Exercise-1

> Marked questions are recommended for Revision.

PART - I : SUBJECTIVE QUESTIONS

Section (A) : Equation of circle, parametric equation, position of a point

- **A-1.** Find the equation of the circle that passes through the points (1, 0), (-1, 0) and (0, 1).
- A-2. ABCD is a square in first quadrant whose side is a, taking AB and AD as axes, prove that the equation to the circle circumscribing the square is $x^2 + y^2 = a(x + y)$.
- **A-3.** Find the equation to the circle which passes through the origin and cuts off intercepts equal to 3 and 4 from the positive axes.
- A-4. Find equation of circle which touches x & y axis & perpendicular distance of centre of circle from 3x + 4y + 11 = 0 is 5. Given that circle lies in Ist quadrant.
- A-5. Find the equation to the circle which touches the axis of x at a distance 3 from the origin and intercepts a distance 6 on the axis of y.
- **A-6.** Find equation of circle whose cartesian equation are $x = -3 + 2 \sin \theta$, $y = 4 + 2 \cos \theta$
- **A-7.** Find the values of p for which the power of a point (2, 5) is negative with respect to a circle $x^2 + y^2 8x 12y + p = 0$ which neither touches the axes nor cuts them.

Section (B) : Line and circle, tangent, pair of tangent

- **B-1.** If radii of the largest and smallest circle passing through the point (1, -1) and touching the circle $x^2 + y^2 + 2\sqrt{2}y 2 = 0$ are r_1 and r_2 respectively, then find the sum of r_1 and r_2 .
- **B-2.** Find the points of intersection of the line x y + 2 = 0 and the circle $3x^2 + 3y^2 29x 19y + 56 = 0$. Also determine the length of the chord intercepted.
- **B-3.** Show that the line 7y x = 5 touches the circle $x^2 + y^2 5x + 5y = 0$ and find the equation of the other parallel tangent.
- **B-4.** Find the equation of the tangents to the circle $x^2 + y^2 = 4$ which make an angle of 60° with the positive x-axis in anticlockwise direction.
- **B-5.** Show that two tangents can be drawn from the point (9, 0) to the circle $x^2 + y^2 = 16$; also find the equation of the pair of tangents and the angle between them.
- **B-6.** If the length of the tangent from (f, g) to the circle $x^2 + y^2 = 6$ be twice the length of the tangent from (f, g) to the circle $x^2 + y^2 + 3x + 3y = 0$, then will $f^2 + g^2 + 4f + 4g + 2 = 0$?

Section (C) : Normal, Director circle, chord of contact, chord with mid point

- **C-1.** Find the equation of the normal to the circle $x^2 + y^2 = 5$ at the point (1, 2)
- **C-2.** Find the equation of the normal to the circle $x^2 + y^2 = 2x$, which is parallel to the line x + 2y = 3.
- **C-3.** Find the equation of director circle of the circle $(x + 4)^2 + y^2 = 8$
- **C-4.** Tangents are drawn from the point (h, k) to the circle $x^2 + y^2 = a^2$; prove that the area of the triangle $a(h^2 + k^2 a^2)^{3/2}$

formed by them and the straight line joining their points of contact is $\frac{a(h^2 + k^2 - a^2)^{3/2}}{h^2 + k^2}$

C-5. Find the equation of the chord of the circle $x^2 + y^2 + 6x + 8y + 9 = 0$ whose middle point is (-2, -3).

C-6. Tangents are drawn to the circle $x^2 + y^2 = 12$ at the points where it is met by the circle $x^2 + y^2 - 5x + 3y - 2 = 0$; find the point of intersection of these tangents.

Section (D) : Position of two circle, Orthogonality, Radical axis and radical centre

- **D-1.** Find the equations to the common tangents of the circles $x^2 + y^2 2x 6y + 9 = 0$ and $x^2 + y^2 + 6x 2y + 1 = 0$
- **D-2.** Show that the circles $x^2 + y^2 2x 6y 12 = 0$ and $x^2 + y^2 + 6x + 4y 6 = 0$ cut each other orthogonally.
- **D-3.** Find the equation of the circle passing through the origin and cutting the circles $x^2 + y^2 4x + 6y + 10 = 0$ and $x^2 + y^2 + 12y + 6 = 0$ at right angles.
- **D-4.** Given the three circles $x^2 + y^2 16x + 60 = 0$, $3x^2 + 3y^2 36x + 81 = 0$ and $x^2 + y^2 16x 12y + 84 = 0$, find (1) the point from which the tangents to them are equal in length and (2) this length.

Section (E) : Family of circles , Locus, Miscellaneous

E-1. If y = 2x is a chord of the circle $x^2 + y^2 - 10x = 0$, find the equation of a circle with this chord as diameter.

- **E-2.** Find the equation of a circle which touches the line 2x y = 4 at the point (1, -2) and (i) Passes through (3, 4) (ii) Radius = 5
- **E-3.** Show that the equation $x^2 + y^2 2x 2\lambda y 8 = 0$ represents for different values of λ a system of circles passing through two fixed points A and B on the x-axis, and also find the equation of that circle of the system the tangent to which at A and B meet on the line x + 2y + 5 = 0.
- **E-4.** Consider a family of circles passing through two fixed points A (3, 7) and B (6, 5). Show that the chords in which the circles $x^2 + y^2 4x 3 = 0$ cuts the members of the family are concurrent at a point. Also find the co-ordinates of this point.
- **E-5.** Find the equation of the circle circumscribing the triangle formed by the lines x + y = 6, 2x + y = 4 and x + 2y = 5.
- **E-6.** Prove that the circle $x^2 + y^2 + 2ax + c^2 = 0$ and $x^2 + y^2 + 2by + c^2 = 0$ touches each other if $\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{c^2}$

PART - II : ONLY ONE OPTION CORRECT TYPE

Section (A) : Equation of circle, parametric equation, position of a point

A-1. The radius of the circle passing through the points (1, 2), (5, 2) & (5, -2) is:

(A) $5\sqrt{2}$ (B) $2\sqrt{5}$ (C) $3\sqrt{2}$ (D) $2\sqrt{2}$

A-2. The centres of the circles $x^2 + y^2 - 6x - 8y - 7 = 0$ and $x^2 + y^2 - 4x - 10y - 3 = 0$ are the ends of the diameter of the circle (A) $x^2 + y^2 - 5x - 9y + 26 = 0$ (B) $x^2 + y^2 + 5x - 9y + 14 = 0$

= 0

	5	· · ·	,	,
(C) $x^2 + y^2 + 5x - y^2$	y - 14 = 0	(D) x ²	+ y² + 5x	+ y + 14

- A-3. The circle described on the line joining the points (0, 1), (a, b) as diameter cuts the x-axis in points whose abscissa are roots of the equation: (A) $x^2 + ax + b = 0$ (B) $x^2 - ax + b = 0$ (C) $x^2 + ax - b = 0$ (D) $x^2 - ax - b = 0$
- A-4. The intercepts made by the circle $x^2 + y^2 5x 13y 14 = 0$ on the x-axis and y-axis are respectively (A) 9, 13 (B) 5, 13 (C) 9, 15 (D) none

Equation of line passing through mid point of intercepts made by circle $x^2 + y^2 - 4x - 6y = 0$ on A-5. co-ordinate axes is (D) 3x + 2y - 6 = 0

(A) 3x + 2y - 12 = 0(B) 3x + y - 6 = 0(C) 3x + 4y - 12 = 0

A-6. Two thin rods AB & CD of lengths 2a & 2b move along OX & OY respectively, when 'O' is the origin. The equation of the locus of the centre of the circle passing through the extremities of the two rods is: (B) $x^2 - y^2 = a^2 - b^2$ (C) $x^2 + y^2 = a^2 - b^2$ (A) $x^2 + y^2 = a^2 + b^2$ (D) $x^2 - y^2 = a^2 + b^2$

A-7. Let A and B be two fixed points then the locus of a point C which moves so that (tan \angle BAC)

(tan
$$\angle ABC$$
)=1, 0 < $\angle BAC$ < $\frac{\pi}{2}$, 0 < $\angle ABC$ < $\frac{\pi}{2}$ is
(A) Circle (B) pair of straight line (C) A point

(A) Circle

- is

(D) Straight line

A-8. **STATEMENT-1**: The length of intercept made by the circle $x^2 + y^2 - 2x - 2y = 0$ on the x-axis is 2.

STATEMENT-2: $x^2 + y^2 - \alpha x - \beta y = 0$ is a circle which passes through origin with centre $\left(\frac{\alpha}{2}, \frac{\beta}{2}\right)$ and

radius
$$\sqrt{\frac{\alpha^2 + \beta^2}{2}}$$

- (A) STATEMENT-1 is true, STATEMENT-2 is true and STATEMENT-2 is correct explanation for STATEMENT-1
- (B) STATEMENT-1 is true, STATEMENT-2 is true and STATEMENT-2 is not correct explanation for STATEMENT-1
- STATEMENT-1 is true, STATEMENT-2 is false (C)
- STATEMENT-1 is false, STATEMENT-2 is true (D)

Section (B) : Line and circle, tangent, pair of tangent

- Find the co-ordinates of a point p on line x + y = -13, nearest to the circle $x^2 + y^2 + 4x + 6y 5 = 0$ B-1. (D) (-7, -6)(A) (-6, -7)(B) (- 15, 2) (C) (-5, -6)
- The number of tangents that can be drawn from the point (8, 6) to the circle $x^2 + y^2 100 = 0$ is B-2. (A) 0 (B) 1 (C) 2 (D) none
- **B-3.** Two lines through (2, 3) from which the circle $x^2 + y^2 = 25$ intercepts chords of length 8 units have equations

(A) 2x + 3y = 13, x + 5y = 17	(B) y = 3, 12x + 5y = 39
(C) $x = 2$, $9x - 11y = 51$	(D) $y = 0$, $12x + 5y = 39$

B-4. The line 3x + 5y + 9 = 0 w.r.t. the circle $x^2 + y^2 - 4x + 6y + 5 = 0$ is (A) chord dividing circumference in 1 : 3 ratio (B) diameter (C) tangent (D) outside line

(B) $\frac{\pi}{3}$

B-5. If one of the diameters of the circle $x^2 + y^2 - 2x - 6y + 6 = 0$ is a chord to the circle with centre (2, 1), then the radius of the circle is (C) 3/2 (D) 1 (A) 3 (B) 2

The tangent lines to the circle $x^2 + y^2 - 6x + 4y = 12$ which are parallel to the line 4x + 3y + 5 = 0 are B-6. given by:

(A) 4x + 3y - 7 = 0, 4x + 3y + 15 = 0(B) 4x + 3y - 31 = 0, 4x + 3y + 19 = 0(D) 4x + 3y - 31 = 0, 4x + 3y - 19 = 0

(C) $\frac{\pi}{2}$

(D) $\frac{\pi}{6}$

(C) 4x + 3y - 17 = 0, 4x + 3y + 13 = 0The condition so that the line $(x + g) \cos\theta + (y + f) \sin\theta = k$ is a tangent to $x^2 + y^2 + 2gx + 2fy + c = 0$ is B-7. (A) $g^2 + f^2 = c + k^2$ (B) $g^2 + f^2 = c^2 + k$ (C) $g^2 + f^2 = c^2 + k^2$ (D) $g^2 + f^2 = c + k$

B-8. The tangent to the circle $x^2 + y^2 = 5$ at the point (1, -2) also touches the circle $x^2 + y^2 - 8x + 6y + 20 = 0$ at (B) (-3, 0) (A) (-2, 1) (C) (−1, −1) (D) (3, -1)

B-9. The angle between the two tangents from the origin to the circle $(x - 7)^2 + (y + 1)^2 = 25$ equals

(A) $\frac{\pi}{4}$

B-10. A point A (2, 1) is outside the circle $x^2 + y^2 + 2gx + 2fy + c = 0$ & AP, AQ are tangents to the circle. The equation of the circle circumscribing the triangle APQ is:

(A) (x+g) (x-2) + (y+f) (y-1) = 0(C) (x-g)(x+2) + (y-f)(y+1) = 0

(B) $(x+g) (x-2) - (y+f) (y-1) = 0$
(D) $(x-g)(x-2) + (y-f)(y-1) = 0$

(-1) = 0

B-11. A line segment through a point P cuts a given circle in 2 points A & B, such that PA = 16 & PB = 9, find the length of tangent from points to the circle (B) 25 (C) 12 (D) 8 (A) 7

B-12. The length of the tangent drawn from any point on the circle $x^2 + y^2 + 2gx + 2fy + p = 0$ to the circle $x^{2} + y^{2} + 2gx + 2fy + q = 0$ is:

(A)
$$\sqrt{q - p}$$
 (B) $\sqrt{p - q}$ (C) $\sqrt{q + p}$ (D) $\sqrt{2q + p}$

- The equation of the diameter of the circle $(x 2)^2 + (y + 1)^2 = 16$ which bisects the chord cut off by the B-13. circle on the line x - 2y - 3 = 0 is (B) 2x + y - 3 = 0 (C) 3x + 2y - 4 = 0 (D) 3x - 2y - 4 = 0(A) x + 2y = 0
- **B-14.** The locus of the point of intersection of the tangents to the circle $x^2 + y^2 = a^2$ at points whose parametric

angles differ by
$$\frac{\pi}{3}$$
 is
(A) $x^2 + y^2 = \frac{4a^2}{3}$ (B)

$$x^{2} + y^{2} = \frac{2a^{2}}{3}$$
 (C) $x^{2} + y^{2} = \frac{a^{2}}{3}$ (D) $x^{2} + y^{2} = \frac{a^{2}}{9}$

Section (C) : Normal, Director circle, chord of contact, chord with mid point

- The equation of normal to the circle $x^2 + y^2 4x + 4y 17 = 0$ which passes through (1, 1) is C-1. (A) 3x + y - 4 = 0(B) x - y = 0(C) x + y = 0(D) 3x - y - 4 = 0
- The normal at the point (3, 4) on a circle cuts the circle at the point (-1, -2). Then the equation of the C-2. circle is (A) $x^2 + y^2 + 2x - 2y - 13 = 0$ (B) $x^2 + y^2 - 2x - 2y - 11 = 0$ (C) $x^2 + y^2 - 2x + 2y + 12 = 0$ (D) $x^2 + y^2 - 2x - 2y + 14 = 0$

The co-ordinates of the middle point of the chord cut off on 2x - 5y + 18 = 0 by the circle C-3. $x^{2} + y^{2} - 6x + 2y - 54 = 0$ are (A) (1, 4) (B) (2, 4) (C) (4, 1) (D) (1, 1)

- **C-4.** The locus of the mid point of a chord of the circle $x^2 + y^2 = 4$ which subtends a right angle at the origin is: (A) x + y = 2(B) $x^2 + y^2 = 1$ (C) $x^2 + y^2 = 2$ (D) x + y = 1
- **C-5.** The chords of contact of the pair of tangents drawn from each point on the line 2x + y = 4 to the circle $x^2 + y^2 = 1$ pass through the point
 - $(\mathsf{B})\left(\frac{1}{2},\frac{1}{4}\right)$ (C) (2, 4) (A) (1, 2) (D) (4, 4)

C-6. The locus of the centers of the circles such that the point (2,3) is the mid point of the chord 5x + 2y = 16 is:

(A) 2x-5y+11=0 (B) 2x+5y-11=0 (C) 2x+5y+11=0 (D) 2x-5y-11=0

C-7. ★ Find the locus of the mid point of the chord of a circle x² + y² = 4 such that the segment intercepted by the chord on the curve x² - 2x - 2y = 0 subtends a right angle at the origin.
(A) x² + y² - 2x - 2y = 0 (B) x² + y² + 2x - 2y = 0 (C) x² + y² + 2x + 2y = 0 (D) x² + y² - 2x + 2y = 0

Section (D) : Position of two circle, Orthogonality, Radical axis and radical centre

D-1. Number of common tangents of the circles $(x + 2)^2 + (y-2)^2 = 49$ and $(x - 2)^2 + (y + 1)^2 = 4$ is: (A) 0 (B) 1 (C) 2 (D) 3

D-2. The equation of the common tangent to the circle $x^2 + y^2 - 4x - 6y - 12 = 0$ and $x^2 + y^2 + 6x + 18y + 26 = 0$ at their point of contact is (A) 12x + 5y + 19 = 0 (B) 5x + 12y + 19 = 0 (C) 5x - 12y + 19 = 0 (D) 12x - 5y + 19 = 0

D-3. Equation of the circle cutting orthogonally the three circles $x^2 + y^2 - 2x + 3y - 7 = 0$, $x^2 + y^2 + 5x - 5y + 9 = 0$ and $x^2 + y^2 + 7x - 9y + 29 = 0$ is (A) $x^2 + y^2 - 16x - 18y - 4 = 0$ (B) $x^2 + y^2 - 7x + 11y + 6 = 0$ (C) $x^2 + y^2 + 2x - 8y + 9 = 0$ (D) $x^2 + y^2 + 16x - 18y - 4 = 0$

D-4. ▲ If the length of a common internal tangent to two circles is 7, and that of a common external tangent is 11, then the product of the radii of the two circles is:
(A) 18
(B) 20
(C) 16
(D) 12

Section (E) : Family of circles , Locus, Miscellaneous

E-1. The locus of the centre of the circle which bisects the circumferences of the circles $x^2 + y^2 = 4$ & $x^2 + y^2 - 2x + 6y + 1 = 0$ is : (A) a straight line (B) a circle (C) a parabola (D) pair of straight line

E-2. Equation of a circle drawn on the chord $x \cos \alpha + y \sin \alpha = p$ of the circle $x^2 + y^2 = a^2$ as its diameter, is

(A) $(x^2 + y^2 - a^2) - 2p (x \sin \alpha + y \cos \alpha - p) = 0$ (B) $(x^2 + y^2 - a^2) - 2p (x \cos \alpha + y \sin \alpha - p) = 0$ (C) $(x^2 + y^2 - a^2) + 2p (x \cos \alpha + y \sin \alpha - p) = 0$ (D) $(x^2 + y^2 - a^2) - p (x \cos \alpha + y \sin \alpha - p) = 0$

E-3. Find the equation of the circle which passes through the point (1, 1) & which touches the circle $x^2 + y^2 + 4x - 6y - 3 = 0$ at the point (2, 3) on it.

$(A) x^2 + y^2 + x - 6y + 3 = 0$	(B) $x^2 + y^2 + x - 6y - 3 = 0$
(C) $x^2 + y^2 + x + 6y + 3 = 0$	(D) $x^2 + y^2 + x - 3y + 3 = 0$

E-4. Find the equation of circle touching the line 2x + 3y + 1 = 0 at (1, -1) and cutting orthogonally the circle having line segment joining (0, 3) and (-2, -1) as diameter.

(A) $2x^2 + 2y^2 - 10x - 5y + 1 = 0$	(B) $2x^2 + 2y^2 - 10x + 5y + 1 = 0$
(C) $2x^2 + 2y^2 - 10x - 5y - 1 = 0$	(D) $2x^2 + 2y^2 + 10x - 5y + 1 = 0$

E-5.a	Equation of the circle which passes through the point (-1, 2) & touches the circle $x^2 + y^2 - 8x + 6y = 0$
	at origin, is -

(A) $x^2 + y^2 - 2x - \frac{3}{2}y = 0$	(B) $x^2 + y^2 + x - 2y = 0$
(C) $x^2 + y^2 + 2x + \frac{3}{2}y = 0$	(D) $x^2 + y^2 + 2x - \frac{3}{2}y = 0$

E-6. Two circles are drawn through the point (a, 5a) and (4a, a) to touch the axis of 'y'. They intersect at an angle of θ then tan θ is -

(A)
$$\frac{40}{9}$$
 (B) $\frac{9}{40}$ (C) $\frac{1}{9}$ (D) $\frac{1}{\sqrt{3}}$

PART - III : MATCH THE COLUMN

1.	Colun	Column – I		Column – II	
	(A)	Number of values of a for which the common chord of the circles $x^2 + y^2 = 8$ and $(x - a)^2 + y^2 = 8$ subtends a right angle at the origin is	(p)	0	
	(B) کھر	The number of circles touching all the three lines $3x + 7y = 2$, $21x + 49y = 5$ and $9x + 21y = 0$ are	(q)	2	
	(C)	The length of common chord of circles $x^2 + y^2 - x - 11y + 18 = 0$ and	(r)	5	
		$x^2 + y^2 - 9x - 5y + 14 = 0$ is			
	(D)	Number of common tangents of the circles $x^2 + y^2 - 2x = 0$ and $x^2 + y^2 + 6x - 6y + 2 = 0$ is	(s)	3	
2.		Column – I	Colun	nn – II	
	(A)	If director circle of two given circles C_1 and C_2 of equal radii touches each other, then ratio of length of internal common tangent of C_1 and C_2 to their radii equals		13	
	(B)	Let two circles having radii r_1 and r_2 are orthogonal to each other. If length of their common chord is k times the square root of hormonic mean between squares of their radii, then k^4 equals to		7	
	(C)	The axes are translated so that the new equation of the circle	(r)	4	
		$x^2 + x^2$ Fig. 2. 5. 0 has no first degree terms and the new equation $x^2 + x^2$	λ ²		

 $x^2 + y^2 - 5x + 2y - 5 = 0$ has no first degree terms and the new equation $x^2 + y^2 = \frac{\lambda^-}{4}$,

then the value of $\boldsymbol{\lambda}_{_{-}}$ is

(D) The number of integral points which lie on or inside the circle
$$x^2 + y^2 = 4$$
 is (s) 2



Exercise-2

PART - I : ONLY ONE OPTION CORRECT TYPE

If $\left(a, \frac{1}{a}\right), \left(b, \frac{1}{b}\right), \left(c, \frac{1}{c}\right) \& \left(d, \frac{1}{d}\right)$ are four distinct points on a circle of radius 4 units, then abcd is 1.2 equal to: (B) 16 (A) 4 (C) 1 (D) 2 From the point A (0⁻ 3) on the circle $x^2 + 4x + (y - 3)^2 = 0$ a chord AB is drawn & extended to a point M 2. such that AM = 2 AB. The equation of the locus of M is : (A) $x^2 + 8x + y^2 = 0$ (B) $x^2 + 8x + (y - 3)^2 = 0$ (C) $(x-3)^2 + 8x + y^2 = 0$ (D) $x^2 + 8x + 8y^2 = 0$ If tangent at (1, 2) to the circle c_1 : $x^2 + y^2 = 5$ intersects the circle c_2 : $x^2 + y^2 = 9$ at A & B and tangents 3. at A & B to the second circle meet at point C, then the co-ordinates of C is (B) $\left(\frac{9}{15}, \frac{18}{5}\right)$ (C) (4, -5) (D) $\left(\frac{9}{5}, \frac{18}{5}\right)$ (A) (4, 5) A circle passes through point $\left(3, \sqrt{\frac{7}{2}}\right)$ touches the line pair $x^2 - y^2 - 2x + 1 = 0$. Centre of circle lies 4.2 inside the circle $x^2 + y^2 - 8x + 10y + 15 = 0$. Co-ordinate of centre of circle is (C) (6, 0) (A) (4, 0) (B) (5, 0) (D) (0, 4) The length of the tangents from any point on the circle $15x^2 + 15y^2 - 48x + 64y = 0$ to the two circles 5.2 $5x^{2} + 5y^{2} - 24x + 32y + 75 = 0$ and $5x^{2} + 5y^{2} - 48x + 64y + 300 = 0$ are in the ratio (A) 1:2 (B) 2:3 (C) 3:4 (D) 2:1 The distance between the chords of contact of tangents to the circle; $x^2 + y^2 + 2gx + 2fy + c = 0$ from the 6. origin & the point (g, f) is: (B) $\frac{\sqrt{g^2 + f^2 - c}}{2}$ (C) $\frac{g^2 + f^2 - c}{2\sqrt{g^2 + f^2}}$ (D) $\frac{\sqrt{g^2 + f^2 + c}}{2\sqrt{g^2 + f^2}}$ (A) $\sqrt{g^2 + f^2}$ 7. If from any point P on the circle $x^2 + y^2 + 2gx + 2fy + c = 0$, tangents are drawn to the circle $x^2 + y^2 + 2gx + 2fy + c \sin^2 \alpha + (g^2 + f^2) \cos^2 \alpha = 0$ then the angle between the tangents is: (C) $\frac{\alpha}{2}$ (D) $\frac{\alpha}{2}$ (A) α (B) 2 α The locus of the mid points of the chords of the circle $x^2 + y^2 + 4x - 6y - 12 = 0$ which subtend an angle 8.2 of $\frac{\pi}{2}$ radians at its circumference is: (A) $(x-2)^2 + (y+3)^2 = 6.25$ (B) $(x + 2)^2 + (y - 3)^2 = 6.25$ (D) $(x + 2)^2 + (y + 3)^2 = 18.75$ (C) $(x + 2)^2 + (y - 3)^2 = 18.75$

9. If the two circles, $x^2 + y^2 + 2g_1x + 2f_1y = 0 \& x^2 + y^2 + 2g_2x + 2f_2y = 0$ touch each other then:

(A)
$$f_1 g_1 = f_2 g_2$$
 (B) $\frac{f_1}{g_1} = \frac{f_2}{g_2}$ (C) $f_1 f_2 = g_1 g_2$ (D) $f_1 + f_2 = g_1 + g_2$

10. A circle touches a straight line $\Box x + my + n = 0$ & cuts the circle $x^2 + y^2 = 9$ orthogonally. The locus of centres of such circles is:

(A) $(\Box x + my + n)^2 = (\Box^2 + m^2) (x^2 + y^2 - 9)$	(B) $(\Box x + my - n)^2 = (\Box^2 + m^2) (x^2 + y^2 - 9)$
(C) $(\Box x + my + n)^2 = (\Box^2 + m^2) (x^2 + y^2 + 9)$	(D) $(\Box x + my - n)^2 = (\Box^2 + m^2) (x^2 + y^2 - 9)$

11. The locus of the point at which two given unequal circles subtend equal angles is:(A) a straight line(B) a circle(C) a parabola(D) an ellipse

12. A circle is given by $x^2 + (y - 1)^2 = 1$. Another circle C touches it externally and also the x-axis, then the locus of its centre is

(A) $\{(x, y) : x^2 = 4y\} \cup \{(x, y) : y \le 0\}$	(B) {(x, y) : $x^2 + (y - 1)^2 = 4$ } U {(x, y) : $y \le 0$ }
(C) $\{(x, y) : x^2 = y\} \cup \{(0, y) : y \le 0\}$	(D) {(x, y) : $x^2 = 4y$ } U {(0, y) : $y \le 0$ }

13. The locus of the centre of a circle touching the circle $x^2 + y^2 - 4y - 2x = 4$ internally and tangent on which from (1, 2) is making a 60° angle with each other.

(A) $(x - 1)^2 + (y - 2)^2 = 2$	(B) $(x - 1)^2 + (y - 2)^2 = 4$
(C) $(x + 1)^2 + (y - 2)^2 = 4$	(D) $(x + 1)^2 + (y + 2)^2 = 4$

14. STATEMENT-1 : If three circles which are such that their centres are non-collinear, then exactly one circle exists which cuts the three circles orthogonally.

STATEMENT-2 : Radical axis for two intersecting circles is the common chord.

- (A) STATEMENT-1 is true, STATEMENT-2 is true and STATEMENT-2 is correct explanation for STATEMENT-1
- (B) STATEMENT-1 is true, STATEMENT-2 is true and STATEMENT-2 is not correct explanation for STATEMENT-1
- (C) STATEMENT-1 is true, STATEMENT-2 is false
- (D) STATEMENT-1 is false, STATEMENT-2 is true

15. The centre of family of circles cutting the family of circles $x^2 + y^2 + 4x \left(\lambda - \frac{3}{2}\right) + 3y \left(\lambda - \frac{4}{3}\right) - 6$

 $(\lambda + 2) = 0$ orthogonally, lies on

(A) x - y - 1 = 0 (B) 4x + 3y - 6 = 0 (C) 4x + 3y + 7 = 0 (D) 3x - 4y - 1 = 0

16. The circle $x^2 + y^2 = 4$ cuts the circle $x^2 + y^2 + 2x + 3y - 5 = 0$ in A & B. Then the equation of the circle on AB as a diameter is:

(A) $13(x^2 + y^2) - 4x - 6y - 50 = 0$ (B) $9(x^2 + y^2) + 8x - 4y + 25 = 0$ (C) $x^2 + y^2 - 5x + 2y + 72 = 0$ (D) $13(x^2 + y^2) - 4x - 6y + 50 = 0$

PART-II: NUMERICAL VALUE QUESTIONS

INSTRUCTION:

- The answer to each question is **NUMERICAL VALUE** with two digit integer and decimal upto two digit.
- ✤ If the numerical value has more than two decimal places truncate/round-off the value to TWO decimal placed.
- **1.** Find maximum number of points having integer coordinates (both x, y integer) which can lie on a circle with centre at $(\sqrt{2}, \sqrt{3})$ is (are)
- **2.** If equation of smallest circle touching the circles $x^2 + y^2 2y 3 = 0$ and $x^2 + y^2 8x 18y + 93 = 0$ is $x^2 + y^2 4x fy + c = 0$ then value of f + c is
- **3.** A line meets the co-ordinate axes in A and B. A circle is circumscribed about the triangle OAB. If d_1 and d_2 are the distances of the tangent to the circle at the origin O from the points A and B respectively and diameter of the circle is $\lambda_1 d_1 + \lambda_2 d_2$, then find the value of $\lambda_1 + \lambda_2$.
- 4. A circle is inscribed (i.e. touches all four sides) into a rhombous ABCD with one angle 60°. The distance from the centre of the circle to the nearest vertex is equal to 1. If P is any point of the circle, then $|PA|^2 + |PB|^2 + |PC|^2 + |PD|^2$ is equal to :
- 5. Let x & y be the real numbers satisfying the equation $x^2 4x + y^2 + 3 = 0$. If the maximum and minimum values of $x^2 + y^2$ are M & m respectively, then find the numerical value of (M + m).

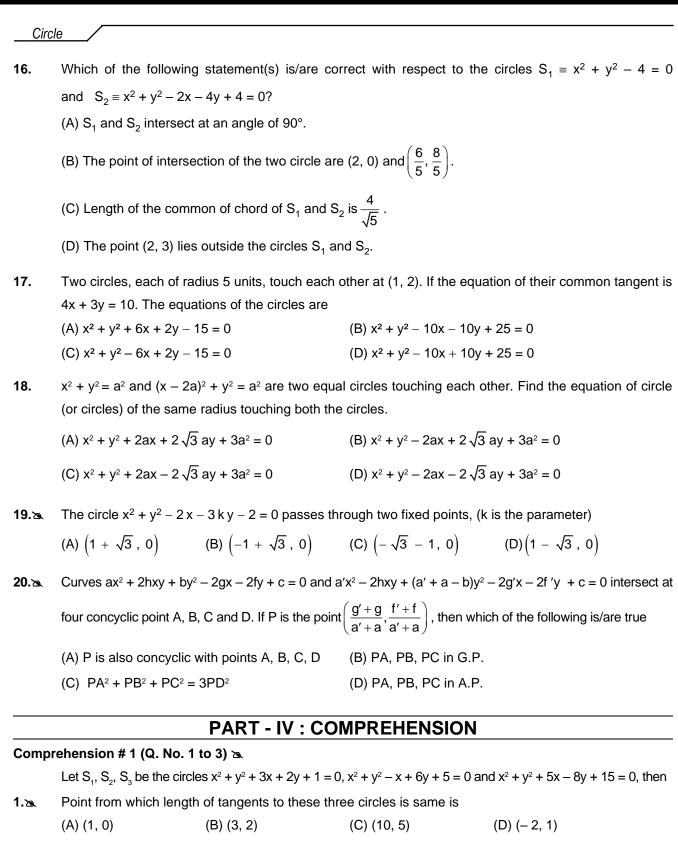
6. Find absolute value of 'c' for which the set, $\{(x, y) | x^2 + y^2 + 2x \le 1\} \cap \{(x, y) | 5x - 12y + c \ge 0\}$ contains only one point is common.

- 7. A rhombus is inscribed in the region common to the two circles $x^2 + y^2 4x 12 = 0$ and $x^2 + y^2 + 4x 12 = 0$ with two of its vertices on the line joining the centres of the circles then area of the rhombus is
- 8. If (α, β) is a point on the circle whose centre is on the x-axis and which touches the line x + y = 0 at (2, -2), then find the greatest value of ' α ' is
- **9.** Two circles whose radii are equal to 4 and 8 intersect at right angles, then length of their common chord is
- **10.** A variable circle passes through the point A (a, b) & touches the x-axis and the locus of the other end of the diameter through A is $(x a)^2 = \lambda by$, then find the value of λ
- **11.** Let A be the centre of the circle $x^2 + y^2 2x 4y 20 = 0$. Suppose that the tangents at the points B (1, 7) & D (4, -2) on the circle meet at the point C. Find the area of the quadrilateral ABCD.
- 12. If the complete set of values of a for which the point (2a, a + 1) is an interior point of the larger segment of the circle $x^2 + y^2 - 2x - 2y - 8 = 0$ made by the chord whose equation is 3x - 4y + 5 = 0 is (p,q) then value of p + q is
- **13.** The circles $x^2 + y^2 + 2ax + cy + a = 0$ and $x^2 + y^2 3ax + dy 1 = 0$ intersect in two distinct points P and Q, then find the number of values of 'a' for which the line 5x + by a = 0 passes through P and Q.
- **14.** The circumference of the circle $x^2 + y^2 2x + 8y q = 0$ is bisected by the circle $x^2 + y^2 + 4x + 12y + p = 0$, then find p + q
- **15.** A circle touches the line y = x at a point P such that $OP = 4\sqrt{2}$ where O is the origin. The circle contains the point (-10, 2) in its interior and the length of its chord on the line x + y = 0 is $6\sqrt{2}$. If the equation of the circle $x^2 + y^2 + 2g x + 2fy + 3c = 0$, then value of g + f + c is

PART - III : ONE OR MORE THAN ONE OPTIONS CORRECT TYPE

The equation of circles passing through (3, -6) touching both the axes is 1. (A) $x^2 + y^2 - 6x + 6y + 9 = 0$ (B) $x^2 + y^2 + 6x - 6y + 9 = 0$ (D) $x^2 + y^2 - 30x + 30y + 225 = 0$ (C) $x^2 + y^2 + 30x - 30y + 225 = 0$ 2. Equations of circles which pass through the points (1, -2) and (3, -4) and touch the x-axis is (A) $x^2 + y^2 + 6x + 2y + 9 = 0$ (B) $x^2 + y^2 + 10x + 20y + 25 = 0$ (D) $x^2 + y^2 + 10x + 20y - 25 = 0$ (C) $x^2 + y^2 - 6x + 4y + 9 = 0$ The centre of a circle passing through the points (0, 0), (1, 0) & touching the circle $x^2 + y^2 = 9$ is : 3.2 (B) $\left(\frac{1}{2}, \sqrt{2}\right)$ (C) $\left(\frac{1}{2}, \frac{1}{2}\right)$ (D) $\left(\frac{1}{2}, -\sqrt{2}\right)$ (A) $\left(\frac{3}{2}, \frac{1}{2}\right)$ The equation of the circle which touches both the axes and the line $\frac{x}{3} + \frac{y}{4} = 1$ and lies in the first 4. quadrant is $(x - c)^2 + (y - c)^2 = c^2$ where c is (A) 1 (B) 2 (C) 4 (D) 6 Find the equations of straight lines which pass through the intersection of the lines x - 2y - 5 = 0, 5.2 7x + y = 50 & divide the circumference of the circle $x^2 + y^2 = 100$ into two arcs whose lengths are in the ratio 2 : 1. (A) 3x - 4y - 25 = 0 (B) 4x + 3y - 25 = 0 (C) 4x - 3y - 25 = 0 (D) 3x + 4y - 25 = 0Tangents are drawn to the circle $x^2 + y^2 = 50$ from a point 'P' lying on the x-axis. These tangents meet the 6.2 y-axis at points 'P₁' and 'P₂'. Possible coordinates of 'P' so that area of triangle PP₁P₂ is minimum, is/are (B) $(10\sqrt{2}, 0)$ (D) $(-10 \sqrt{2}, 0)$ (C) (-10, 0) (A) (10, 0) 7. If (a, 0) is a point on a diameter segment of the circle $x^2 + y^2 = 4$, then $x^2 - 4x - a^2 = 0$ has (A) exactly one real root in (-1, 0](B) Exactly one real root in [2, 5] (C) distinct roots greater than-1 (D) Distinct roots less than 5 8. The tangents drawn from the origin to the circle $x^2 + y^2 - 2rx - 2hy + h^2 = 0$ are perpendicular if (C) $r^2 + h^2 = 1$ (A) h = r(B) h = - r (D) $r^2 = h^2$ 9. The equation (s) of the tangent at the point (0, 0) to the circle where circle makes intercepts of length 2a and 2b units on the coordinate axes, is (are) -(C) x = y(A) ax + by = 0(B) ax - by = 0(D) bx + ay = ab

Consider two circles C_1 : $x^2 + y^2 - 1 = 0$ and C_2 : $x^2 + y^2 - 2 = 0$. Let A(1,0) be a fixed point on the circle 10.2 C_1 and B be any variable point on the circle C_2 . The line BA meets the curve C_2 again at C. Which of the following alternative(s) is/are correct? (A) $OA^2 + OB^2 + BC^2 \in [7, 11]$, where O is the origin. (B) $OA^2 + OB^2 + BC^2 \in [4, 7]$, where O is the origin. (C) Locus of midpoint of AB is a circle of radius $\frac{1}{\sqrt{2}}$. (D) Locus of midpoint of AB is a circle of area $\frac{\pi}{2}$. 11.2 One of the diameter of the circle circumscribing the rectangle ABCD is x - 3y + 1 = 0. If two verticles of rectangle are the points (-2, 5) and (6, 5) respectively, then which of the following hold(s) good? (A) Area of rectangle ABCD is 64 square units. (B) Centre of circle is (2, 1) (C) The other two vertices of the rectangle are (-2, -3) and (6, -3)(D) Equation of sides are x = -2, y = -3, x = 5 and y = 6. Three concentric circles of which the biggest is $x^2 + y^2 = 1$, have their radii in A.P. If the line y = x + 112. cuts all the circles in real and distinct points. The permissible values of common difference of A.P. is/are (A) 0.4 (B) 0.6 (C) 0.01 (D) 0.1 If $4\Box^2 - 5m^2 + 6\Box + 1 = 0$. Prove that $\Box x + my + 1 = 0$ touches a definite circle, then which of the 13.2 following is/are true. (C) Radius $\sqrt{5}$ (D) Radius 5 (A) Centre (0, 3) (B) centre (3, 0) If the circle C_1 : $x^2 + y^2 = 16$ intersects another circle C_2 of radius 5 in such a manner that the common 14.æ chord is of maximum length and has a slope equal to 3/4, then the co-ordinates of the centre of C₂ are: (A) $\left(\frac{9}{5}, \frac{12}{5}\right)$ (B) $\left(\frac{9}{5}, \frac{-12}{5}\right)$ (C) $\left(\frac{-9}{5}, \frac{-12}{5}\right)$ (D) $\left(\frac{-9}{5}, \frac{+12}{5}\right)$ For the circles $x^2 + y^2 - 10x + 16y + 89 - r^2 = 0$ and $x^2 + y^2 + 6x - 14y + 42 = 0$ which of the following 15.ര. is/are true. (A) Number of integral values of r are 14 for which circles are intersecting. (B) Number of integral values of r are 9 for which circles are intersecting. (C) For r equal to 13 number of common tangents are 3. (D) For r equal to 21 number of common tangents are 2.



2. Equation of circle S_4 which cut orthogonally to all given circle is

(A) $x^2 + y^2 - 6x + 4y - 14 = 0$	(B) $x^2 + y^2 + 6x + 4y - 14 = 0$
(C) $x^2 + y^2 - 6x - 4y + 14 = 0$	(D) $x^2 + y^2 - 6x - 4y - 14 = 0$

Circle								
3.2	Radical centre of circles S_1 , S_2 , & S_4 is							
	$(A)\left(-\frac{3}{5},-\frac{8}{5}\right)$	(B) (3, 2)	(C) (1, 0)	$(D)\left(-\frac{4}{5},-\frac{3}{2}\right)$				
Comprehension # 2 (Q. No. 4 to 6) 🖎								
	Two circles are $S_1 \equiv ($	$(x + 3)^2 + y^2 = 9$						
	$S_2 \equiv (x - 5)^2 + y^2 = 16$							
	with centres $C_1 \& C_2$							
4.2	A direct common tar	ngent is drawn from a	point P (on x-axis) wh	ich touches $S_1 \& S_2$ at Q & R,				
	respectively. Find the ratio of area of $\triangle PQC_1 \& \triangle PRC_2$.							
	(A) 3 : 4	(B) 9 : 16	(C) 16 : 9	(D) 4 : 3				
5.2	From point 'A' on S ₂ which is nearest to C ₁ , a variable chord is drawn to S ₁ . The locus of mid point of the							
	chord.							
	(A) circle		(B) Diameter of s ₁					
	(C) Arc of a circle		(D) chord of s_1 but no	t diameter				
6.2	Locus obtained in que	estion 5 cuts the circle S_1	at B & C, then line segn	nent BC subtends an angle on				
	the major arc of circle	S₁ is						
	(A) $\cos^{-1} \frac{3}{4}$	(B) $\frac{\pi}{2} - \tan^{-1}\frac{4}{3}$	(C) $\frac{\pi}{2} - \frac{1}{2} \tan^{-1} \frac{3}{4}$	(D) $\frac{\pi}{2}$ cot ⁻¹ $\left(\frac{4}{3}\right)$				

Exercise-3

* Marked Questions may have more than one correct option.

PART - I : JEE (ADVANCED) / IIT-JEE PROBLEMS (PREVIOUS YEARS)

- 1. Two parallel chords of a circle of radius 2 are at a distance $\sqrt{3} + 1$ apart. If the chords subtend at the center, angles of $\frac{\pi}{k}$ and $\frac{2\pi}{k}$, where k > 0, then the value of [k] is [Note : [k] denotes the largest integer less than or equal to k] [IIT-JEE 2010, Paper-2, (3, 0), 79]
- 2. The circle passing through the point (-1, 0) and touching the y-axis at (0, 2) also passes through the point [IIT-JEE 2011, Paper-2, (3, -1), 80]

(A)
$$\left(-\frac{3}{2}, 0\right)$$
 (B) $\left(-\frac{5}{2}, 2\right)$ (C) $\left(-\frac{3}{2}, \frac{5}{2}\right)$

3. The straight line 2x - 3y = 1 divides the circular region $x^2 + y^2 \le 6$ into two parts.

If S = $\left\{ \left(2, \frac{3}{4}\right), \left(\frac{5}{2}, \frac{3}{4}\right), \left(\frac{1}{4}, -\frac{1}{4}\right), \left(\frac{1}{8}, \frac{1}{4}\right) \right\}, \right\}$

[IIT-JEE 2011, Paper-2, (4, 0), 80]

(D) (-4, 0)

then the number of point(s) in S lying inside the smaller part is

4.2	The locus of the mid-point of the chord of contact of tangents drawn from points lying on the straigh							
	line $4x - 5y = 20$ to the	the circle $x^2 + y^2 = 9$ is	[IIT-JEE 2012, Paper-1, (3, –1), 70]					
	(A) $20(x^2 + y^2) - 36x$	+ 45y = 0	(B) $20(x^2 + y^2) + 36x$	(B) $20(x^2 + y^2) + 36x - 45y = 0$				
	(C) $36(x^2 + y^2) - 20x$	+ 45y = 0	(D) $36(x^2 + y^2) + 20x$	x - 45y = 0				
Parag	graph for Question I	Nos. 5 to 6						
	A tangent PT is draw	In to the circle $x^2 + y^2 =$	4 at the point P($\sqrt{3}$, 1)	at the point P($\sqrt{3}$, 1). A straight line L, perpendicular to				
	PT is a tangent to the	e circle $(x - 3)^2 + y^2 = 1$.	[ווד	[IIT-JEE 2012, Paper-2, (3, −1), 66]				
5.	A common tangent o	f the two circles is						
	(A) x = 4	(B) y = 2	(C) x + $\sqrt{3}$ y = 4	(D) x + 2 $\sqrt{3}$ y = 6				
6.	A possible equation of	of L is						
	(A) $x - \sqrt{3} y = 1$	(B) x + $\sqrt{3}$ y = 1	(C) $x - \sqrt{3} y = -1$	(D) x + $\sqrt{3}$ y = 5				
7*.	Circle(s) touching x-a is (are) (A) $x^2 + y^2 - 6x + 8y - (C) x^2 + y^2 - 6x - 8y - (C)$	+ 9 = 0	the origin and having an intercept of length $2\sqrt{7}$ on y-axis [JEE (Advanced) 2013, Paper-2, (3, -1)/60] (B) $x^2 + y^2 - 6x + 7y + 9 = 0$ (D) $x^2 + y^2 - 6x - 7y + 9 = 0$					
8*.	A circle S passes and $x^2 + y^2 = 1$. Then (A) radius of S is 8 (C) centre of S is (–7		 and is orthogonal to the circles (x - 1)² + y² = 16 [JEE (Advanced) 2014, Paper-1, (3, 0)/60] (B) radius of S is 7 (D) centre of S is (-8, 1) 					
9*.æ	The circle $C_1 : x^2 + y^2 = 3$, with centre at O, intersects the parabola $x^2 = 2y$ at the point P in							
	quadrant. Let the ta	ngent to the circle C_1	t P touches other two circles C_2 and C_3 at R_2 and R_3 ,					
	respectively. Suppos	e C, and C, have equal	radii $2\sqrt{3}$ and centres Q_2 and Q_3 , respectively. If Q_2 and					
	Q_3 lie on the y-axis, t		[JEE (Advanced) 2016, Paper-1, (4, –2)/62]					
	(A) $Q_2 Q_3 = 12$		(B) $R_2 R_2 = 4\sqrt{6}$					
	(C) area of the triang	le OR ₂ R ₃ is 6 $\sqrt{2}$	(D) area of the triangle PQ_2Q_3 is $4\sqrt{2}$					
10*.	Let RS be the diameter of the circle $x^2 + y^2 =$ (other than R and S) on the circle and tangents		= 1, where S is the point (1, 0). Let P be a variable point is to the circle at S and P meet at the point Q. The norm gh Q parallel to RS at point E. Then the locus of E pass [JEE (Advanced) 2016, Paper-1, (4, -2)/62 (C) $\left(\frac{1}{3}, -\frac{1}{\sqrt{3}}\right)$ (D) $\left(\frac{1}{4}, -\frac{1}{2}\right)$					

11.For how many values of p, the circle $x^2 + y^2 + 2x + 4y - p = 0$ and the coordinate axes have exactly
three common points?[JEE(Advanced) 2017, Paper-1,(3, 0)/61]

PARAGRAPH "X"

[JEE(Advanced) 2018, Paper-1, (3, -1)/60]

Let S be the circle in the xy-plane defined by the equation $x^2 + y^2 = 4$. (*There are two questions based on PARAGRAPH* "X", *the question given below is one of them*)

12. Let E₁E₂ and F₁F₂ be the chords of S passing through the point P₀(1, 1) and parallel to the x-axis and the y-axis, respectively. Let G₁G₂ be the chord of S passing through P₀ and having slope –1. Let the tangents to S at E₁ and E₂ meet at E₃, the tangents to S at F₁ and F₂ meet at F₃, and the tangents to S at G₁ and G₂ meet at G₃. Then, then, the points E₃, F₃, and G₃ lie on the curve

(A) x + y = 4 (B) $(x - 4)^2 + (y - 4)^2 = 16$ (C) (x - 4)(y - 4) = 4 (D) xy = 4

13. Let P be a point on the circle S with both coordinates being positive. Let the tangent to S at P intersect the coordinate axes at the points M and N. Then, the mid-point of the line segment MN must lie on the curve

(A) $(x + y)^2 = 3xy$ (B) $x^{2/3} + y^{2/3} = 2^{4/3}$ (C) $x^2 + y^2 = 2xy$ (D) $x^2 + y^2 = x^2y^2$

- 14*. Let T be the line passing through the points P(-2, 7) and Q(2, -5). Let F₁ be the set of all pairs of circles (S₁, S₂) such that T is tangent to S₁ at P and tangent to S₂ at Q, and also such that S₁ and S₂ touch each other at a point, say, M. Let E₁ be the set representing the locus of M as the pair (S₁, S₂) varies in F₁. Let the set of all straight line segments joining a pair of distinct points of E₁ and passing through the point R(1, 1) be F₂. Let E₂ be the set of the mid-points of the line segments in the set F₂. Then, which of the following statement(s) is (are) TRUE
 - (A) The point (-2, 7) lies in E₁ (B) The point $\left(\frac{4}{5}, \frac{7}{5}\right)$ does **NOT** lie in E₂ (C) The point $\left(\frac{1}{2}, 1\right)$ lies in E₂ (D) The point $\left(0, \frac{3}{2}\right)$ does **NOT** lie in E₁

PART - II : JEE (MAIN) / AIEEE PROBLEMS (PREVIOUS YEARS)

1.	The circle $x^2 + y^2 = 4x + 8y + 5$ intersects the line $3x - 4y = m$ at two distinct points if [AIEEE 2010, (4, -1), 144]						
	(1) – 35 < m < 15	(2) 15 < m < 65	(3) 35 < m < 85	(4) - 85 < m < - 35			
2.	The two circles $x^2 + y^2$	= ax and $x^2 + y^2 = c^2(c > c)$	0) touch each other if:				
	(1) 2 a = c	(2) a = c	(3) a = 2c	[AIEEE-2011, I, (4, −1), 120] (4) a = 2c			
3.	The equation of the circle passing through the point (1, 0) and (0, 1) and having the smallest radius is						
	(1) $x^2 + y^2 - 2x - 2y + 1 = 0$		(2) $x^2 + y^2 - x - y = 0$	[AIEEE-2011, II, (4, –1), 120]			
	(3) $x^2 + y^2 + 2x + 2y - 7$	7 = 0	(4) $x^2 + y^2 + x + y - 2 = 0$				
4.	The length of the diam the point (2, 3) is :	eter of the circle which t	ouches the x-axis at the	point (1, 0) and passes through [AIEEE- 2012, (4, -1), 120]			
	(1) $\frac{10}{3}$	(2) $\frac{3}{5}$	(3) $\frac{6}{5}$	(4) $\frac{5}{3}$			
5.	The circle passing thro	ugh (1, –2) and touching	the axis of x at (3, 0) als	so passes through the point [AIEEE - 2013, (4, –1),120]			
	(1) (-5, 2)	(2) (2, -5)	(3) (5, -2)	$(4) \ (-2, 5)$			

6.	Let C be the circle with centre at (1, 1) and radius = 1. If T is the circle centred at (0, y), passing the origin and touching the circle C externally, then the radius of T is equal to :						
	5 5		_	[JEE(Main) 2014, (4, – 1), 120]			
	(1) $\frac{1}{2}$	(2) $\frac{1}{4}$	(3) $\frac{\sqrt{3}}{\sqrt{2}}$	(4) $\frac{\sqrt{3}}{2}$			
7.	Locus of the image of	the point (2, 3) in the line	e (2x – 3y + 4) + k (x	− 2y + 3) = 0, k ∈ R, is a [JEE(Main) 2015, (4, − 1), 120]			
	(1) straight line paralle (3) circle of radius $\sqrt{2}$	I to x-axis	(2) straight line parallel to y-axis (4) circle of radius $\sqrt{3}$				
8.	The number of commo	on tangents to the circles	$x^2 + y^2 - 4x - 6y - 12$	$x^2 = 0$ and $x^2 + y^2 + 6x + 18y + 26 = 0$,			
	is (1) 1	(2) 2	(3) 3	[JEE(Main) 2015, (4, - 1), 120] (4) 4			
9.	The centres of those of the x-axis, lie on :	circles which touch the c	tircle, x² + y² – 8x – 8	3y - 4 = 0, externally and also touch [IEE(Main) 2016 (4 - 1) 120]			
	(1) an ellipse which is(3) a parabola	not a circle	[JEE(Main) 2016, (4, – 1), 120 (2) a hyperbola (4) a circle				
10.	If one of the diameter	s of the circle, given by	the equation, $x^2 + y^2$	- 4x + 6y - 12 = 0, is a chord of a			
	circle S, whose centre	is at (-3, 2), then the ra	Idius of S is : [JEE(Main) 2016, (4, - 1), 120]				
	(1) 5√3	(2) 5	(3) 10	(4) $5\sqrt{2}$			
11.			le be A (-3, 5) and B(3,3) respectively. If C is the the circle having line segement AC as diameter, is : [JEE(Main) 2018, (4, -1), 120]				
	_	_					
	(1) $3\sqrt{\frac{5}{2}}$	(2) $\frac{3\sqrt{5}}{2}$	(3) √10	(4) 2√10			
12.	12	Z		(4) $2\sqrt{10}$ ly, If they have x-axis as a common			
12.	12	Z	each other external				
12.	Three circles of radii, tangent, then :	∠ a, b, c (a < b < c) touch	each other external [JEE(Main) 2019,	ly, If they have x-axis as a common			
12. 13.	Three circles of radii, tangent, then : (1) a, b, c are in A.P.	2 a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$	each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} a	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, – 1), 120]			
	Three circles of radii, tangent, then : (1) a, b, c are in A.P.	a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ hrough the point (4, 0) to	the each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} and puches the circle x ² -	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, - 1), 120] are in A.P. (4) $\frac{1}{\sqrt{b}} = \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{c}}$			
	Three circles of radii, tangent, then : (1) a, b, c are in A.P. If a circle C passing th	a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ hrough the point (4, 0) to	the each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} and puches the circle x ² -	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, - 1), 120] are in A.P. (4) $\frac{1}{\sqrt{b}} = \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{c}}$ + y ² + 4x - 6y = 12 externally at the			
13.	Three circles of radii, tangent, then : (1) a, b, c are in A.P. If a circle C passing th point (1, -1), then the (1) $2\sqrt{5}$	a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ hrough the point (4, 0) to radius of C is: (2) $\sqrt{57}$	a each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} a puches the circle x ² - [JEE(Main) 2019, (3) 4	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, - 1), 120] are in A.P. (4) $\frac{1}{\sqrt{b}} = \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{c}}$ + y ² + 4x - 6y = 12 externally at the Online (10-01-19),P-1 (4, - 1), 120] (4) 5			
	Three circles of radii, tangent, then : (1) a, b, c are in A.P. If a circle C passing th point (1, -1), then the (1) $2\sqrt{5}$ If a variable line, 3x	a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ hrough the point (4, 0) to radius of C is: (2) $\sqrt{57}$ + 4y - λ = 0 is such	a each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} a puches the circle x ² - [JEE(Main) 2019, (3) 4 a that the two circle	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, - 1), 120] are in A.P. (4) $\frac{1}{\sqrt{b}} = \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{c}}$ + y ² + 4x - 6y = 12 externally at the Online (10-01-19),P-1 (4, - 1), 120]			
13.	Three circles of radii, tangent, then : (1) a, b, c are in A.P. If a circle C passing th point (1, -1), then the (1) $2\sqrt{5}$ If a variable line, 3x	a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ hrough the point (4, 0) to radius of C is: (2) $\sqrt{57}$ + 4y - λ = 0 is such	a each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} a puches the circle x ² - [JEE(Main) 2019, (3) 4 a that the two circle des, then the set of al	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, - 1), 120] are in A.P. (4) $\frac{1}{\sqrt{b}} = \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{c}}$ + y ² + 4x - 6y = 12 externally at the Online (10-01-19),P-1 (4, - 1), 120] (4) 5 es x ² + y ² - 2x - 2y + 1 = 0 and			
13.	Three circles of radii, tangent, then : (1) a, b, c are in A.P. If a circle C passing th point (1, -1), then the (1) $2\sqrt{5}$ If a variable line, 3x	a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ hrough the point (4, 0) to radius of C is: (2) $\sqrt{57}$ + 4y - λ = 0 is such	a each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} a puches the circle x ² - [JEE(Main) 2019, (3) 4 a that the two circle des, then the set of al	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, -1), 120] are in A.P. (4) $\frac{1}{\sqrt{b}} = \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{c}}$ + y ² + 4x - 6y = 12 externally at the Online (10-01-19),P-1 (4, -1), 120] (4) 5 es x ² + y ² - 2x -2y + 1 = 0 and Il values of λ is the interval:			
13.	Three circles of radii, tangent, then : (1) a, b, c are in A.P. If a circle C passing th point (1, -1), then the (1) $2\sqrt{5}$ If a variable line, $3x$ $x^2 + y^2 - 18x - 2y + 78 =$ (1) (2, 17) If a circle of radius R	a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ hrough the point (4, 0) to radius of C is: (2) $\sqrt{57}$ + 4y - λ = 0 is such = 0 are on its opposite sid (2) [12, 21]	a each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} a puches the circle x^2 - [JEE(Main) 2019, (3) 4 a that the two circle des, then the set of al [JEE(Main) 2019, (3) [13, 23] an O and intersects th	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, - 1), 120] are in A.P. (4) $\frac{1}{\sqrt{b}} = \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{c}}$ + y ² + 4x - 6y = 12 externally at the Online (10-01-19),P-1 (4, - 1), 120] (4) 5 es x ² + y ² - 2x -2y + 1 = 0 and Il values of λ is the interval: Online (12-01-19),P-1 (4, - 1), 120]			
13. 14.	Three circles of radii, tangent, then : (1) a, b, c are in A.P. If a circle C passing th point (1, -1), then the (1) $2\sqrt{5}$ If a variable line, $3x$ $x^2 + y^2 - 18x - 2y + 78 =$ (1) (2, 17) If a circle of radius R	a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ (3) $\frac{1}{\sqrt{57}}$ (4) $\frac{1}{\sqrt{57}}$ (2) $\frac{12}{\sqrt{57}}$ (2) [12, 21] passes through the original	a each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} a puches the circle x^2 - [JEE(Main) 2019, (3) 4 a that the two circle des, then the set of al [JEE(Main) 2019, (3) [13, 23] an O and intersects the h AB is -	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, - 1), 120] are in A.P. (4) $\frac{1}{\sqrt{b}} = \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{c}}$ + y ² + 4x - 6y = 12 externally at the Online (10-01-19),P-1 (4, - 1), 120] (4) 5 es x ² + y ² - 2x -2y + 1 = 0 and Il values of λ is the interval: Online (12-01-19),P-1 (4, - 1), 120] (4) (23,31)			
13. 14.	Three circles of radii, tangent, then : (1) a, b, c are in A.P. If a circle C passing th point (1, -1), then the (1) $2\sqrt{5}$ If a variable line, $3x$ $x^2 + y^2 - 18x - 2y + 78 =$ (1) (2, 17) If a circle of radius R	a, b, c (a < b < c) touch (2) $\frac{1}{\sqrt{a}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{c}}$ hrough the point (4, 0) to radius of C is: (2) $\sqrt{57}$ + 4y - λ = 0 is such = 0 are on its opposite sid (2) [12, 21] passes through the origination of the	a each other external [JEE(Main) 2019, (3) \sqrt{a} , \sqrt{b} , \sqrt{c} a puches the circle x^2 - [JEE(Main) 2019, (3) 4 a that the two circle des, then the set of al [JEE(Main) 2019, (3) [13, 23] an O and intersects the h AB is -	ly, If they have x-axis as a common Online (09-01-19),P-1 (4, - 1), 120] are in A.P. (4) $\frac{1}{\sqrt{b}} = \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{c}}$ + y ² + 4x - 6y = 12 externally at the Online (10-01-19),P-1 (4, - 1), 120] (4) 5 es x ² + y ² - 2x -2y + 1 = 0 and Il values of λ is the interval: Online (12-01-19),P-1 (4, - 1), 120] (4) (23,31) the coordinate axes at A and B, then Online (12-01-19),P-2 (4, - 1), 120]			

- **16.** The sum of the squares of the lengths of the chords intercepted on the circle, $x^2 + y^2 = 16$, by the lines, $x + y = n, n \in N$, where N is the set of all natural numbers, is:
 - (1) 105 (2) 210 [JEE(Main) 2019, Online (08-04-19),P-1 (4, 1), 120] (4) 160
- 17.If a tangent to the circle $x^2 + y^2 = 1$ intersects the coordinate axes at distinct points P and Q, then the
locus of the mid-point of PQ is :[JEE(Main) 2019, Online (09-04-19), P-1 (4, -1), 120]

(1)
$$x^2 + y^2 - 4x^2y^2 = 0$$
 (2) $x^2 + y^2 - 16x^2y^2 = 0$ (3) $x^2 + y^2 - 2x^2y^2 = 0$ (4) $x^2 + y^2 - 2xy = 0$

18. The locus of the centres of the circles, which touch the circle, $x^2 + y^2 = 1$ externally, also touch the y-axis and lie in the first quadrant, is : [JEE(Main) 2019, Online (10-04-19), P-2 (4, -1), 120]

(1) $x = \sqrt{1+4y}, y \ge 0$ (2) $y = \sqrt{1+4x}, x \ge 0$ (3) $x = \sqrt{1+2y}, y \ge 0$ (4) $y = \sqrt{1+2x}, x \ge 0$

19. If a line, y = mx + c is a tangent to the circle, $(x - 3)^2 + y^2 = 1$ and it is perpendicular to a line L₁, where L₁ is the tangent to the circle, $x^2 + y^2 = 1$ at the point $\left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$; then:

[JEE (Main) 2020, Online (08-01-20), P-2 (4, -1), 120]

(1) $c^2 + 7c + 6 = 0$ (2) $c^2 + 6c + 7 = 0$ (3) $c^2 - 6c + 7 = 0$ (4) $c^2 - 7c + 6 = 0$

20. If the curves, $x^2 - 6x + y^2 + 8 = 0$ and $x^2 - 8y + y^2 + 16 - k = 0$, (k > 0) touch each other at a point, then the largest value of k is _____ [JEE(Main) 2020, Online (09-01-20),P-2 (4, 0), 120]

Advanced Level Problems

> Marked Questions may have for Revision Questions.

SUBJECTIVE QUESTIONS

- Find the equation of the circle passing through the points A(4, 3), B(2, 5) and touching the axis of y. Also find the point P on the y-axis such that the angle APB has largest magnitude.
- 2. Let a circle be given by 2x (x a) + y (2y b) = 0, $(a \neq 0, b \neq 0)$. Find the condition on a & b if two chords, each bisected by the x-axis, can be drawn to the circle from $\left(a, \frac{b}{2}\right)$
- 3. A circle is described to pass through the origin and to touch the lines x = 1, x + y = 2. Prove that the radius of the circle is a root of the equation $(3 2\sqrt{2})$ $t^2 2\sqrt{2}t + 2 = 0$.
- 4. If (a, α) lies inside the circle $x^2 + y^2 = 9$: $x^2 4x a^2 = 0$ has exactly one root in (-1, 0), then find the area of the region in which (a, α) lies.
- 5. Let $S = x^2 + y^2 + 2gx + 2fy + c = 0$ be a given circle. Find the locus of the foot of the perpendicular drawn from the origin upon any chord of S which subtends right angle at the origin.

- 6. A ball moving around the circle $x^2 + y^2 2x 4y 20 = 0$ in anti-clockwise direction leaves it tangentially at the point P(-2, -2). After getting reflected from a straight line it passes through the centre of the circle. Find the equation of this straight line if its perpendicular distance from P is $\frac{5}{2}$. You can assume that the angle of incidence is equal to the angle of reflection.
- 7. The lines 5x + 12y 10 = 0 and 5x 12y 40 = 0 touch a circle C₁ of diameter 6 unit. If the centre of C₁ lies in the first quadrant, find the equation of the circle C₂ which is concentric with C₁ and cuts of intercepts of length 8 on these lines.
- 8. The chord of contact of tangents drawn from a point on the circle $x^2 + y^2 = a^2$ to the circle $x^2 + y^2 = b^2$ touches the circle $x^2 + y^2 = c^2$. Show that a, b, c are in G.P.
- **9.** Find the locus of the middle points of chords of a given circle $x^2 + y^2 = a^2$ which subtend a right angle at the fixed point (p, q).
- **10.** Let $a \square ^2 bm^2 + 2 d \square + 1 = 0$, where a, b, d are fixed real numbers such that $a + b = d^2$. If the line $\square x + my + 1 = 0$ touches a fixed circle then find the equation of circle
- 11. The centre of the circle S = 0 lies on the line 2x 2y + 9 = 0 and S = 0 cuts orthogonally the circle $x^2 + y^2 = 4$. Show that circle S = 0 passes through two fixed points and also find their co-ordinates.
- **12.** Prove that the two circles which pass through the points (0, a), (0, -a) and touch the straight line y = m x + c will cut orthogonaly if $c^2 = a^2 (2 + m^2)$.
- **13.** Consider points A $(\sqrt{13}, 0)$ and B $(2\sqrt{13}, 0)$ lying on x-axis. These points are rotated in ananticlockwise direction about the origin through an angle of $\tan^{-1}\left(\frac{2}{3}\right)$. Let the new position of A and B be A' and B' respectively. With A' as centre and radius $\frac{2\sqrt{13}}{3}$ a circle C₁ is drawn and with B' as a centre and radius $\frac{\sqrt{13}}{3}$ circle C₂ is drawn. Find radical axis of C₁ and C₂.
- **14.** P(a, b) is a point in the first quadrant. If the two circles which pass through P and touch both the co–ordinate axes cut at right angles, then find condition in a and b.
- **15.** Prove that the square of the tangent that can be drawn from any point on one circle to another circle is equal to twice the product of perpendicular distance of the point from the radical axis of two circles and distance between their centres.
- **16.** Find the equation of the circle which cuts each of the circles, $x^2 + y^2 = 4$, $x^2 + y^2 6x 8y + 10 = 0$ & $x^2 + y^2 + 2x - 4y - 2 = 0$ at the extremities of a diameter.
- **17.** Show that if one of the circle $x^2 + y^2 + 2gx + c = 0$ and $x^2 + y^2 + 2g_1x + c = 0$ lies within the other, then gg_1 and c are both positive.

18. Let ABCD is a rectangle. Incircle of \triangle ABD touches BD at E. Incircle of \triangle CBD toches BD at F.

If AB = 8 units, and BC = 6 units, then find length of EF.

- 19. Let circles S₁ and S₂ of radii r₁ and r₂ respectively (r₁ > r₂) touches each other externally. Circle S radii r touches S₁ and S₂ externally and also their direct common tangent. Prove that the triangle formed by joining centre of S₁, S₂ and S is obtuse angled triangle.
- **20.** Circles are drawn passing through the origin O to intersect the coordinate axes at point P and Q such that m. OP + n. OQ is a constant. Show that the circles pass through a fixed point.
- **21.** A triangle has two of its sides along the axes, its third side touches the circle $x^2 + y^2 2 ax 2 ay + a^2 = 0$. Find the equation of the locus of the circumcentre of the triangle.
- **22.** Let S₁ be a circle passing through A(0, 1), B(-2, 2) and S₂ is a circle of radius $\sqrt{10}$ units such that AB is common chord of S₁ and S₂. Find the equation of S₂.
- 23. The curves whose equations are $S = ax^{2} + 2hxy + by^{2} + 2gx + 2fy + c = 0$ $S' = a'x^{2} + 2h'xy + b'y^{2} + 2g'x + 2f'y + c' = 0$ intersect in four concyclic points then find relation in a, b, h, a', b', h'.
- **24.** A circle of constant radius 'r' passes through origin O and cuts the axes of coordinates in points P and Q, then find the equation of the locus of the foot of perpendicular from O to PQ.
- 25. The ends A , B of a fixed straight line of length 'a' and ends A' and B' of another fixed straight line of length 'b' slide upon the axis of X & the axis of Y (one end on axis of X & the other on axis of Y). Find the locus of the centre of the circle passing through A, B, A' and B'.

Answers

EXERCISE - 1 PART - I Section (A): A-1. $x^2 + y^2 = 1$ A-3. $x^2 + y^2 - 3x - 4y = 0$ A-4. $x^2 + y^2 - 4x - 4y + 4 = 0$ A-5. $x^2 + y^2 \pm 6 \sqrt{2y} \pm 6x + 9 = 0$ $(x + 3)^2 + (y - 4)^2 = 4$ A-6. A-7. (36, 47)Section (B): (1, 3), (5, 7), 4 \sqrt{2} B-1. B-2. B-3. 2 x - 7y - 45 = 0 $\sqrt{3}x - y \pm 4 = 0$ B-4. $16x^2 - 65y^2 - 288x + 1296 = 0, \tan^{-1}\left(\frac{8\sqrt{65}}{100}\right)$ B-5. B-6. Yes Section (C): C-2. x + 2y - 1 = 0C-1. 2x - y = 0C-3. $(x + 4)^2 + y^2 = 16$ $\left(6,-\frac{18}{5}\right)$ C-6. C-5. x + y + 5 = 0Section (D): D-1. x = 0, 3x + 4y = 10, y = 4 and 3y = 4x. **D-4.** $\left(\frac{33}{4}, 2\right); \frac{1}{4}$ D-3. $2(x^2 + y^2) - 7x + 2y = 0$ Section (E): E-1. $x^2 + y^2 - 2x - 4y = 0.$ E-2. (i) $(x-1)^2 + (y+2)^2 + 20(2x-y-4) = 0$ (ii) $(x-1)^2 + (y+2)^2 \pm \sqrt{20}(2x-y-4) = 0$ $\left(\frac{52}{3}, -\frac{23}{9}\right)$ E-4. E-5. $x^2 + y^2 - 17x - 19y + 50 = 0$ PART - II Section (A): A-1. A-2. (A) A-3. (C) A-5. (D) A-7. (A) (D) (B) A-4. A-6. (B) A-8. (C) Section (B): B-1. (A) B-2. B-7. (B) B-3. (B) B-4. (B) B-5. (A) B-6. (B) (A) B-8. (D) B-9. (C) B-10. (A) B-11. (C) B-12. (A) B-13. (B) B-14. (A) Section (C): C-1. (A) C-2. (B) C-3. (A) C-4. (C) C-5. (B) C-6. (A) C-7. (A) Section (D): D-2. D-3. D-1. (B) (B) (A) D-4. (A)

Section (E): E-1. (A) E-2. (B) E-3. (A) E-4. (A) E-5. (D) E-6. (A) PART - III 1. $(A) \rightarrow (q), (B) \rightarrow (p), (C) \rightarrow (r), (D) \rightarrow (s)$ 2. $(A) \rightarrow (s), (B) \rightarrow (r), (C) \rightarrow (q), (D) \rightarrow (p)$

					I	EXERC	CISE - 2	2					
						PAF	RT - I						
1.	(C)	2.	(B)	3.	(D)	4.	(A)	5.	(A)	6.	(C)	7.	(B)
8.	(B)	9.	(B)	10.	(A)	11.	(B)	12.	(D)	13.	(B)	14.	(D)
15.	(B)	16.	(A)										
						PAR	х т - II						
1.	01.00	2.	32.88 0	or 32.89	3.	02.00	4.	11.00	5.	10.00	6.	13.38	
7.	13.85 (or 13.86	i		8.	06.82	or 06.83		9.	07.15	10.	04.00	
11.	75.00	12.	01.30		13.	00.00	14.	10.00	15.	18.66	or 18.67		
						PAR	T - III						
1.	(AD)	2.	(BC)	3.	(BD)	4.	(AD)	5.	(CD)	6.	(AC)	7. (<i>i</i>	ABCD)
8.	(ABD)	9.	(AB)	10.	(ACD)	11.	(ABC)	12.	(CD)	13.	(BC)	14. (B	SD)
15.	(AC)	16.	(ACD)	17.	(AB)	18.	(BD)	19.	(AD)	20.	(BCD)		
						PAR	T - IV						
1.	(B)	2.	(D)	3.	(A)	4.	(B)	5.	(C)	6.	(A)		
							CISE - 3	<u>, </u>					
								5					
							RT - I						
1.	3	2.	(D)	3.	2	4.	(A)	5.	(D)	6.	(A)	7.	(AC
8.	(BC)	9.	(ABC)	10.	(A, C)	11.	(2)	12.	(A)	13.	(D)	14.	(BD
						PAR	T - II						
1.	(1)	2.	(2)	3.	(2)	4.	(1)	5.	(3)	6.	(2)	7.	(3)
8.	(3)	9.	(3)	10.	(1)	11.	(1)	12.	(2)	13.	(4)	14.	(2)
15.	(2)	16.	(2)	17.	(1)	18.	(4)	19.	(2)	20.	36		

ALP Answers

1.	$x^{2} + y^{2} - 4x - 6y + 9 = 0$ OR $x^{2} + y^{2} - 20x - 6y + 9 = 0$	22y + 12	$e^{1} = 0, P(0, 3), \theta = 45^{\circ}$
2.	(a² > 2b²)	4.	$4\left\{\sqrt{5}+\frac{9}{2}\cot^{-1}\left(\frac{2}{\sqrt{5}}\right)\right\}$
5.	$x^2 + y^2 + gx + fy + \frac{c}{2} = 0$	6.	$(4\sqrt{3} - 3) x - (4 + 3\sqrt{3}) y - (39 - 2\sqrt{3}) = 0$
7.	$x^2 + y^2 - 10 x - 4 y + 4 = 0$	9.	$2x^{2} + 2y^{2} - 2px - 2qy + p^{2} + q^{2} - a^{2} = 0$
10.	$x^2 + y^2 - 2dx + d^2 - b = 0$	11.	$(-4, 4); \left(-\frac{1}{2}, \frac{1}{2}\right)$
13.	9x + 6y = 65	14.	$a^2 - 4ab + b^2 = 0$
16.	$x^2 + y^2 - 4x - 6y - 4 = 0$	18.	2
21.	$2(x+y)-a=\frac{2xy}{a}$	22.	$x^{2} + y^{2} + 2x - 3y + 2 \pm \sqrt{7} (x + 2y - 2) = 0$
23.	$\frac{a-b}{h} = \frac{a'-b'}{h'}$	24.	$(x^2 + y^2)^2 (x^{-2} + y^{-2}) = 4r^2$
25.	$(2ax - 2by)^2 + (2bx - 2ay)^2 = (a^2 - b^2)^2$		