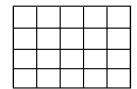


Marked questions are recommended for Revision.

PART - I: SUBJECTIVE QUESTIONS

Section (A): Problems based on Classical definition of Probability (PRCD)

- **A-1.** Write the sample space of the following experiment
 - (i) 'Three coins are tossed'.
 - (ii) 'Selection of two children from a group of 3 boys and 2 girls without replacement'.
- **A-2.** There are three events A, B, C, one of which must, and only one can, happen; the odds are 8 to 3 against A, 5 to 2 against B: find the odds against C.
- **A-3.** If the letters of the word BANANA are arranged randomly, then find the probability that the word thus formed does not contain the pattern BAN.
- **A-4.** Nine cards are labelled 0, 1, 2, 3, 4, 5, 6, 7, 8. Two cards are drawn at random and put on a table in a sucessive order, and then the resulting number is read say 07(seven), 42(fourty two) and so on. Find the probability that the number is even.
- **A-5.** Three persons A, B and C speak at a function along with 5 other persons. If the persons speak at random, find the probability that A speaks before B and B speaks before C
- **A-6.** (i) A rectangle is randomly selected from the grid of equally spaced squares as shown.



Find the probability that the rectangle is a square.

- (ii) Three of the six vertices of a regular hexagon are chosen at random. Then the probability that the triangle with three vertices is equilateral is 'p' then 100p equals
- **A-7.** In throwing a pair of dice, find whether the two events
 - (i) E₁: 'coming up of an odd number on first dice' and E₂: 'coming up of a total of 8'.
 - (ii) E₁: 'coming up of 4 on first dice' and E₂: 'coming up of 5 on the second dice'. are mutually exclusive or not
- **A-8.** In throwing of a pair of dice, find the probability of the event: total is 'not 8' and 'not 11'.
- A-9. Before a race the chance of three runners, A, B, C were estimated to be proportional to 5, 3, 2, but during the race A meets with an accident which reduces his chance to 1/3. What are the respective chance of B and C now?
- **A-10.** Tickets are numbered from 1 to 100. One ticket is picked up at random. Then find the probability that the ticket picked up has a number which is divisible by 5 or 8.
- A-11. Three cards are drawn at random from a pack of well shuffled 52 cards. Find the probability that
 - (i) all the three cards are of the same suit;
 - (ii) one is a king, the other is a queen and the third a jack.
- **A-12.** In a throw of a pair of dice, then find the probability of 'A total of 8 but not 11'.

- **A-13.** Six boys and six girls sit in a row at random. Find the probability that boys and girls sit alternately
- **A-14.** Four persons draw 4 cards from an ordinary pack find the chance
 - (1) that a card is of each suit
 - (2) that no two cards are of equal value.

Section (B): Problems based on venn diagram & set theory (PRVD)

B-1. Prove that

$$P(A-B) = P(A) - P(A \cap B) = P(A \cup B) - P(B) = P(A \cap \overline{B}) = 1 - P(\overline{A} \cup B)$$

B-2 If P(A) = 0.7 and $P(A \cap B) = 0.5$ find

(i) $P(A-\bar{B})$

(ii) $P(\overline{A} \cup B)$

B-3. If P(A) = 0.4, P(B) = 0.48 and $P(A \cap B) = 0.16$, then find the value of each of the following:

(i) $P(A \cup B)$

(ii) $P(A' \cap B)$

(iii) $P(A' \cap B')$

(iv) $P((A \cap B') \cup (A' \cap B))$

B-4. There are three clubs A,B,C in a town with 40, 50, 60 members respectively 10 people are members of all the three clubs, 70 members belong to only one club. A member is randomly selected. Find the probability that he has membership of exactly two clubs

Section (C): Problems based on Conditional Probability/ Total probability & Bayes' theorem

- C-1. (i) In a two child family, one child is a boy. What is the probability that the other child is a girl?
 - (ii) If the older child is a boy, then probability that the second child is a girl is
- **C-2.** A fair dice is thrown untill a score of less than 5 points is obtained. Find the probability of obtaining not less than 2 points on the last throw.
- **C-3.** A card is drawn from a well shuffled ordinary deck of 52 playing cards. Find the probability that the card drawn is :
 - (i) A king or a queen
- (ii) A king or a spade
- **C-4.** The odds against a certain event are 5 to 2, and the odds in favor of another event independent of the former are 6 to 5 : find the chance that one at least of the events will happen.
- **C-5.** A, B, C in order draws a card from a pack of cards, replacing them after each draw, on condition that the first who draws a spade shall win a prize : find their respective chances.
- **C-6.** 6 persons A,B,C,D,E,F are arranged in row. Find the conditional probability that C & D are separated given that A & B are together.
- **C-7.** There are 5 brilliant students in class XI and 8 brilliant students in class XII. Each class has 50 students. The odds in favour of choosing the class XI are 2 : 3. One of the classes is chosen randomly and then a student is randomly selected. Find the probability of selecting a brilliant student.
- **C-8.** Box I contains 5 red and 2 blue balls while box II contains 2 red and 6 blue balls. A fair coin is tossed. If it turns up head, a ball is drawn from box–I, else a ball is drawn from box–II. Find the probability of each of the following:
 - (i) A red ball is drawn
 - (ii) Ball drawn is from box-I if it is blue
- **C-9.** Two cards are drawn successively from a well-shuffled ordinary deck of 52-playing cards without replacement and is noted that the second card is a king. Find the probability of the event 'first card is also a king'.

Probabilit	\mathbf{v}

A-1.

- C-10. 12 cards, numbered 1 to 12, are placed in a box, mixed up throughly and then a card is drawn at random from the box. If it is known that the number on the drawn card is more than 3, find the probability that it is an even number.
- In a building programme the event that all the materials will be delivered at the correct time is M, and the event that the building programme will be completed on time is F. Given that P(M) = 0.8 & $P(M \cap F) = 0.65$. If P(F) = 0.7, find the probability that the building programme will be completed on time if all the materials are not delivered at the correct time.

Section (D): Problem based on Binomial Distribution / Expectation / mean & Variance

- D-1. South African cricket captain lost the toss of a coin 13 times out of 14. Then find the chance of this happening.
- D-2. In an examination of 10 multiple choice questions (1 or more can be correct out of 4 options). A student decides to mark the answers at random. Find the probability that he gets exactly two questions correct. (Assume he attempts all the questions)
- D-3. Three cards are drawn successively with replacement from a well shuffled deck of 52 playing cards. If getting a card of spade is considered a success, find the probability distribution of the number of successes.
- A had in his pocket a 100 Rupee and four 10 rupee notes; taking out two notes at random he promises D-4. to give them to B and C. What is the worth of C's expectation?
- D-5. A box contains 2 red and 3 blue balls. Two balls are drawn successively with replacement. If getting 'a red ball on first draw and a blue ball on second draw' is considered a success, then write the probability distribution of successes. It is given that the above experiment is performed 3-times,
- D-6. A coin is tossed 5-times. Find the mean and variance of the probability distribution of appearance of heads on the tosses.

PART - II: ONLY ONE OPTION CORRECT TYPE

In drawing of a card from a well shuffled ordinary deck of playing cards the events 'card drawn is

(B) equally likely

(D) none of these

Section (A): Problems based on Classical definition of Probability (PRCD)

spade' and 'card drawn is an ace' are

(C) forming an exhaustive system

(A) mutually exclusive

A-2.		er using the digits 1, 2, he number will be divisite		ritten randomly without re	petition. The
	(A) 1/9	(B) 1/2	(C) 1	(D) 9!/9 ⁹	
A-3.	Entries of a 2 × value is	2 determinant are chose	en from the set {-1, 1}. The	he probability that determin	ant has zero
	(A) $\frac{1}{4}$	(B) $\frac{1}{3}$	(C) $\frac{1}{2}$	(D) none of these	

A dice is thrown a fixed number of times. If probability of getting even number 3 times is same as the probability of getting even number 4 times, then probability of getting even number exactly once is

	(A) $\frac{1}{4}$	(B) $\frac{3}{128}$	(C) $\frac{5}{64}$	(D) $\frac{7}{128}$	
A-5.	A and B throw with t	wo dice; if A throws 9	9, then B's chance of thr	owing a higher number e	quals

(B) $\frac{3}{}$

(A) $\frac{1}{6}$ (B) $\frac{1}{3}$

		-	
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A-6. 🖎	If an integer q is chose equation $x^2 + qx + \frac{3q}{4}$	ne probability that the roots of the		
	(A) $\frac{16}{21}$	(B) $\frac{15}{21}$	(C) $\frac{14}{21}$	(D) $\frac{17}{21}$
A-7.	bridge, in which 9 card	eard combination from a parameter of the same suit, is $(B) \frac{4! \cdot {}^{13} C_9 \cdot {}^{39} C_4}{{}^{52}C_{12}}$, , ,	is is dealt to a player in a game of (D) $2^{\frac{13}{12}}$ C ₉ . 39 C ₄
A-8.≿	313	~13	~ 13	respectively. A ticket is drawn &

replaced. Then the chance that after 4 drawings the sum of the numbers drawn is 8 is:

(A) 165/2401

(B) 149/2401

(C) 3/49

(D) 1/49

A-9. A & B having equal skill, are playing a game of best of 5 points. After A has won two points & B has won one point, the probability that A will win the game is:

(A) 1/2
(B) 2/3
(C) 3/4
(D) 2/5

Section (B): Problems based on venn diagram & set theory (PRVD)

B-1. If two subsets A and B of set S containing n elements are selected at random, then the probability that $A \cap B = \phi$ and $A \cup B = S$ is

(A)
$$\frac{1}{2}$$
 (B) $\frac{1}{2^n}$ (C) $\left(\frac{3}{4}\right)^4$ (D) $\frac{1}{3^n}$

B-2. If $P(A) = \frac{3}{5}$ and $P(B) = \frac{2}{3}$ then –

(i) The range of values of $P(A \cap B)$ is $(A) \left[\frac{2}{5}, \frac{9}{10} \right] \qquad (B) \left[\frac{2}{3}, 1 \right] \qquad (C) \left[0, \frac{1}{3} \right] \qquad (D) \left[\frac{4}{15}, \frac{3}{5} \right]$

(ii) The range of values of P(A \cup B) is (A) $\left[\frac{2}{5}, \frac{9}{10}\right]$ (B) $\left[\frac{2}{3}, 1\right]$ (C) $\left[0, \frac{1}{3}\right]$ (D) $\left[\frac{4}{15}, \frac{3}{5}\right]$

(iii) The range of values of P(A \cap B') is $(A) \left[\frac{2}{5}, \frac{9}{10} \right] \qquad (B) \left[\frac{2}{3}, 1 \right] \qquad (C) \left[0, \frac{1}{3} \right] \qquad (D) \left[\frac{4}{15}, \frac{3}{5} \right]$

B-3 Let X = {1,2,, 10}, if set A and B are formed from elements of X the probability that n (A \cap B) = 2, is (A) $\frac{^{10}C_2}{4^{10}}$ (B) $5.\left(\frac{3}{4}\right)^{10}$ (C) $\left(\frac{3}{4}\right)^{10}$ (D) $\frac{3^8}{4^{10}}$

B-4 If probability that exactly one of events A, B, C occurs, is 0.6 and probability that none of A,B,C occur is 0.2, then probability that atleast two of A,B,C occur is
(A) 0.6 (B) 0.4 (C) 0.8 (D) 0.2

Section (C): Problems based on Conditional Probability/ Total probability & Bayes' theorem

C-1. The odds that a book will be favourably reviewed by three independent critics are 5 to 2, 4 to 3, and 3 to 4 respectively. Then the probability that of the three reviews a majority will be favourable.

(A) $\frac{163}{343}$ (B) $\frac{209}{343}$ (C) $\frac{209}{387}$ (D) $\frac{208}{387}$

Probability	
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C-2.	In throwing a pair of dice, the events 'coming up of 6 on Ist dice' and 'a total of 7 on both the dice' are (A) mutually exclusive (B) forming an exhaustive system (C) independent (D) dependent							
C-3.	A dice is thrown twice and the sum of the numbers appearing is observed to be 8. The conditional probability that the number 5 has appeared at least once is							
	(A) 1/6	(B) 2/5	5	(C) 3	3/5	(D)	1/2	
C-4.	An instrument cons of the first unit is 0. that "only the first u	.9 and that only failed &	of the secor the second	nd unit is 0.	8. The instr			
	(A) $\frac{1}{7}$	(B) $\frac{2}{7}$		(C)	3	(D)	$\frac{4}{7}$	
C-5.	A pack of cards is o	counted with	n face down	nwards. It is	found that	one card is	,	ne card is drawn
	and is found to be r		-	-			25	
	(A) $\frac{25}{51}$	(B) $\frac{26}{5}$	<u>^</u> 1	(C) -	<u>.</u> 2	(D)	25 52	
C-6.2s	Pal's gardner is not dependable, the probability that he will forgot to water the rose bush is 2/3. The rose bush is in questionable condition. Any how if watered, the probability of its withering is 1/2 & if not watered then the probability of its withering is 3/4. Pal went out of station & after returning he finds that rose bush has withered. Then the probability that the gardner did not water the rose bush is. (A) 3/4 (B) 2/5 (C) 1/4 (D) 1/2							ng is 1/2 & if not ing he finds that
C-7.a	A dice is weighted:	so that the p	orobability o	of different fa	aces to turn	up is as giv	ren	
	Number	1	2	3	4	5	6	
	Probability	0.2	0.1	0.1	0.3	0.1	0.2	
	If P(A/B) = p ₁ and F Take the events A, (A) $\frac{2}{3}$, $\frac{1}{3}$, $\frac{1}{4}$	B & C as A	$= \{1, 2, 3\},\$	$B = \{2, 3, 5\}$	and C = {2	2, 4, 6}		re -
Section	on (D) : Problem	based o	n Binomi	al Distrib	ution / Ex	xpectatio	n / mean	& Variance
D-1.	A bag contains 2 w drawn. The probabi (A) 4/81		ast 4 of the	balls drawr		is:	replaced b	efore another is
D-2.	In a series of 3 in	` ,		` ,		` ,		as large as the
D-2.	probability of 3 succession (A) 1/5		probability		ss in each tr	ial is:	4/5	as large as the
D-3.	A coin is tossed n t	imes, what i	s the chand	ce that the h	ead will pre	sent itself a	ın odd numl	per of times.
	(A) $\frac{1}{2}$	(B) $\frac{2}{3}$		(C) -	<u>1</u> 4	(D)	$\frac{2}{5}$	
D-4.	From a bag contarandomly then the v		expectation	۱.	pee coins		Rs. 3.20	o draw 2 coins
D-5.	A & B throw with or has the first throw t (A) 50 & 49		spective ex	pectations of		e:	ayer who fii	rst throws 4. If A
	. ,	、 /		` '		()		

- **D-6.** A fair coin is tossed 99 times. If X is the number of times heads occur, if P(X = r) is maximum then sum of possible values of r is
 - (A) 98
- (B) 99
- (C) 101
- (D) 104

PART - III: MATCH THE COLUMN

- 1. Column I Column II
 - (A) If the probability that units digit in square of an even integer is 4 is p, then the value of 5p is
- (p) 1
- (B) If A and B are independent events and $P(A \cap B) = \frac{1}{6}$,
- (q) 2

- $P(A) = \frac{1}{3}$, then $6P\left(\frac{B}{\overline{A}}\right) =$
- (C) One mapping is selected at random from all mappings of the set $S = \{1, 2, 3,, n\}$ into itself. If the probability that the mapping is one-one is $\frac{3}{32}$, then the value of n is
- (r) 3
- (D) A boy has 20% chance of hitting at a target. Let p denote the probability of hitting the target for the first time at the n^{th} trial. If p satisfies the inequality $625p^2-175p+12<0$, then value of n is
- (s) 4
- 2. Column I
 - (A) A pair of dice is thrown. If total of numbers turned up on both the dice is 8, then the probability that the number turn up on the second dice is 5' is

- (p) 5/16
- (B) A box contains 4 white and 3 black balls. Two balls are drawn successively and is found that second ball is white, then the probability that 1st ball is also white is
- (q) 1/3
- (C) A biased coin with probability p, 0 < p < 1 of heads is tossed until a head appears for the first time. If the probability that the number of tosses required is even is
- (r) $\frac{1}{2}$
- probability that the number of tosses required is even is 2/5, then p equals

 (D) A coin whose faces are marked 3 and 5 is tossed 4 times : what
- (s) $\frac{1}{2}$
- is the probability that the sum of the numbers thrown being less, than 15?

Exercise-2

Marked questions are recommended for Revision.

PART - I: ONLY ONE OPTION CORRECT TYPE

1.🔈	A local post office is to send M telegrams which are distributed at random over N communication
	channels, (N > M). Each telegram is sent over any channel with equal probability. Chance that not more
	than one telegram will be sent over each channel is:

(A)
$$\frac{{}^{N}C_{M} \cdot M!}{N^{M}}$$

(B)
$$\frac{{}^{N}C_{M} \cdot N}{{}^{M}{}^{N}}$$

(A)
$$\frac{{}^{N}C_{M} \cdot M!}{N^{M}}$$
 (B) $\frac{{}^{N}C_{M} \cdot N!}{M^{N}}$ (C) $1 - \frac{{}^{N}C_{M} \cdot M!}{M^{N}}$ (D) $1 - \frac{{}^{N}C_{M} \cdot N!}{N^{M}}$

(D)
$$1 - \frac{{}^{N}C_{M} \cdot N!}{N^{M}}$$

A cube painted red on all sides, is cut into 125 equal small cubes. A small cube when picked up is 2. found to show red colour on one of its faces. Then the probability that two more faces also show red colour

(A)
$$\frac{4}{49}$$

(B)
$$\frac{4}{120}$$

(C)
$$\frac{8}{49}$$

(D)
$$\frac{3}{49}$$

A car is parked by an owner in a parking lot of 25 cars in a row, including his car not at either end. On 3.≿ his return he finds that exactly 15 placed are still occupied. The probability that both the neighboring places are empty is

(A)
$$\frac{91}{276}$$

(B)
$$\frac{15}{184}$$

(C)
$$\frac{15}{92}$$

(D)
$$\frac{17}{92}$$

A has 3 tickets in a lottery containing 3 prizes and 9 blanks; B has 2 tickets in a lottery containing 2 4.3 prizes and 6 blanks. Compare their chances of success

A 2n digit number starts with 2 and all its digits are prime, then the probability that the sum of all 2 5. consecutive digits of the number is prime, is

(A)
$$4 \times 2^{3n}$$

(B)
$$4 \times 2^{-3n}$$

6. A fair coin is tossed eight times, then find the probability that resulting sequence of heads and tails looks the same when viewed from the beginning or from the end.

7.3 An urn contains 'm' green and 'n' red balls. K (< m, n) balls are drawn and laid aside, their colur being ignored. Then one more ball is drawn. Then the probability that it is green.

(A)
$$\frac{m}{m+n}$$

(B)
$$\frac{n}{m+n}$$

(B)
$$\frac{n}{m+n}$$
 (C) $\frac{2n}{m+n}$

(D)
$$\frac{3n}{m+n}$$

8. S In a regular decagon find the probability that the two diagonal chosen at random will intersect inside the polygon.

(A)
$$\frac{6}{17}$$

(B)
$$\frac{12}{17}$$

(C)
$$\frac{5}{17}$$

(D)
$$\frac{3}{17}$$

An urn contains m white and n black balls. A ball is drawn at random and is put back into the urn along 9.3 with k additional balls of the same colour as that of the ball drawn. A ball is again drawn at random. Then the probability that the ball drawn now is white.

(A)
$$\frac{m}{m+n}$$

(B)
$$\frac{n}{m+n}$$

(C)
$$\frac{2n}{m+n}$$

(D)
$$\frac{2m}{m+n}$$

10. There are two urns. There are m white & n black balls in the first urn and p white & g black balls in the second urn. One ball is taken from the first urn & placed into the second. The probability of drawing a white ball from the second urn is -

(A)
$$\frac{(p+1)n+pm}{(m+n)(p+q+1)}$$

(B)
$$\frac{(p+1)m+pn}{(m+n)(p-q+1)}$$

(C)
$$\frac{(p+1)m+2pn}{(m+n)(p+q+1)}$$

(D)
$$\frac{(p+1)m+pn}{(m+n)(p+q+1)}$$

- 11. The chance that the top card in the deck is a diamond given that the fourth card from the top is a eight in well shuffled deck.
- (C) $\frac{1}{2}$
- A fair coin is tossed 9 times the probability that at least 5 consecutive heads occurs is 12.2
 - (A) $\frac{5}{64}$
- (B) $\frac{3}{32}$
- (C) ${}^{9}C_{5}\left(\frac{1}{2}\right)^{9}$ (D) $\frac{5}{2^{9}}$
- 13. A man has 10 coins and one of them is known to have two heads. He takes one at random and tosses it 5 times and it always falls head. Then the chance that it is the coins with two heads.
- (B) $\frac{32}{51}$
- (C) $\frac{23}{32}$
- 14. 2 hunters A & B shot at a bear simultaneously. The bear was shot dead with only one hole in its hide. Probability of A shooting the bear 0.8 & that of B shooting the bear is 0.4. The hide was sold for Rs. 280/-. If this sum of money is divided between A & B in a fair way, then find the share of A (A) 130 (B) 240
- A number is chosen at random from the numbers 10 to 99. A number whose product of digits is 12 will 15. be called a good number. If he choose three numbers with replacement then the probability that he will choose a good number at least once is
 - (A) 0.872
- (B) 0.127
- (C) 0.562
- (D) 0.461

PART - II: SINGLE AND DOUBLE VALUE INTEGER TYPE

- Seven digits from the number 1, 2, 3, 4, 5, 6, 7, 8 & 9 are written in random order. The probability that 1. this seven digit number is divisible by 9 is $\frac{p}{q}$ then (p + q) equals. (Where p & q are co-prime natural numbers)
- Three numbers are chosen at random without replacement from {1, 2, 3,....., 10}. The probability that 2. the minimum of the chosen numbers is 3 or their maximum is 7 is $\frac{p}{q}$ then (q-2p) equals.
 - (Where p & g are co-prime natural numbers)
- In a multiple choice question there are 4 alternative answers of which 1, 2, 3 or all may be correct. A 3.3 candidate will get marks in the question only if he ticks all the correct answer. The candidate decides to tick answers at random. If he is allowed upto 5 chances to answer the question, If the probability that he will get the marks in the question is p then 3p equals
- 4. 3 firemen X, Y and Z shoot at a common target. The probabilities that X and Y can hit the target are 2/3 and 3/4 respectively. If the probability that exactly two bullets are found on the target is 11/24, then the probability of Z to hit the target is ' λ ' then 6λ equals

- A mapping is selected at random from all the mappings defined on the set. A consisting of three distinct elements. Probability that the mapping selected is one to one is $\frac{p}{q}$ (where p and q are co-prime natural numbers) then p + q is
- 6.3 A card is drawn from a pack, the card is replaced & the pack shuffled. If this is done 6 times, the probability that the cards drawn are 2 hearts, 2 diamonds & 2 black cards is $\frac{p}{q}$ then total number of proper divisors of (pq). (Where p & q are co-prime natural numbers):
- 7. There is a three volume dictionary among 40 books arranged on a shelf in random order. Then the raciprocal of probability of these volumes standing in increasing order from left to right (the volumes are not necessarily kept side by side) is
- 8. There are 4 urns. The first urn contains 1 white & 1 black ball, the second urn contains 2 white & 3 black balls, the third urn contains 3 white & 5 black balls & the fourth urn contains 4 white & 7 black balls. The selection of each urn is not equally likely. The probability of selecting ith urn is $\frac{i^2 + 1}{34}$ (i=1,2,3, 4). If we randomly select one of the urns & draw a ball, then the probability of ball being white is $\frac{p}{q}$ then sum of digits of p is. (Where p & q are co-prime natural numbers):
- 9.> In a Nigerian hotel, among the english speaking people 40% are English & 60% Americans. The English & American spellings are "RIGOUR" & "RIGOR" respectively. An English speaking person in the hotel writes this word. A letter from this word is chosen at random & found to be a vowel. If the probability that the writer is an Englishman is a/b, then (b − a) equals. (Where a & b are co-prime natural numbers)
- 10. Mr. Modi is a professional tea taster. When given a high grade tea, he will identify it with probability 0.9 correctly as high grade and will mistake it for a low grade tea with probability 0.1. When given a low grade tea, he will identify it with probability 0.8 correctly as low grade tea and will mistake it for a high grade tea with probability 0.2. Suppose that Mr. Modi is given ten unlabelled cups of tea, three with high grade and seven with low grade tea. He randomly picks a cup, tries the tea and solemnly says "high grade tea". If the probability that the tea he tasted was low grade tea is express in form of a/b then (3a b) equals. (Where a & b are co-prime natural numbers)
- A gambler has one rupee in his pocket. He tosses an unbiased normal coin unless either he is ruined or unless the coin has been tossed for a maximum of five times. If for each head he wins a rupee and for each tail he looses a rupee, then if the probability that the gambler is ruined is $\frac{p}{q}$ (where p and q are co-prime natural numbers) then p + q is
- 3 cards are given, one of them is red on both sides, one is blue on both sides & one is blue on one side and red on the other side. One of them is chosen randomly & put on the table. It shows red colour on the upper side. If probability of the other side of the card being red is $\frac{p}{q}$ (where p and q are co-prime natural numbers) then q p is
- 13. In a purse there are 10 coins, all 5 paise except one which is a rupee. In another purse there are 10 coins all 5 paise. 9 coins are taken out from the former purse & put into the latter & then 9 coins are taken out from the latter & put into the former. Then the chance that the rupee is still in the first purse is p then 19p 9 equals:

- 14. A Teacher wrote either of words "PARALLELOGRAM" or "PARALLELOPIPED" on board but due to malfunction of marker words is not properly written and only two consecutive letters "RA" are visible then the chance that the written word is "PARALLELOGRAM" is $\frac{p}{q}$ then (p + q) equals. (Where p & q are co-prime natural numbers):
- The numbers 'a and b' are randomly selected from the set of natural numbers. Probability that the 15.2 number $3^a + 7^b$ has a digit equal to 8 at the units place, is $\frac{p}{q}$ then p + q is : (Where p & q are co-prime natural numbers)
- 16. Suppose that of all used cars of a particular year, 30% have bad brakes. You are considering buying a used car of that year. You take the car to a mechanic to have the brakes checked. The chance that the mechanic will give you wrong report is 20%. Assuming that the car you take to the mechanic is selected "at random" from the population of cars of that year. The odds in favor of chance that the car's brakes are good given that the mechanic says its brakes are good is m: n then (m - 7n) equals. (Where m & n are co-prime natural numbers)
- 17. A bag contains (n + 1) coins. It is known that one of these coins has a head on both sides, whereas the other coins are normal. One of these coins is selected at random & tossed. If the probability that the toss results in head, is 7/12, then the value of n is.
- 18. In a certain factory machines A, B and C produce bolts of their production A, B and C produce 2%, 1% and 3% defective bolts respectively. Machine A produces 35% of the total output of bolts machine B produces 25% and machine C produces 40%. A bolts is chosen at random from the factory's production and its found to be defective. The odds in favor that it was produced on machine C is m:n then (m –n) equals. (Where m & n are co-prime natural numbers)
- In each of a set of games it is 2 to 1 in favor of the winner of the previous game. If the probabilty that 19. the player who wins the first game shall win three at least of the next four is $\frac{p}{q}$ then pq equals : (Where p & q are co-prime natural numbers)
- A couple has one or two or three children with probability $\frac{1}{4}$, $\frac{1}{2}$ and $\frac{1}{4}$ respectively. Probability of a 20. couple having exactly four grandchildren in such a type of society is $\frac{p}{q}$ then sum of digit of q equals. (Where p & q are co-prime natural numbers)

PART - III: ONE OR MORE THAN ONE OPTIONS CORRECT TYPE

- 1. In throwing a dice let A be the event 'coming up of an odd number', B be the event 'coming up of an even number', C be the event 'coming up of a number ≥ 4' and D be the event 'coming up of a number < 3',
 - (A) A and B are mutually exclusive and exhautive
 - (B) A and C are mutually exclusive and exhautive
 - (C) A, C and D form an exhautive system
 - (D) B, C and D form an exhautive system
- 2. If M & N are any two events, then which one of the following represents the probability of the occurence of exactly one of them?

(A)
$$P(M) + P(N) - 2P(M \cap N)$$

(B)
$$P(M) + P(N) - P(M \cap N)$$

$$\begin{array}{lll} \text{(A) P (M)} + \text{P (N)} - 2 \text{P (M} \cap \text{N)} & \text{(B) P (M)} + \text{P (N)} - \text{P (M} \cap \text{N)} \\ \text{(C) P (\overline{M})} + \text{P (\overline{N})} - 2 \text{P (\overline{M} \cap N)} & \text{(D) P (M \cap N$)} + \text{P ($\overline{M}$ \cap N)} \\ \end{array}$$

(D) P
$$(M \cap \overline{N}) + P (\overline{M} \cap N)$$

Probability

- 3. Let 0 < P(A) < 1, $0 < P(B) < 1 & P(A \cup B) = P(A) + P(B) P(A)$. P(B), then:
 - (A) P(B/A) = P(B) P(A)

- (B) $P(A^c \cup B^c) = P(A^c) + P(B^c)$
- (C) $P((A \cup B)^c) = P(A^c)$. $P(B^c)$
- (D) P(A/B) = P(A)
- **4.** A box contains 11 tickets numbered from 1 to 11. Two tickets are drawn similtaneously at random.
 - Let E₁ denotes the event that the sum of the numbers on the tickets drawn is even
 - and E_2 denotes the event that the sum of the numbers on the tickets drawn is odd

Which of the following hold good?

(A) $P(E_1/E_2) = P(E_2/E_1)$

(B) E, and E, are exhaustive

(C) $P(E_2) > P(E_1)$

- (D) E₁ and E₂ are equally likely
- **5.** The probabilities of events, $A \cap B$, A, $B \& A \cup B$ are respectively in A.P. with second term equal to the common difference. Therefore A & B are :
 - (A) mutually exclusive
 - (B) independent
 - (C) such that one of them must occur
 - (D) such that one is twice as likely as the other
- A bag contains four tickets marked with numbers 112, 121, 211, 222. One ticket is drawn at random from the bag. Let $E_i(i = 1, 2, 3)$ denote the event that ith digit on the ticket is 2. Then
 - (A) E₁ and E₂ are independent
- (B) E₂ and E₃ are independent
- (C) E₃ and E₁ are independent
- (D) E_1 , E_2 , E_3 are independent
- 7. In an experimental performance of a single throw of a pair of unbiased normal dice, three events E₁, E₂ & E₃ are defined as follows:
 - E₁: getting a prime numbered face on each dice
 - E₂: getting the same number on each dice
 - E₃: getting a sum total of dots on two dice equal to 8. Then:
 - (A) the events E₁, E₂ & E₃ are mutually exclusive
 - (B) the events E₁, E₂ & E₃ are not pairwise mutually exclusive
 - (C) the events E₁, E₂ are independent
 - (D) $P(E_2 \mid E_1) = 2/9$.
- 8. The probability that a bulb produced by a factory will fuse after an year of use is 0.1. Then the probability that out of 4 such bulbs
 - (A) None of then bulb will fuse after an year of use is $\frac{9^4}{10^4}$
 - (B) More then three bulbs will fuse after an year of use is $\frac{1}{10^4}$
 - (C) Not more then three bulbs will fuse after an year of use is $\frac{9999}{10000}$
 - (D) All the bulbs will fuse after an year of use is $\frac{1}{10^4}$
- 9. If 4 whole numbers taken at random are multiplied together
 - (A) Probability that the last digit in the product is 1, 3, 7 or 9 is $\frac{16}{625}$
 - (B) Probability that the last digit in the product is '5' is $\frac{369}{10^4}$
 - (C) Probability that the last digit in the product is 0 is $\frac{3727}{10^4}$
 - (D) Probability that the last digit in the product is 0 is $\frac{2357}{10^4}$

18.🔈

10.	The probabil	ity that 4th p	power of a positive	integer en	ds in the digit i	λ is P(λ))		
	(A) P(6) = $\frac{4}{10}$	<u>1</u> 0	(B) $P(1) = \frac{4}{10}$	(C)	$P(5) = \frac{1}{10}$	(D) $P(0) = \frac{1}{1}$	<u>1</u> 0	
11.8	Mean and variance of a Binomial variate of 10 trials of the experiment are in the ratio of 3:2. (A) The most probable number of happening of variable is 3 (B) Sum of the mean and variance is 10								
	(C) Probabili	ty of getting	g exactly 5 succes	s is $\frac{8064}{3^{10}}$					
			number of happen	•	ble is 5				
12.	& III. The pro	babilities ovely. If the p	ests I, II & III. The soft the student pass probability that the	ing in the te student is s (B)	ests I, II & III a	re p, q & 1/2, then 1/2	x :		or tests I
13.	A student has to match three historical events i.e. Dandi March, Quit India Movement and Maha Gandhi's assasination with the years 1948, 1930 and 1942 and each event happens in different ye. The student has no knowledge of the correct answers and decides to match the events and ye randomly. Let E_i : $(0 \le i \le 3)$ denote the event that the student gets exactly i correct answer, then (A) $P(E_o) + P(E_3) = P(E_1)$ (B) $P(E_o) \cdot P(E_1) = P(E_3)$ (C) $P(E_o \cap E_1) = P(E_2)$ (D) $P(E_o) + P(E_1) + P(E_3) = 1$						nt years. id years		
14.	For any two events A & B defined on a sample space, (A) $P(A/B) \ge \frac{P(A) + P(B) - 1}{P(B)}$, $P(B) \ne 0$ is always true								
	(B) P $\left(A\cup\bar{E}\right)$	\bar{B}) = $P(A)$ -	P (A ∩ B)						
	. , .	, ,	°). P (B°), if A & B a °). P (B°), if A & B a	•	dent				
15.			tossed n times P(X = 6) are in AF (B) 10		alue of n can	be	of times D) 14	head oc	curs. If
16.	A random va	ıriable x tak	es values 0, 1, 2,	3,, with	probability pro	oportion	al to (x + 1)	$\left(\frac{1}{5}\right)^{x}$, the	en
			(B) $P(x \le 1) = \frac{112}{125}$						
17.3			g 'n' elements. If t aving same numb			are pick	ed at rando	om. The	
	(A) $\frac{^{2n}C_n}{2^{2n}}$		(B) $\frac{1}{{}^{2n}C_{cn}}$	(C)	$\frac{1.3.5(2n-}{2^n.n!}$	(1)	D) $\frac{3^n}{4^n}$		

A square matrix of order 3×3 is formed using the elements of the set $\{-2016, 0, 2016\}$

(A) Probability of getting a matrix which is symmetric $\frac{1}{3^3}$ is

(B) Probability of getting a matrix which is skew symmetric $\frac{1}{3^6}$ is

(C) Probability of getting a matrix which has maximum trace is $\frac{1}{3^3}$

(D) Probability of getting a matrix which has minimum trace is $\frac{1}{3^3}$

PART - IV : COMPREHENSION

Comprehension # 1

If sample space contains infinite number of points then with the help of geometry that is length, area, volume many problems of probibility can be solved

For example : A point is selected randomely inside the circle then the probability that it is nearer to centre then its circumeference

Probability =
$$\frac{\text{Favourable}}{\text{Total Area}} = \frac{\frac{\pi r^2}{4}}{\pi r^2} = \frac{1}{4}$$



1. A sphere is circumscribed over a cube. Find the probability that a point lies inside the sphere, lies outside the cube.

(A)
$$1 - \frac{2}{\pi\sqrt{3}}$$

(B)
$$1 - \frac{1}{\pi\sqrt{3}}$$

(C)
$$1 - \frac{1}{2\pi\sqrt{3}}$$

(D)
$$1 - \frac{2}{2\pi\sqrt{3}}$$

2. A parallelogram is inscribed inside a circle of radius 10 cm. One side of parallelogram being 12 cms. Then the probability that a point inside the circle also lies inside the parallelogram.

(A)
$$\frac{48}{25\pi}$$

(B)
$$\frac{24}{25\pi}$$

(C)
$$\frac{42}{25\pi}$$

(D)
$$\frac{1}{2}$$

3. The sides of a rectangle are chosen at random, each less than 10 cm, all such lengths being equally likely. The chance that the diagonal of the rectangle is less than 10 cm is

(C)
$$\pi/4$$

Comprehension # 2

A JEE aspirant estimates that he will be successful with an 80 percent chance if he studies 10 hours per day, with a 60 percent chance if he studies 7 hours per day and with a 40 percent chance if he studies 4 hours per day. He further believes that he will study 10 hours, 7 hours and 4 hours per day with probabilities 0.1, 0.2 and 0.7 respectively.

4. The chance he will be successfull is

5. Given that he is successful the chance that he studied for 4 hours, is

(A)
$$\frac{6}{12}$$

(B)
$$\frac{7}{12}$$

(C)
$$\frac{8}{12}$$

(D)
$$\frac{9}{12}$$

6. Given that he does not achieve success, the chance that he studied for 4 hour, is

(A)
$$\frac{18}{26}$$

(B)
$$\frac{19}{26}$$

(C)
$$\frac{20}{26}$$

(D)
$$\frac{21}{26}$$

Comprehension #3

A bag contain 6 Red and 4 White balls. 4 balls are drawn one by one without replacement and were found to be atleast 2 white.

7.b Then the probability that next draw of a ball from this bag will give a white ball.

(A)
$$\frac{34}{115}$$

(B)
$$\frac{19}{115}$$

(C)
$$\frac{90}{115}$$

(D)
$$\frac{24}{115}$$

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- 8. If the next draw of a ball from this bag will give a white ball then the probablity that the drawn of four balls initially contain two white and two red balls.
 - (A) $\frac{8}{17}$
- (B) $\frac{15}{17}$
- (C) $\frac{13}{17}$
- (D) $\frac{13}{34}$

Comprehension # 4

Eight digit number can be formed using all the digits 1,1,2,2,3,3,4,5.

- 9. A number is selected at random then the probability such that no two identical digits appear together
 - (A) $\frac{37}{84}$
- (B) $\frac{43}{84}$
- (C) $\frac{17}{84}$
- (D) $\frac{23}{84}$
- **10.** A number is selected at random then the probability that it has exactly two pair of identical digits occurring together
 - (A) $\frac{1}{7}$
- (B) $\frac{2}{9}$
- (C) $\frac{3}{5}$
- (D) $\frac{4}{9}$

Exercise-3

marked questions are recommended for Revision.

PART - I : JEE (ADVANCED) / IIT-JEE PROBLEMS (PREVIOUS YEARS)

* Marked Questions may have more than one correct option.

Comprehension (Q.1 to 3)

A fair die is tossed repeatedly until a six is obtained. Let X denote the number of tosses required.

- 1. The probability that X = 3 equals
 - (A) $\frac{25}{216}$ (E
- (B) $\frac{25}{36}$
- (C) $\frac{5}{36}$
- (D) $\frac{125}{216}$

2. The probability that $X \ge 3$ equals

[IIT-JEE 2009, Paper-1, (4, -1), 80]

- (A) $\frac{125}{216}$
- (B) $\frac{25}{36}$
- (C) $\frac{5}{36}$
- (D) $\frac{25}{216}$
- **3.** The conditional probability that $X \ge 6$ given X > 3 equals

[IIT-JEE 2009, Paper-1, (4, -1), 80]

[IIT-JEE 2009, Paper-1, (4, -1), 80]

- (A) $\frac{125}{216}$
- (B) $\frac{25}{216}$
- (C) $\frac{5}{36}$
- (D) $\frac{25}{36}$
- Let ω be a complex cube root of unity with $\omega \neq 1$. A fair die is thrown three times. If r_1 , r_2 and r_3 are the numbers obtained on the die, then the probability that $\omega^{r_1} + \omega^{r_2} + \omega^{r_3} = 0$ is

[IIT-JEE 2010, Paper-1, (3, -1), 84]

- (A) $\frac{1}{18}$
- (B) $\frac{1}{9}$
- (C) $\frac{2}{9}$
- (D) $\frac{1}{36}$

A signal which can be green or red with probability $\frac{4}{5}$ and $\frac{1}{5}$ respectively, is received by station A and then transmitted to station B. The probability of each station receiving the signal correctly is $\frac{3}{4}$. If the signal received at station B is green, then the probability that the original signal was green is

[IIT-JEE 2010, Paper-2, (5, -2), 79]

- (A) $\frac{3}{5}$
- (B) $\frac{6}{7}$
- (C) $\frac{20}{23}$
- (D) $\frac{9}{20}$

Comprehension (Q.6 & 7)

Let U_1 and U_2 be two urns such that U_1 contains 3 white and 2 red balls, and U_2 contains only 1 white ball. A fair coin is tossed. If head appears then 1 ball is drawn at random from U_1 and put into U_2 . However, if tail appears then 2 balls are drawn at random from U_1 and put into U_2 . Now 1 ball is drawn at random from U_2 .

[IIT-JEE 2011, Paper-1, (3, -1), 80]

- 6. The probability of the drawn ball from U₂ being white is
 - (A) $\frac{13}{30}$
- (B) $\frac{23}{30}$
- (C) $\frac{19}{30}$
- (D) $\frac{11}{30}$
- 7. Given that the drawn ball from U₂ is white, the probability that head appeared on the coin is
 - (A) $\frac{17}{23}$
- (B) $\frac{11}{23}$
- (C) $\frac{15}{23}$
- (D) $\frac{12}{23}$
- 8.* Let E and F be two independent events. The probability that exactly one of them occurs is $\frac{11}{25}$ and the probability of none of them occurring is $\frac{2}{25}$. If P(T) denotes the probability of occurrence of the event T, then [IIT-JEE 2011, Paper-2, (4, 0), 80]
 - (A) $P(E) = \frac{4}{5}$, $P(F) = \frac{3}{5}$

(B) $P(E) = \frac{1}{5}$, $P(F) = \frac{2}{5}$

(C) $P(E) = \frac{2}{5}$, $P(F) = \frac{1}{5}$

- (D) P(E) = $\frac{3}{5}$, P(F) = $\frac{4}{5}$
- **9*.** A ship is fitted with three engines E_1 , E_2 and E_3 . The engines function independently of each other with respective probabilities $\frac{1}{2}$, $\frac{1}{4}$ and $\frac{1}{4}$. For the ship to be operational at least two of its engines must function. Let X denote the event that the ship is operational and let X_1 , X_2 and X_3 denotes respectively the events that the engines E_1 , E_2 and E_3 are functioning. Which of the following is (are) true?
 - (A) P $[X_1^c | X] = \frac{3}{16}$
 - (B) P[Exactly two engines of the ship are functioning $| X | = \frac{7}{8}$
 - (C) $P[X \mid X_2] = \frac{5}{16}$
 - (D) $P[X \mid X_1] = \frac{7}{16}$

[IIT-JEE 2012, Paper-1, (4, 0), 70]

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(A) $\frac{91}{216}$

following is (are) correct?

(A) $P(X \cup Y) = \frac{2}{3}$

10.3

11*.

	(C) X and Y are not inc	lependent	(D) $P(X^c \cap Y) = \frac{1}{3}$				
12.				obabilities $\frac{1}{2}, \frac{3}{4}, \frac{1}{4}, \frac{1}{8}$. Then the			
	probability that the prot	elem is solved correctly b		ed) 2013, Paper-1, (2, 0)/60]			
	(A) $\frac{235}{256}$	(B) $\frac{21}{256}$	(C) $\frac{3}{256}$	(D) $\frac{253}{256}$			
13.24	β and only E ₃ occurs equations ($\alpha - 2\beta$) p = interval (0, 1).	is γ . Let the probability	p that none of events γ . All the given probabi	E_1 occurs is α ,only E_2 occurs is E_1 , E_2 or E_3 occurs satisfy the lities are assumed to lie in the ed) 2013, Paper-1, $(4, -1)/60$]			
	Probability of	occurrence of E ₃	[OLL (Advance	ca) 2013, 1 apci-1, (4, – 1)/00]			
Compr	ehension (Q.14 & 15)						
	A box B_1 contains 1 white ball, 3 red balls and 2 black balls. Another box B_2 contains 2 white balls, 3 red balls and 4 black balls. A third box B_3 contains 3 white balls, 4 red balls and 5 black balls.						
14.	If 1 ball is drawn from a same colour is		[JEE (Advance	that all 3 drawn balls are of the ed) 2013, Paper-2, (3, -1)/60]			
	(A) $\frac{82}{648}$	(B) $\frac{90}{648}$	(C) $\frac{558}{648}$	(D) $\frac{566}{648}$			
15.		thout replacement) from I, the probability that thes	se 2 balls are drawn from	-			
	116	126		ed) 2013, Paper-2, (3, –1)/60]			
	(A) $\frac{116}{181}$	(B) $\frac{126}{181}$	(C) $\frac{65}{181}$	(D) $\frac{55}{181}$			
16.	is at least one more tha	n the number of girls ahe	ead of her, is [JEE (A	nber of boys ahead of every girl dvanced) 2014, Paper-2, (3, –1)/60]			
	(A) $\frac{1}{2}$	(B) $\frac{1}{3}$	(C) $\frac{2}{3}$	(D) $\frac{3}{4}$			

Four fair dice D_1 , D_2 , D_3 and D_4 each having six faces numbered 1,2,3,4,5 and 6 are rolled

(C) $\frac{125}{216}$

Let X and Y be two events such that $P(X \mid Y) = \frac{1}{2}$, $P(Y \mid X) = \frac{1}{3}$ and $P(X \cap Y) = \frac{1}{6}$. Which of the

(B) X and Y are independent

[IIT-JEE 2012, Paper-2, (3, -1), 66]

[IIT-JEE 2012, Paper-2, (4, 0), 66]

(D) $\frac{127}{216}$

simultaneously. The probability that D_4 shows a number appearing on one of D_1 , D_2 and D_3 is

(B) $\frac{108}{216}$

Comprehension (Q.17 & 18)

[JEE (Advanced) 2014, Paper-2, (3, -1)/60]

Box 1 contains three cards bearing numbers 1, 2, 3; box 2 contains five cards bearing numbers 1, 2, 3, 4, 5; and box 3 contains seven cards bearing numbers 1, 2, 3, 4, 5, 6, 7. A card is drawn from each of the boxes. Let x_i be the number on the card drawn from the i^{th} box, i = 1, 2, 3.

17. The probability that $x_1 + x_2 + x_3$ is odd, is

- (A) $\frac{29}{105}$
- (B) $\frac{53}{105}$
- (C) $\frac{57}{105}$
- (D) $\frac{1}{2}$

18. The probability that x_1 , x_2 , x_3 are in an arithmetic progression, is

- (A) $\frac{9}{105}$
- (B) $\frac{10}{105}$
- $(C)\frac{11}{105}$
- (D) $\frac{7}{105}$

19. The minimum number of times a fair coin needs to be tossed, so that the probability of getting at least two heads is at least 0.96, is [JEE (Advanced) 2015, P-1 (4, 0) /88]

Comprehension (Q.20 & 21)

Let n_1 and n_2 be the number of red and black balls, respectively, in box I. Let n_3 and n_4 be the number of red and black balls, respectively, in box II. [JEE (Advanced) 2015, P-2 (4, -2)/ 80]

20*. One of the two boxes, box I and box II, was selected at random and a ball was drawn randomly out of this box. The ball was found to be red. If the probability that this red ball was drawn from box II is $\frac{1}{3}$, then the correct option(s) with the possible values of n_1 , n_2 , n_3 and n_4 is(are)

- (A) $n_1 = 3$, $n_2 = 3$, $n_3 = 5$, $n_4 = 15$
- (B) $n_1 = 3$, $n_2 = 6$, $n_3 = 10$, $n_4 = 50$
- (C) $n_1 = 8$, $n_2 = 6$, $n_3 = 5$, $n_4 = 20$
- (D) $n_1 = 6$, $n_2 = 12$, $n_3 = 5$, $n_4 = 20$

21*. A ball is drawn at random from box I and transferred to box II. If the probability of drawing a red ball from box I, after this transfer, is $\frac{1}{3}$, then the correct option(s) with the possible values of n_1 and n_2 is(are)

(A) $n_1 = 4$ and $n_2 = 6$

(B) $n_1 = 2$ and $n_2 = 3$

(C) $n_1 = 10$ and $n_2 = 20$

(D) $n_1 = 3$ and $n_2 = 6$

22. A computer producing factory has only two plants T₁ and T₂. Plant T₁ produces 20% and plant T₂ produces 80% of the total computers produced. 7% of computers produced in the factory turn out to be defective. It is known that

P(computer turns out to be defective given that it is produced in plant T₄)

= 10 P(computer turns out to be defective given that it is produced in Plant T₂),

where P(E) denotes the probability of an event E. A computer produced in the factory is randomly selected and it does not turn out to be defective. Then the probability that it is produced in plant T_2 is

[JEE (Advanced) 2016, Paper-1, (3, -1)/62]

- (A) $\frac{36}{73}$
- (B) $\frac{47}{79}$
- (C) $\frac{78}{93}$
- (D) $\frac{75}{83}$

Comprehension (Q.23 & 24)

Football teams T_1 and T_2 have to play two games against each other. It is assumed that the outcomes of the two games are independent. The probabilities of T_1 winning, drawing and losing a game against

 T_2 are $\frac{1}{2}$, $\frac{1}{6}$ and $\frac{1}{3}$, respectively. Each team gets 3 points for a win, 1 point for a draw and 0 point for a

loss in a game. Let X and Y denote the total points scored by teams T_1 and T_2 , respectively, after two games. [JEE (Advanced) 2016, Paper-2, (3, -1)/62]

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P(X > Y) is 23.

(A)
$$\frac{1}{4}$$

(B)
$$\frac{5}{12}$$

(C)
$$\frac{1}{2}$$

(D)
$$\frac{7}{12}$$

24. P(X = Y) is

(A)
$$\frac{11}{36}$$

(B)
$$\frac{1}{3}$$

(C)
$$\frac{13}{36}$$

(D)
$$\frac{1}{2}$$

Let X and Y be two events such that $P(X) = \frac{1}{3}$, $P(X|Y) = \frac{1}{2}$ and $P(Y|X) = \frac{2}{5}$. Then 25*.

[JEE(Advanced) 2017, Paper-1,(4, -2)/61]

(A)
$$P(Y) = \frac{4}{15}$$

(B)
$$P(X'|Y) = \frac{1}{2}$$

(B)
$$P(X'|Y) = \frac{1}{2}$$
 (C) $P(X \cup Y) = \frac{2}{5}$ (D) $P(X \cap Y) = \frac{1}{5}$

(D)
$$P(X \cap Y) = \frac{1}{5}$$

26. Three randomly chosen nonnegative integers x, y and z are found to satisfy the equation x + y + z = 10. Then the probability that z is even, is [JEE(Advanced) 2017, Paper-2,(3, -1)/61]

(A)
$$\frac{1}{2}$$

(B)
$$\frac{36}{55}$$

(C)
$$\frac{6}{11}$$

(D)
$$\frac{5}{11}$$

Comprehension (Q.27 & 28)

There are five students S₁, S₂, S₃, S₄ and S₅ in a music class and for them there are five seats R₁, R₂, R_3 , R_4 and R_5 arranged in a row, where initially the seat R_i is allotted to the student S_i , i = 1, 2, 3, 4, 5. But, on the examination day, the five students are randomly allotted the five seats.

(There are two questions based on PARAGRAPH "A", the question given below is one of them) [JEE(Advanced) 2018, Paper-1,(3, -1)/60]

The probability that, on the examination day, the student S₁ gets the previously allotted seat R₁, and 27. NONE of the remaining students gets the seat previously allotted to him/her, is

(A)
$$\frac{3}{40}$$

(B)
$$\frac{1}{8}$$

(C)
$$\frac{7}{40}$$

(D)
$$\frac{1}{5}$$

28. For i = 1, 2, 3, 4, let T_i denote the event that the students S_i and S_{i+1} do **NOT** sit adjacent to each other on the day of the examination. Then, the probability of the event $T_1 \cap T_2 \cap T_3 \cap T_4$ is

(A)
$$\frac{1}{15}$$

(B)
$$\frac{1}{10}$$

(C)
$$\frac{7}{60}$$

(D)
$$\frac{1}{5}$$

PART - II: JEE (MAIN) / AIEEE PROBLEMS (PREVIOUS YEARS)

In a binomial distribution B $\left(n, p = \frac{1}{4}\right)$, if the probability of at least one success is greater than or equal 1.

to $\frac{9}{10}$, then n is greater than :

[AIEEE 2009 (4, -1), 144]

$$(1) \ \frac{1}{\log_{10} 4 + \log_{10} 3}$$

$$(2) \frac{9}{\log_{10} 4 - \log_{10} 3}$$

(1)
$$\frac{1}{\log_{10} 4 + \log_{10} 3}$$
 (2) $\frac{9}{\log_{10} 4 - \log_{10} 3}$ (3) $\frac{4}{\log_{10} 4 - \log_{10} 3}$ (4) $\frac{1}{\log_{10} 4 - \log_{10} 3}$

$$(4) \ \frac{1}{\log_{10} 4 - \log_{10} 3}$$

2. One ticket is selected at random from 50 tickets numbered 00, 01, 02,, 49. Then the probability that the sum of the digits on the selected ticket is 8, given that the product of these digits is zero, equal:

[AIEEE 2009 (4, -1), 144]

$$(1) \frac{1}{7}$$

(2)
$$\frac{5}{14}$$

(3)
$$\frac{1}{50}$$

$$(4)\frac{1}{14}$$



3.

	difference is {±1, ±2, ±3 (1) Statement- is true, (2) Statement-1 is true (3) Statement -1 is fals	s, ±4, ±5} Statement-2 is true ; Stat , Statement-2 is false. e, Statement -2 is true.	tement -2 is not a correc	all possible values of common texplanation for Statement -1.
4.	drawn at random without colours is			two are green. Three balls are at the three balls have different [AIEEE 2010 (4, -1), 144]
	$(1) \frac{2}{7}$	(2) $\frac{1}{21}$	(3) $\frac{2}{23}$	$(4) \frac{1}{3}$
5.	Consider 5 independen	t Bernoulli's trials each v	with probability of succes	s p. If the probability of at least
	one failure is greater the	an or equal to $\frac{31}{32}$, then	p lies in the interval :	[AIEEE 2011, I, (4, -1), 120]
	$(1)\left(\frac{1}{2}, \frac{3}{4}\right]$	$(2) \left(\frac{3}{4}, \frac{11}{12}\right]$	$(3) \left[0, \frac{1}{2}\right]$	$(4)\left(\frac{11}{12}, 1\right]$
6.	is:			statement among the following [AIEEE 2011, I, (4, -1), 120]
	(1) P(C D) = P(C)	(2) $P(C D) \ge P(C)$	(3) $P(C D) < P(C)$	$(4) P(C D) = \frac{P(D)}{P(C)}$
7.	Let A, B, C be pairwise	independent events with	$P(C) > 0$ and $P(A \cap B \cap B)$	$A(C) = 0$. Then $P(A^c \cap B^c / C)$. [AIEEE 2011, II, (4, -1), 120]
	(1) 1 – P(B ^c)	(2) $P(A^c) + P(B^c)$	(3) $P(A^c) - P(B^c)$	(4) $P(A^c) - P(B)$
8.	minimum is 3, given tha	at their maximum is 6, is		, 8}. The probability that their [AIEEE-2012, (4, -1)/120]
	(1) $\frac{3}{8}$	(2) $\frac{1}{5}$	(3) $\frac{1}{4}$	(4) $\frac{2}{5}$
9.				ee alternative answers of which prrect answers just by guessing
		12	11	[AIEEE - 2013, (4, – 1) 120]
	(1) $\frac{17}{3^5}$	(2) $\frac{13}{3^5}$	$(3)\frac{11}{3^5}$	(4) $\frac{10}{3^5}$
10.	Let A and B be two even	ent such that $P(\overline{A \cup B}) =$	$\frac{1}{6}$, P(A \cap B) = $\frac{1}{4}$ and B	$P(\overline{A}) = \frac{1}{4}$, where \overline{A} stands for
	the complement of the (1) independent but not (3) mutually exclusive a		s A and B are : (2) independent and eq (4) equally likely but no	
11.	If 12 identical balls are contains exactly 3 balls	-	tical boxes, then the pr	obability that one of the boxes [JEE(Main)2015, (4, - 1), 20]
	$(1) \ \frac{55}{3} \left(\frac{2}{3}\right)^{11}$	(2) $55\left(\frac{2}{3}\right)^{10}$	(3) $220\left(\frac{1}{3}\right)^{12}$	(4) $22\left(\frac{1}{3}\right)^{11}$

Four numbers are chosen at random (without replacement) from the set {1,2,3,....,20}. **Statement -1:** The probability that the chosen numbers when arranged in some order will form an AP

[AIEEE 2010 (8, -2), 144]

١

12.

13.

	= P(Exactly one of C o	$r A occurs) = \frac{1}{4} and P$	(All the three events occ	cur simultaneously) = $\frac{1}{16}$. Then
		ast one of the events oc		[JEE(Main)2017,(4, -1), 120]
	(1) $\frac{7}{32}$	(2) $\frac{7}{16}$	(3) $\frac{7}{64}$	(4) $\frac{3}{16}$
14.	well as absolute differen	nce are both multiple of	4, is	he probability that their sum as [JEE(Main)2017,(4, -1), 120]
	(1) $\frac{6}{55}$	(2) $\frac{12}{55}$	(3) $\frac{14}{45}$	(4) $\frac{7}{55}$
15.	replacement, then the v			domly drawn, one-by-one, with IEE(Main) 2017, (4, – 1), 120]
	(1) $\frac{12}{5}$	(2) 6	(3) 4	(4) $\frac{6}{25}$
16.	and this ball along with	two additional balls of t		the bag, its colour is observed rned to the bag. If now a ball is red, is [JEE(Main)2018,(4, -1), 120]
	$(1) \frac{1}{5}$	(2) $\frac{3}{4}$	(3) $\frac{3}{10}$	(4) $\frac{2}{5}$
17.			obtained in the two draw	uffled deck of 52 cards. Let X r cards. Then $P(X = 1) + P(X = 1)$ ne (09-01-19),P-1 (4, -1), 120] (4) 25/169
18.		subset B of S is said to be ndomly chosen subset o	f S is " nice" is :	e elements of B is 203. Then ne (11-01-19),P-2 (4, -1), 120]
	(1) $\frac{4}{2^{20}}$	(2) $\frac{5}{2^{20}}$	(3) $\frac{7}{2^{20}}$	(4) $\frac{6}{2^{20}}$
19.		t a fair die is rolled until in the fifth throw of the c	lie is equal	n succession the probability that
	(1) $\frac{200}{6^5}$	(2) $\frac{175}{6^5}$	[JEE(Main) 2019, Onli (3) $\frac{150}{6^5}$	ne (12-01-19),P-1 (4, -1), 120] (4) $\frac{225}{6^5}$
20.	In a game, a man wins other number on the di	Rs. 100 if he gets 5 or 6	on a throw of a fair die to the die either till he gets	and loses Rs. 50 for getting any s a five or a six or to a maximum
		400	- '	ne (12-01-19),P-2 (4, – 1), 120]
	(1) 0	(2) $\frac{400}{9}$ loss	(3) $\frac{400}{3}$ gain	(4) $\frac{400}{3}$ loss

Let two fair six-faced dice A and B be thrown simultaneously. If E_1 is the event that die A shows up four, E_2 is the event that die B shows up two and E_3 is the event that the sum of numbers on both dice is odd,

For three events A, B and C, P(Exactly one of A or B occurs) = P(Exactly one of B or C occurs)

(2) E_1 and E_3 are independent

(4) E₁ and E₂ are independent

[JEE(Main)2016,(4, -1), 120]

then which of the following statements is NOT True?

(1) E_2 and E_3 are independent

(3) E_1 , E_2 and E_3 are independent

Answers

EXERCISE - 1

PART - I

Section (A):

- **A-1.** (i) {HHH, HHT, HTH, THH, HTT, THT, TTH, TTT}
 - (ii) $\{B_1 B_2, B_1 B_3, B_1 G_1, B_1 G_2, B_2 B_3, B_2 G_1, B_2 G_2, B_3 G_1, B_3 G_2, G_1 G_2\}$
- **A-2.** 43 to 34 **A-3.** $\frac{4}{5}$ **A-4.** $\frac{5}{9}$ **A-5.** $\frac{1}{6}$ **A-6.** (i) $\frac{4}{15}$ (ii) 10
- **A-7.** (i) No (ii) No **A-8.** $\frac{29}{36}$ **A-9.** $B = \frac{2}{5}$, $C = \frac{4}{15}$ **A-10.** $\frac{3}{10}$
- **A-11.** (i) $\frac{22}{425}$ (ii) $\frac{16}{5525}$ **A-12.** $\frac{5}{36}$ **A-13.** $\frac{1}{462}$ **A-14.** (i) $\frac{2197}{20825}$ (ii) $\frac{{}^{13}C_4 \times 4^4}{{}^{52}C_4}$

Section (B):

B-2 (i) 0.5 (ii) 0.8 **B-3**. (i) 0.72 (ii) 0.32 (iii) 0.28 (iv) 0.56 **B-4**. 5/21

Section (C):

- **C-1.** (i) $\frac{2}{3}$ (ii) $\frac{1}{2}$ **C-2.** $\frac{3}{4}$ **C-3.** (i) $\frac{2}{13}$ (ii) $\frac{4}{13}$ **C-4.** $\frac{52}{77}$
- **C-5.** $\frac{16}{37}$, $\frac{12}{37}$, $\frac{9}{37}$ **C-6.** 3/5 **C-7.** $\frac{17}{125}$ **C-8.** (i) $\frac{27}{56}$ (ii) $\frac{8}{29}$ **C-9.** $\frac{1}{17}$
- **C-10.** $\frac{5}{9}$ **C-11.** $\frac{1}{4}$

Section (D):

- **D-1.** $\frac{7}{2^{13}}$ **D-2.** ${}^{10}\text{C}_2 \cdot \frac{(14)^8}{15^{10}}$ **D-3.** $\frac{X}{P(X)} = \frac{27}{64} = \frac{3}{64} = \frac{3}{64}$ **D-4.** 28 rupees
- **D-6.** mean = 2.5, variance = 1.25

Prob	ability												
Sect	ion (A)	:											
A-1.	(D)	A-2.	(C)	A-3.	(C)	A-4.	(D)	A-5.	(A)	A-6.	(D)		
A-7.	(A)	A-8.	(B)	A-9.	(C)								
Sect	ion (B)	:											
B-1.	(B)	B-2.	(i) (D)	(ii) (B)	(iii) (C)		B-3	(B)	B-4	(D)			
Sect	ion (C)	:											
C-1.	(B)	C-2.	(C)	C-3.	(B)	C-4.	(B)	C-5.	(A)	C-6.	(A)		
C-7.	(D)												
Sect	ion (D)	:											
D-1.	(C)	D-2.	(A)	D-3.	(A)	D-4.	(D)	D-5.	(B)	D-6.	(B)		
						PAF	RT - III						
1. 2.	$\begin{array}{c} (A) \to \\ (A) \to \end{array}$		$(B) \rightarrow (B) \rightarrow (B)$		$(C) \rightarrow (C)$		$\begin{array}{c} (D) \to \\ (D) \to \end{array}$						
					i	EXER	CISE - 2	2					
						PA	RT - I						
1.	(A)	2.	(A)	3.	(C)	4.	(A)	5.	(B)	6.	(B)	7.	(A)
8.	(A)	9.	(A)	10.	(D)	11.	(A)	12.	(B)	13.	(A)	14.	(B)
15.	(B)												
_		_		_			RT - II	_		_			
1.	10	2.	18	3.	1	4.	3	5.	11	6.	59	7.	6
8. 15.	20 19	9. 16.	6 7	10. 17.	1 5	11. 18.	27 5	12. 19.	1 36	13. 20.	1 11	14.	32
13.	19	10.	,	17.	5		RT - III	13.	30	20.	11		
1.	(AC)	2.	(ACD)	3.	(CD)	4.	(ABC)	5.	(AD)	6.	(ABC)	7.	(BD)
8.	(ABCI		(AB)	10.	(ABCD		(AC)	12.	(ABCE		13.	(ABCI	
14.	(AC)	15.	(AD)	16.	(ABC)	17.	(AC)	18.	(ABC	D)			
						PAF	RT - IV						
1.	(A)	2.	(A)	3.	(C)	4.	(C)	5.	(B)	6.	(D)	7.	(A)
8.	(B)	9.	(A)	10.	(A)								

D.	1 1		
Pro	nar) I I	tv
110	$\sigma u \sigma$	••••	ιy

EXERCISE - 3

PART - I

1. (A) 2. (B) 3. (D) 4. (C) 5. (C) 6.

PART - II

Advance Level Problems (ALP)

- 1. Urn A contains 6 red & 4 black balls and urn B contains 4 red & 6 black balls. One ball is drawn at random from urn A & placed in urn B. Then one ball is drawn at random from urn B & placed in urn A. If one ball is now drawn at random from urn A, then find the probability that it is red.
- 2. Let p be the probability that a man aged x years will die in a year time. Then find the probability that out of 'n' men A₁, A₂, A₃,....., A_n each aged 'x' years. A₁ will die & will be the first to die.
- 3. A Sudoku matrix is defined as a 9 x 9 arrary with entries from {1, 2, 3 9} and with the constraint that each row, each column and each of the nine 3 x 3 boxes that tile the array contains each digit from 1 to 9 exactly once. A Sudoku matrix is chosen at random (so that every Sudoku matrix has equal probability of being chosen). We know two of square in this matrix as shown. Then find the probability that the square marked by ? contains the digit 3.
- 4. 5 girls and 10 boys sit at random in a row having 15 chairs numbered as 1 to 15, then find the probability that end seats are occupied by the girls and between any two girls an odd number of boys sit.
- **5.** Team A plays with 5 other teams exactly once. Assuming that for each match the probabilities of a win, draw and loss are equal then find the probability that A wins and losses equal no. of matches.
- Suppose that S be the set of all the ordered 4-tuples (x, y, z, w) of the +ve integers, which are the solutions of x + y + z + w = 21. One such ordered tuple of solution is selected at random from S. Then find the probability that x > y.
- 7. In a betting game in an exhibition two dice P and Q are being used. Dice P has four red faces and two white faces where as dice Q has two red and four white faces. A fair coin is tossed once. If it shows head the game continues by throwing dice P. If it falls tail dice Q is thrown. If first n throws of the die all turns up red then find the probability that P is being used.
- 8. On a particular day, six persons pick six different books, one each from different counters at a public library. At the closing time, they arbitrarily put their books to the vacant counters. Then find the probability that exactly two books are at their previous places.
- **9.** A dice has one 1, two 2's and three 3's on its faces. A player throws it till he gets three consecutive 1's. If p_n is the probability that no 3 consecutive 1's appear in n throws, then prove that

(i)
$$p_1 = p_2 = 1$$
 and $p_3 = \frac{215}{216}$

(ii)
$$p_n = \frac{5}{216} [p_{n-3} + 6p_{n-2} + 36p_{n-1}], \ n > 3$$

10. In students filled their forms for a competitive exam. Probability that exactly r students will not appear in the exam is proportional to r. If probability that out of remaining n-r students exactly i students are selected is proportional to i. Prove that the probability of exactly two students finally getting selected is

$$\frac{8}{n(n+1)}\Bigg[n\bigg(\frac{1}{2}-\frac{1}{n}\bigg)-\bigg(\frac{1}{3}+\frac{1}{4}+\ldots\ldots+\frac{1}{n}\bigg)\Bigg]$$

In an organization number of women are μ times that of men. If n things are to be distributed among them then the probability that the number of things received by men are odd is $\left(\frac{1}{2} - \left(\frac{1}{2}\right)^{n+1}\right)$ Evaluate

- 12. The color of a person's eyes is determined by a single pair of genes. If they are both blue eyed genes, then the person will have blue eyes; if they are both brown -eyed genes, then the person will have brown eyes; and if one of them is a blue-eyed gene and the other a brown-eyed gene, then the person will have brown eyes. (Because of the latter fact we say that the brown-eyed gene is dominant over the blue-eyed one.) A newborn child independently receives one eye gene from each of its parents and the gene it receives from a parent is equally likely to be either of the two eye genes of that parent. Suppose that Smith and both of his parents have brown eyes, but Smith's sister has blue eyes. Suppose that Smith's wife has blue eyes. Find
 - (i) What is the probability that both of Smith's parents has one blue-eyed gene and one brown eyed gene?
 - (ii) What is the probability that Smith's possesses a blue-eyed gene?
 - (iii) What is the probability that Smith's first child will have blue eyes?
 - (iv) If Smith's first child has brown eyes, what is the probability that both Smith's genes are browneyed genes?
 - (v) If Smith's first child has brown-eyes, what is the probability that Smith's next child will also have brown eyes?
- 13. Each square of a 3×3 board is coloured either red or blue at random (each having probability 1/2). Then find the probability that there is no 2×2 red square.
- **14.** A fair coin is tossed (2m + 1) times, then find the probability of getting at least m consecutive heads.
- **15.** In a single throw of three dice find the probability of the event 'a total of 8.
- Suppose A & B shoot independently until each hits his target. They have probabilities $\frac{3}{5}$, $\frac{5}{7}$ of hitting the target at each shoot. Find the probability that B will require more shots than A.
- 17. A quadratic equation is chosen by selecting two real numbers as its roots such that the quadratic equation doesn't change by squaring the numbers. Now find probability that both roots are equal.
- **18.** Five team of equal strength play against each other in a tournament and each match either ends in a win or loss for a team. Find the probability that no team win all its games or loss all its game.
- **19.** If A and B has (n + 1) and n fair coins respectively. Then find the probability that A gets more heads then B.
- 20. Let the probability p_n that a family has exactly n children be αp^n , where $n \ge 1$ and $p_0 = 1 \alpha p(1 + p + p^2 +)$ (0 < α , p < 1). Giving birth to a boy and girl is equally likely. If $k \ge 1$, then find the probability that the family has exactly k boys.
- 21. A bear hides itself either behind bush A with probability $\frac{9}{25}$ or behind bush B with probability $\frac{16}{25}$. A hunter have 5 bullets each of which can be fired either at bush A or B. Hunter hits each target independtly with an accuracy of 1/4. How many bullets can be fired at bush A to hit the bear with max. probability.
- Set A: {randomly choosen 100 years in which 76 are simple and 24 are leap years}
 Set B: {randomly choosen 100 years in which 75 are simple and 25 are leap years}
 An year is chosen from either set A or set B and is found to have 53 sundays. Probability that the chosen year was a leap year.
- 23. In ten trials of an experiment, if the probability of getting '4 successes' is maximum, then find the range of probability of success in each trial.
- 24. There are two lots of identical articles with different amounts of standard & defective articles. There are N articles in the first lot, n of which are defective & M articles in the second lot, m of which are defective. K articles are selected from the first lot & L articles from the second & a new lot results. Find the probability that an article selected at random from the new lot is defective.
- **25.** Find the chance of throwing 10 exactly in one throw with 3 dice.

- 26. Two players of equal skill, A and B, are playing a set of games; they leave off playing when A gets 3 points and B gets 2 (in each game winner get one point). If the stake is Rs.1600, what share ought each to take?
- 27. A family has three children. Event 'A' is that family has at most one boy, Event 'B' is that family has at least one boy and one girl, Event 'C' is that the family has at most one girl. Find whether events 'A' and 'B' are independent. Also find whether A, B, C are independent or not.
- 28. A line segment of length a is divided in two parts at random by taking a point on it, find the probability that no part is greater than b, where 2b > a
- 29. Two ants are on the opposite corners of a grid of size 8 x 8 if they move then what is the probability that they will meet after each travelled eight steps (Assuming that they do not move in backward direction)
- **33. Match**: A box contains n coins. Let $P(E_i)$ be the probability that exactly i out of n coins are biased. If $P(E_i)$ is directly proportional to i(i + 1); $1 \le i \le n$.
 - (A) Proportionality constant k is equal to

- (p) $\frac{(3n+1)^2}{4n}$
- (B) If P be the probability that a coin selected at
- (q) $\frac{3}{n(n+1)(n+2)}$

- random is biased then P is
- (C) If a coin selected at random is found to be $(r) \qquad \frac{3}{n+2}$
- biased then the probability that it is the only biased coin in the box is
- (D) $P(E_n)$ is equal to

(s) $\frac{24}{n(n+1)(n+2)(3n+1)}$

Answers

- 1. $\frac{32}{55}$ 2. $\frac{1-(1-p)^n}{n}$ 3. $\frac{2}{21}$ 4. $\frac{20\times10!\times5!}{15!}$ 5. $\frac{17}{81}$ 6. $\frac{35}{76}$
- 7. $\frac{2^n}{2^n+1}$ 8. 3/16 11. 3 12. (i) 1 (ii) 2/3 (iii) 1/3 (iv) 1/2 (v) 2/3
- **13.** $\frac{417}{512}$ **14.** $\frac{(m+3)2^m-1}{2^{2m+1}}$ **15.** $\frac{7}{72}$ **16.** $\frac{6}{31}$ **17.** $\frac{1}{2}$ **18.** $\frac{17}{32}$
- **19.** $\frac{2\alpha p^k}{(2-p)^{k+1}}$ **21.** 1, 2 **22.** $\frac{98}{249}$ **23.** $p \in \left[\frac{4}{11}, \frac{5}{11}\right]$
- **24.** $\frac{\text{KnM} + \text{LmN}}{\text{MN} (\text{K} + \text{L})}$ **25.** 1/8 **26.** 500 Rs. & 1100 Rs.
- 27. A and B are independent but A,B,C are not independent 28. $\frac{2b-a}{a}$ 29. $\frac{^{16}C_8}{2^{16}}$
- **30.** $\frac{1}{256}$ **31.** $\frac{1}{256}$ **32.** $\frac{9}{64}$ **33.** A-q; B-p, C-s, d-r