Integration (B) Upper limit
 (C) Lower limit (D) Limit of an integral
- Q.2** The value of $\int_0^\pi \sin y dy$ is 2.
 (A) True (B) False
- Q.3** Compute $\int \cos(x) - \frac{3}{x^4} dx$.
 (A) $\sec(x) + \frac{3}{4}x^{-7} + C$ (B) $\sec(x) + \frac{3}{4}x^{-3} + C$
 (C) $\sin(x) + \frac{3}{4}x^{-3}$ (D) $\sin(x) + \frac{3}{4}x^{-3} + C$
- Q.4** What is the value of $\int_2^3 \cos(x) - \frac{3}{x^4} dx$.
 (A) $\sin(3) - \sin(2)$ (B) $\sin(3) - \sin(9) - \frac{19}{288}$
 (C) $\sin(8) - \sin(2) - \frac{19}{288}$ (D) $\sin(3) - \sin(2) - \frac{19}{288}$
- Q.5** Evaluate $\int_7^9 \cos(x) dx$.
 (A) $8(-\sin 9 - \sin 7)$ (B) $8(\sin 9 + \sin 7)$
 (C) $8(\sin 9 - \sin 7)$ (D) $7(\sin 9 - \sin 7)$
- Q.6** Compute $\int_2^3 \frac{\cos x - \sin x}{4} dx$.
 (A) $\frac{1}{4}(\sin 2 + \cos 3 - \sin 3 - \cos 2)$ (B) $\frac{1}{4}(\sin 3 - \cos 3 - \sin 2 - \cos 2)$
 (C) $\frac{1}{4}(\sin 3 + \cos 3 - \sin 2 - \cos 2)$ (D) $\frac{1}{4}(\sin 3 + \cos 3 + \sin 2 - \cos 2)$
- Q.7** What y is in $\int_a^b f(y) dy$ called as?
 (A) Random variable (B) Dummy symbol
 (C) Integral (D) Integrand

- Q.8** The value of $\int_1^2 1y^5 dy$ is.
(A) 10.5 (B) 56 (C) 9 (D) 23
- Q.9** The value of $\int_1^2 1y^5 / 5 dy$ is.
(A) 12 (B) 2.1 (C) 21 (D) 11.1
- Q.10** Evaluate $\int_0^x \sin x dx$.
(A) 2 (B) 6 (C) 17 (D) 3
- Q.11** Evaluate $\int_2^3 \cos x dx$.
(A) 38.2 (B) $\sin(9) - \sin(4)$
(C) 89.21 (D) $\sin(3) - \sin(2)$
- Q.12** Compute $\int_2^3 2e^x dx$.
(A) $2(e^9 - e^4)$ (B) 84.32 (C) $2(e^3 - e^2)$ (D) 83.25
- Q.13** In $\int_b^a f(x) dx$, b called as lower limit and a is called as upper limit.
(A) False (B) True
- Q.14** Compute $\int_0^6 9e^x dx$.
(A) 30.82 (B) $9(e^6 - e^3)$ (C) 11.23 (D) $81(e^6 - e^3)$
- Q.15** Evaluate $\int_3^7 \sin(t) - 2 \cos(t) dt$.
(A) $\cos(7) - 2\sin(7) + (\cos(3) + 2\sin(3))$
(B) -17
(C) 12
(D) $\cos(7) - 2\sin(7) - (\cos(3) + 2\sin(3))$
- Q.16** Find $\int_0^8 x dx$.
(A) 32 (B) 34 (C) 21 (D) 24
- Q.17** Find $\int_0^{\frac{\pi}{2}} 5 \sin x dx$.
(A) -5 (B) 9 (C) 5 (D) -9
- Q.18** Solve the value of $\int_4^5 \log x dx$.
(A) $5 \log 5 - \log 4 + 1$ (B) $5 \log 5 - 4 \log 4 - 1$
(C) $4 \log 5 - 4 \log 4 - 1$ (D) $5 - 4 \log 4 - \log 5$

Q.19 Determine $\int_0^{\frac{\pi}{4}} 9 \cos^2 x dx$.

- (A) $\frac{9}{2} \left(\frac{\pi}{6} - 1 \right)$ (B) $\frac{9}{4} \left(\frac{\pi}{6} + 1 \right)$ (C) $\frac{9}{4} \left(\frac{\pi}{2} - 1 \right)$ (D) $\left(\frac{\pi}{2} - 1 \right)$

Q.20 Determine $\int_0^2 e^{2x} dx$

- (A) $\frac{e^4 - 1}{6}$ (B) $\frac{e^4 + 1}{2}$ (C) $\frac{e - 1}{2}$ (D) $\frac{e^4 - 1}{2}$

Q.21 Evaluate $\int_{\frac{\pi}{4}}^{\frac{\pi}{2}} 2 \sin x \sin(\cos x) dx$.

- (A) $2 \left(1 - \cos \frac{1}{\sqrt{2}} \right)$ (B) $\left(\cos \frac{1}{\sqrt{2}} - \cos 1 \right)$
(C) $2 \left(\cos \frac{1}{\sqrt{2}} + 1 \right)$ (D) $\left(\cos \frac{1}{\sqrt{2}} + \cos 1 \right)$

Q.22 Find $\int_{-2}^1 5x^4 dx$.

- (A) 54 (B) 75 (C) 33 (D) 36

Q.23 Find $\int_0^3 e^x dx$.

- (A) $e^3 + 1$ (B) $-e^3 - 1$ (C) $e^3 - 1$ (D) $3e^2 - 2$

Q.24 Find $\int_0^{\frac{\pi}{4}} 2 \tan x dx$.

- (A) $\log 2$ (B) $\log \sqrt{2}$ (C) $2 \log 2$ (D) 0

Q.25 Solve $\int_{-1}^1 2xe^x dx$.

- (A) $\frac{4}{e}$ (B) $4e$ (C) $-\frac{4}{e}$ (D) $-4e$

Q.26 Evaluate the integral $\int_0^{\frac{x^2}{4}} \frac{9 \sin \sqrt{x}}{2\sqrt{x}} dx$.

- (A) 9 (B) -9 (C) $\frac{9}{2}$ (D) $-\frac{9}{2}$

Q.27 Find $\int_0^{-1} 20x^3 e^{x^4} dx$.

- (A) $(e - 1)$ (B) $5(e + 1)$ (C) $5e$ (D) $5(e - 1)$

- Q.28** Solve $\int_{-1}^1 \frac{5x^4}{\sqrt{x^5+3}} dx$.
 (A) $4-\sqrt{2}$ (B) $4+2\sqrt{2}$ (C) $4-2\sqrt{2}$ (D) $1-2\sqrt{2}$
- Q.29** Find $\int_0^{\frac{\sqrt{\pi}}{2}} 2x \cos x^2 dx$.
 (A) 1 (B) $\frac{1}{\sqrt{2}}$ (C) $-\frac{1}{\sqrt{2}}$ (D) $\sqrt{2}$
- Q.30** Evaluate the integral $\int_1^6 \frac{\sqrt{x}+3}{\sqrt{x}} dx$.
 (A) 9 (B) $\frac{9}{2}$ (C) $-\frac{9}{2}$ (D) $\frac{4}{5}$
- Q.31** Solve $\int_1^2 \frac{12 \log x}{x} dx$.
 (A) $-12 \log 2$ (B) $24 \log 2$ (C) $12 \log 2$ (D) $24 \log 4$
- Q.32** Determine $\int_0^{\frac{\pi}{4}} \frac{5 \sin(\tan^{-1} x)}{1+x^2} dx$.
 (A) $5-\frac{1}{\sqrt{2}}$ (B) $5+\frac{5}{\sqrt{2}}$ (C) $-5+\frac{5}{\sqrt{2}}$ (D) $5-\frac{5}{\sqrt{2}}$
- Q.33** Find $\int_{-1}^1 7x^2(x^7+8)dx$.
 (A) -386 (B) $-\frac{386}{3}$ (C) $\frac{386}{3}$ (D) 386
- Q.34** Evaluate $\int_{\sqrt{2}}^2 14x \log x^2 dx$.
 (A) $14(3 \log 2 - 1)$ (B) $14(3 \log 2 + 1)$ (C) $\log 2 - 1$ (D) $3 \log 2 - 1$
- Q.35** Solve $\int_2^3 2x^2 e^{x^3} dx$.
 (A) $e^{27} - e^8$ (B) $\frac{2}{3}(e^{27} - e^8)$ (C) $\frac{2}{3}(e^8 - e^{27})$ (D) $\frac{2}{3}(e^{27} + e^8)$
- Q.36** What does the difference property of definite integrals state?
 (A) $\int_a^b [-f(x) - g(x)] dx$ (B) $\int_a^b [-f(-x) + g(x)] dx$
 (C) $\int_a^b [f(x) - g(x)] dx$ (D) $\int_a^b [f(x) + g(x)] dx$

- Q.37** The sum property pertaining to definite integrals is $\int_a^b [f(x) + g(x)] dx$?
 (A) False (B) True
- Q.38** What does the constant multiple property of definite integrals state?
 (A) $\int_a^b k - f(x) dy$ (B) $\int_a^b [f(-x) + g(x)] dx$
 (C) $\int_a^b k - f(x) dx$ (D) $\int_a^b [f(x) + g(x)] dx$
- Q.39** What does the reverse integration property of definite integrals entail?
 (A) $-\int_a^b f(x) dx = -\int_b^a g(x) dx$ (B) $-\int_a^b f(x) dx = \int_b^a g(x) dx$
 (C) $\int_a^b f(x) dx = \int_b^a g(x) dx$ (D) $\int_a^b f(x) dx = -\int_b^a f(x) dx$
- Q.40** Recognize the property of the zero-length interval.
 (A) $\int_a^b f(x) dx = -1$ (B) $\int_a^b f(x) dx = 1$
 (C) $\int_a^b f(x) dx = 0$ (D) $\int_a^b f(x) dx = 0.1$
- Q.41** What does the property of adding intervals entail?
 (A) $\int_a^c f(x) dx + \int_b^c f(x) dx = \int_a^c f(x) dx$ (B) $\int_a^b f(x) dx + \int_b^a f(x) dx = \int_a^c f(x) dx$
 (C) $\int_a^b f(x) dx + \int_b^c f(x) dx = \int_a^c f(x) dx$ (D) $\int_a^b f(x) dx - \int_b^c f(x) dx = \int_a^c f(x) dx$
- Q.42** What is the designation of the property $\int_a^b f(x) dx + \int_b^c f(x) dx = \int_a^c f(x) dx$?
 (A) Zero interval property (B) Adding intervals property
 (C) Adding integral property (D) Adding integrand property
- Q.43** What is the designation of this property $\int_a^b f(x) dx = -\int_b^a f(x) dx$?
 (A) Reverse integral property (B) Adding intervals property
 (C) Zero interval property (D) Adding integrand property
- Q.44** What is the title or designation of this property $\int_a^b f(x) dx = 0$?
 (A) Reverse integral property (B) Adding intervals property
 (C) Zero-length interval property (D) Adding integrand property
- Q.45** Under which property does this equation fall $\int_{-1}^1 \sin x dx = -\int_1^{-1} \sin x dx$?
 (A) Reverse integral property (B) Adding intervals property
 (C) Zero-length interval property (D) Adding integrand property

- Q.46** Evaluate $\int_2^3 3f(x) - g(x) dx$, if $\int_2^3 f(x) = 4$ and $\int_2^3 g(x) dx = 4$.
 (A) 38 (B) 12 (C) 8 (D) 7
- Q.47** Compute $\int_3^2 f(x) dx$ if $\int_2^3 f(x) = 4$.
 (A) -4 (B) 84 (C) 2 (D) -8
- Q.48** Compute $\int_8^2 2f(x) dx$ if $\int_2^8 f(x) = -3$
 (A) -4 (B) 84 (C) 2 (D) -8
- Q.49** Compute $\int_2^6 7e^x dx$.
 (A) 30.82 (B) $7(e^6 - e^2)$ (C) 11.23 (D) $81(e^6 - e^3)$
- Q.50** Evaluate $\int_3^7 2f(x) - g(x) dx$, if $\int_3^7 f(x) = 4$ and $\int_3^7 g(x) dx = 2$.
 (A) 38 (B) 12 (C) 6 (D) 7
- Q.51** If $\int_{-1}^4 f(x) dx = 4$ and $\int_2^4 (3 - f(x)) dx = 7$, then the value of $\int_2^{-1} f(x) dx =$
 (A) 2 (B) -2
 (C) -3 (D) -5
- Q.52** If $\int_0^\infty \frac{x^2 dx}{(x^2+a^2)(x^2+b^2)(x^2+c^2)} = \frac{\pi}{2(a+b)(b+c)(c+a)}$, then the value of $\int_0^\infty \frac{dx}{(x^2+4)(x^2+9)}$ is
 (A) $\frac{\pi}{60}$ (B) $\frac{\pi}{20}$
 (C) $\frac{\pi}{40}$ (D) $\frac{\pi}{80}$
- Q.53** The value of $\int_0^\infty \frac{xdx}{(1+x)(1+x^2)}$ is equal to
 (A) $\frac{\pi}{4}$ (B) $\frac{\pi}{2}$
 (C) π (D) $\frac{\pi}{8}$
- Q.54** The value of the definite integral $\int_0^{\pi/2} \sqrt{\tan x} dx$ is
 (A) $\sqrt{2}\pi$ (B) $\frac{\pi}{\sqrt{2}}$
 (C) $2\sqrt{2}\pi$ (D) $\frac{\pi}{2\sqrt{2}}$
- Q.55** For $x \in \mathbb{R}$ and a continuous function f ,
 let $I_1 = \int_{\sin^2 t}^{1+\cos^2 t} xf\{x(2-x)\} dx$ and $I_2 = \int_{\sin^2 t}^{1+\cos^2 t} f\{x(2-x)\} dx$, then $\frac{I_1}{I_2}$
 (A) -1 (B) 1
 (C) 2 (D) 3
- Q.56** The value of $\int_0^\infty \frac{\log x}{1+x^2} dx$, equals
 (A) $\frac{\pi}{2} \log 2$ (B) $-\frac{\pi}{2} \log 2$
 (C) 0 (D) $\frac{\pi}{4} \log 2$
- Q.57** The value of $\int_{-1}^{10} \operatorname{sgn}(x - [x]) dx$, where $[]$ is G.I.F., equals
 (A) 0 (B) 11
 (C) -11 (D) 12
- Q.58** The value of $\int_{-\pi}^{\pi} \frac{\cos^2 x}{1+a^x} dx$, where $a > 0$, is
 (A) π (B) $a\pi$ (C) $\frac{\pi}{2}$ (D) 2π

- Q.59** The value of $\int_0^\pi e^{\sin^2 x} \cdot \cos(2n+1)x dx$, where $n \in \mathbb{N}$, equals
 (A) 0 (B) $2n+1$
 (C) n (D) $n+1$
- Q.60** The value of $\lim_{t \rightarrow \infty} \frac{\int_0^t (\tan^{-1} x)^2 dx}{\sqrt{t^2+1}}$ is
 (A) $\frac{\pi}{4}$ (B) $\frac{\pi^2}{4}$
 (C) $\frac{\pi^2}{2}$ (D) $\frac{\pi}{2}$
- Q.61** If $I = \int_0^1 \frac{1}{\sqrt{2-x-x^2}} dx$, then which of the following is true?
 (A) $\frac{\pi}{6} < I < \frac{\pi}{4}$ (B) $I < \frac{\pi}{4}$
 (C) $I < \frac{\pi}{6}$ (D) $I > \frac{\pi}{4}$
- Q.62** If $I_n = \int_0^{\pi/4} \sec^n x dx$, then $I_{10} - \frac{8}{9} I_8 =$
 (A) $\frac{9}{16}$ (B) $\frac{25}{16}$
 (C) $\frac{16}{9}$ (D) $\frac{4}{9}$
- Q.63** The value of $\int_0^{\pi/2} \frac{dx}{1+\tan^3 x}$ is equal to
 (A) 0 (B) 1
 (C) $\frac{\pi}{2}$ (D) $\frac{\pi}{4}$
- Q.64** The value of $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x}+\sqrt{x}} dx$ is equal to
 (A) 1 (B) 0
 (C) -1 (D) $\frac{1}{2}$
- Q.65** The value of $\int_{-1}^1 x^{17} \cos^4 x dx$ is equal to
 (A) -2 (B) -1
 (C) 0 (D) 2
- Q.66** $\int_0^\pi (x \cdot \sin^2 x \cdot \cos x) dx$ is equal to
 (A) 0 (B) $\frac{2}{9}$
 (C) $-\frac{2}{9}$ (D) $-\frac{4}{9}$
- Q.67** The value of $\int_0^{1000} e^{x-[x]} dx$, where $[]$ is G.I.F., is
 (A) $\frac{e^{1000}-1}{1000}$ (B) $\frac{e^{1000}-1}{e-1}$
 (C) $1000(e-1)$ (D) $\frac{e-1}{1000}$
- Q.68** The value of $\int_2^{10} \{(x-1)(x-2)(x-3) \dots \dots (x-11)\} dx$ is
 (A) 45 (B) 55
 (C) 0 (D) 110
- Q.69** The value of $\int_{-\pi/2}^{\pi/2} \frac{dx}{e^{\sin x} + 1}$ is equal to
 (A) 0 (B) 1
 (C) $-\frac{\pi}{2}$ (D) $\frac{\pi}{2}$

- Q.70** The value of the integral $I = \int_0^1 x(1-x)^n dx$ is equal to
 (A) $\frac{1}{n+1}$ (B) $\frac{1}{n+2}$
 (C) $\frac{1}{n+1} - \frac{1}{n+2}$ (D) $\frac{1}{n+1} + \frac{1}{n+2}$
- Q.71** The value of $\int_1^5 (|x-3| + |1-x|) dx$ is equal to
 (A) 10 (B) $\frac{5}{6}$
 (C) 21 (D) 12
- Q.72** If $[]$ and $\{ \}$ represents greatest integer function and fractional function then
 $\int_{-1}^1 ([x] + \{x\} + |x|) dx$ equals
 (A) 0 (B) 1
 (C) -1 (D) $\frac{1}{2}$
- Q.73** The value of $\int_0^{\pi/2} \frac{\cos 2x}{(\sin x + \cos x)^2} dx$ is equal to
 (A) 0 (B) $\frac{\pi}{4}$
 (C) $\frac{\pi}{2}$ (D) $\frac{\pi}{6}$
- Q.74** The value of $\int_{-1/2}^{1/2} ([x] + \ln(\frac{1+x}{1-x})) dx$ is equals to (where $[.]$ represents the greatest integer function)
 (A) $-\frac{1}{2}$ (B) 0
 (C) 1 (D) $2 \log\left(\frac{1}{2}\right)$
- Q.75** The value of $\int_0^{\pi/2} \frac{\cos x dx}{1 + \cos x + \sin x}$ is equal to
 (A) $\frac{\pi}{4} + \log 2$ (B) $\frac{\pi}{4} + \frac{1}{2} \log 2$
 (C) $\pi - \frac{1}{2} \log 2$ (D) $\frac{\pi}{4} - \frac{1}{2} \log 2$
- Q.76** $\int_{-2}^0 \{x^3 + 3x^2 + 3x + 3 + (x+1)\cos(x+1)\} dx =$
 (A) -4 (B) 0
 (C) 4 (D) 6
- Q.77** $\int_{19}^{37} (\{x\}^2 + 3\sin 2\pi x) dx$, where $\{x\}$ is fractional part of x , equals
 (A) 0 (B) 6
 (C) 9 (D) 7
- Q.78** If $x^{f(x)} = e^{x-f(x)}$, then the value of integral $\int_1^2 f'(x)\{(1+\log x)^2\} dx + 1$ is
 (A) $3\log 3$ (B) $2\log 2$
 (C) $\log 2$ (D) $\log 3$
- Q.79** Let $f(x) = \min\{|x+2|, |x|, |x-2|\}$, then the value of the integral $\int_{-2}^2 f(x) dx$ is
 (A) 4 sq. units (B) 10 sq. units
 (C) 2 sq. units (D) 7 sq. units

Q.80 STATEMENT 1: $\int_0^{\frac{\pi}{2}} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx = \frac{\pi^2}{32}$

And

STATEMENT-2: $\int_0^a f(x) dx = \int_0^a f(a-x) dx$

- (A) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
 (B) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
 (C) Statement-1 is True, Statement-2 is False
 (D) Statement-1 is False, Statement-2 is True

Q.81 STATEMENT-1: $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(\log(x + \sqrt{1+x^2})) dx = 0$

And

STATEMENT-2: $\int_{-a}^a f(x) = 0$ if $f(x)$ is an even function

- (A) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
 (B) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
 (C) Statement-1 is True, Statement-2 is False
 (D) Statement-1 is False, Statement-2 is true

Q.82 STATEMENT-1: $\int_0^{\frac{\pi}{2}} \sin 2kx \cdot \cot x \cdot dx = \frac{\pi}{2}$; where $k \in \ell^+$

And

STATEMENT-2: $\frac{\sin 2kx}{\sin x} = 2[\cos x + \cos 3x + \dots + \cos(2k-1)x]$

- (A) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1
 (B) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
 (C) Statement-1 is True, Statement-2 is False
 (D) Statement-1 is False, Statement-2 is True

$$|x| = \begin{cases} x & ; \quad x \geq 0 \\ -x & ; \quad x < 0 \end{cases}$$

and $[.]$ represents greatest integer function less than or equal to x , then answer the Q.21 to 25.

Q.83 $\int_0^4 (|x-1| + |x-3|) dx$ equals

- (A) 5 (B) 8
 (C) 10 (D) 9

Q.84 $\int_{0.5}^{4.5} [x] dx + \int_{-1}^1 |x| dx$ equal to

- (A) 6 (B) 7
 (C) 8 (D) 9

Q.85 $\int_0^{\frac{\pi}{3}} [\sqrt{3} \tan x] dx$ is equal to

- (A) $\frac{\pi}{2} - \tan^{-1} \frac{2}{\sqrt{3}}$ (B) $\frac{5\pi}{6} - \tan^{-1} \frac{2}{\sqrt{3}}$
 (C) $\frac{5\pi}{6}$ (D) $\frac{\pi}{6}$

- Q.86** $\int_{-5}^5 (|x| + |x + 1|)dx$ is equal to
 (A) 31 (B) 51
 (C) 61 (D) 91
- Q.87** $\int_0^{100} [\sqrt{x}]dx$
 (A) 585 (B) 605
 (C) 615 (D) 650
- Q.88** The value of $\int_0^a \frac{dx}{x + \sqrt{a^2 - x^2}}$ is equal to
 (A) $\frac{\pi}{4}$ (B) $\frac{\pi}{2}$
 (C) π (D) $\frac{\pi}{6}$
- Q.89** The value of $\int_0^{\pi/2n} \frac{dx}{1 + \tan^n(nx)}$ is equal to, ($n \in \mathbb{N}$)
 (A) 0 (B) $\frac{\pi}{4n}$
 (C) $\frac{\pi}{2n}$ (D) $\frac{\pi}{2}$
- Q.90** $f: \mathbb{R} \rightarrow \mathbb{R}, g: \mathbb{R} \rightarrow \mathbb{R}$ are continuous functions.
 The value of integral $\int_{-\pi/2}^{\pi/2} [f(x) + f(-x)][g(x) - g(-x)]dx$ is equal to
 (A) π (B) 1
 (C) -1 (D) 0
- Q.91** If $f(x) = \begin{cases} e^{\cos x} \sin x & \text{for } |x| \leq 2 \\ 2 & \text{otherwise} \end{cases}$ then the value of
 (A) 0 (B) 1
 (C) 2 (D) 3
- Q.92** If $I_1 = \int_0^{n\pi} f(|\cos x|)dx$ and $I_2 = \int_0^{5\pi} f(|\cos x|)dx$, where $n \in \mathbb{N}$ and $f(x)$ is a function such that $I_2 \neq 0$, then which of the following must be true.
 (A) $\frac{I_1}{I_2} = \frac{5}{n}$ (B) $\frac{I_1}{I_2} = \frac{n}{5}$
 (C) $I_1 + I_2 = n + 5$ (D) $I_1 - I_2 = n - 5$
- Q.93** If $I_n = \int_0^{\pi/4} \tan^n x dx$ where $n \in \mathbb{N}$, then $\frac{1}{I_2 + I_4}, \frac{1}{I_3 + I_5}, \frac{1}{I_4 + I_6}, \dots$ form
 (A) An A.P. (B) A G.P.
 (C) A H.P. (D) None of these
- Q.94** The value of $\int_{2010\pi}^{2010\pi + \frac{\pi}{3}} (\sin x + \cos x)dx$ is
 (A) $\sqrt{2} - 1$ (B) $\sqrt{3} - 1$
 (C) $\sqrt{3} + 1$ (D) $\sqrt{2} + 1$
- Q.95** Let $\int_a^b f(x)dx = \int_{a+c}^{b+c} f(x-c)dx$. Then the value of $\int_0^\pi \sin^{2010} x \cdot \cos^{2009} x dx$ is
 (A) 2010 (B) 2009
 (C) 0 (D) 2011

- Q.96** If $\int_0^x t f(t) dt = \sin x - x \cos x - \frac{x^2}{2}$, $\forall x \in \mathbb{R} - \{0\}$. Then the value of $f\left(\frac{\pi}{6}\right)$ is
 (A) 0 (B) 1
 (C) $-\frac{1}{2}$ (D) 10
- Q.97** The value of the integral $\int_{-201}^{2012\pi} \left\{ \frac{d}{dx} \int_0^{x^2} (\cos t^2) dt \right\} dx$ is
 (A) 2012π (B) 4024π
 (C) 0 (D) -2012π
- Q.98** If $\int \frac{dx}{x(x^2+1)^3} = \frac{1}{4(f(x))^2} + \frac{1}{2f(x)} + \frac{1}{2} \ln\left(\frac{x^2}{f(x)}\right) + c$ then $\lim_{x \rightarrow 0} (f(x))^{1/x}$ is
 (A) 3 (B) $1 + \int_0^1 e^x \cdot dx$
 (C) e^2 (D) $\int_0^{\pi/2} \sin x dx$
- Q.99** $\int_{1/2}^{7/2} \left[\frac{1}{2} (|x-3| + |1-x|-4) \right] dx$ equals
 (A) $-\frac{3}{2}$ (B) $\frac{9}{8}$
 (C) $\frac{1}{4}$ (D) $-\frac{11}{4}$
- Q.100** Let a, b, c be non-zero real numbers such that $\int_0^1 (1 + \cos^8 x) (ax^2 + bx + c) dx = \int_0^2 (1 + \cos^8 x) (ax^2 + bx + c) dx$, then the equation $ax^2 + bx + c = 0$ Has
 (A) No root in (0,2) (B) At least one root in (0,2)
 (C) Two roots in (0,2) (D) none of these

EXERCISE LEVEL -II


 EL- II

- Q.1 Find the value of $\int_{-1}^1 x^3 \cdot e^{x^4} dx$.
- Q.2 Find the value of $\int_{-1}^1 x|x| dx$.
- Q.3 Find the value of $\int_{-1}^2 \frac{|x|}{x} dx$.
- Q.4 Find the value of $\int_3^6 2[x] dx$, where $[.]$ denotes greatest integer function.
- Q.5 Find the value of $\int_0^{\pi/4} \sec^2 x dx$.
- Q.6 Evaluate the value of $\int_0^4 \frac{1}{\sqrt{x^2+2x+3}} dx$.
- Q.7 Evaluate the value of $\int_0^1 \frac{e^x}{1+e^{2x}} dx$.
- Q.8 Evaluate the value of $\int_{-1}^1 f(x) dx$, where $f(x) = \begin{cases} 1-2x, & x \leq 0 \\ 1+2x, & x > 0 \end{cases}$
- Q.9 Evaluate the value of $\int_0^{\pi/2} \frac{\sqrt{\cos x}}{\sqrt{\cos x} + \sqrt{\sin x}} dx$.
- Q.10 Evaluate the value of $\int_0^1 \sin^{-1}\left(\frac{2x}{1+x^2}\right) dx$.
- Q.11 Evaluate the value of $\int_0^{\pi} \frac{x}{1+\sin x} dx$.
- Q.12 Evaluate $\int_0^{\pi/4} \frac{\sin x + \cos x}{9+16s-2x} dx$
- Q.13 Evaluate $\int_0^{2\pi} |\cos x| dx$
- Q.14 Evaluate $\int_0^{\pi/4} \frac{dx}{1+\cos 2x}$.
- Q.15 Evaluate $\int_{1/3}^1 \frac{(x-x^3)^{1/3}}{x^4} dx$
- Q.16 Evaluate $\int_0^{\pi/4} \log(1 + \tan x) dx$
- Q.17 Evaluate $\int_0^{\pi} \frac{x dx}{1+\cos^2 x}$
- Q.18 Evaluate $\int_0^{\pi/2} \ln \sin 2x dx$
- Q.19 Evaluate $\int_{-\pi/4}^{\pi/4} x^3 \sin^2 x dx$
- Q.20 Evaluate $\int_{-\pi/2}^{\pi/2} \sin^2 x dx$
- Q.21 Evaluate $\int_0^1 x^2 dx$ as the limit of a sum.
- Q.22 Evaluate $\int_0^{\pi/4} \frac{\sin x + \cos x}{9+16s-2x} dx$
- Q.23 Evaluate $\int_0^{2\pi} |\cos x| dx$
- Q.24 Evaluate $\int_0^{\pi} \frac{e^{\cos x}}{e^{\cos x} + e^{-\cos x}} dx$
- Q.25 Evaluate $\int_{-\pi/4}^{\pi/4} \frac{x + \frac{\pi}{4}}{2 - \cos 2x} dx$

ANSWER KEY – LEVEL – I

Q.	1	2	3	4	5	6	7	8	9	10
Ans.	B	A	D	D	C	C	B	A	B	A
Q.	11	12	13	14	15	16	17	18	19	20
Ans.	D	D	B	B	D	A	C	B	C	D
Q.	21	22	23	24	25	26	27	28	29	30
Ans.	A	C	C	A	A	A	D	C	B	B
Q.	31	32	33	34	35	36	37	38	39	40
Ans.	B	D	C	A	B	C	B	C	D	C
Q.	41	42	43	44	45	46	47	48	49	50
Ans.	C	B	A	B	A	C	C	C	B	C
Q.	51	52	53	54	55	56	57	58	59	60
Ans.	d	A	A	B	B	C	B	C	A	B
Q.	61	62	63	64	65	66	67	68	69	70
Ans.	D	C	D	D	C	D	C	C	D	C
Q.	71	72	73	74	75	76	77	78	79	80
Ans.	D	B	A	A	D	C	B	B	C	D
Q.	81	82	83	84	85	86	87	88	89	90
Ans.	C	A	C	D	A	B	C	A	B	D
Q.	91	92	93	94	95	96	97	98	99	100
Ans.	C	B	A	B	C	C	C	D	D	B