

DIFFERENTIAL EQUATIONS

HOMOGENEOUS DIFFERENTIAL EQUATIONS

EXERCISE

Q.1 Find the solutions to the following differential equations:

(1) $\left(x \frac{dy}{dx} - y\right) \tan^{-1} \frac{y}{x} = x$ Given that $y = 0$ at $x = 1$

(2) $x \frac{dy}{dx} = y - x \tan \frac{y}{x}$

(3) $\frac{dy}{dx} = \frac{x + 2y - 3}{2x + y + 3}$

(4) $\frac{dy}{dx} = \frac{x + y + 1}{2x + 2y + 3}$

(5) $\frac{dy}{dx} = \frac{3x + 2y - 5}{3y - 2x + 5}$

Q.2 Find $x^2 dy + y(x + y) dx = 0$

Q.3 Solve: $(x^2 - y^2) dx + 2xy dy = 0$ given that $y = 1$ when $x = 1$

Q.4 Evaluate the differential equation $\frac{dy}{dx} = \frac{x + 2y - 5}{2x + y - 4}$

Q.5 Solve $\frac{dy}{dx} = \frac{yf'(x) - y^2}{f(x)}$

Q.6 Evaluate $\frac{dy}{dx} = \frac{x - 2y + 5}{2x + y - 1}$

ANSWER KEY

1. (1) $\sqrt{x^2 + y^2} = e^{x \tan^{-1} \frac{y}{x}}$

(2) $x \sin \frac{y}{x} = C$

(3) $x + y = c(x - y + 6)^3$

$$(4) \quad 3(2y - x) + \ln(3x + 3y + 4) = C$$

$$(5) \quad 3x^2 + 4xy - 3y^2 - 10x - 10y = C$$

$$2. \quad \left| \frac{vx^2}{v+2} \right| = c \Rightarrow \left| \frac{x^2y}{2x+y} \right| = c; c > 0$$

$$3. \quad x^2 + y^2 = 2x$$

$$4. \quad x + y - 3 = c' (x - y + 1)^3$$

$$5. \quad \frac{f(x)}{y} = x + c \quad \text{or} \quad f(x) = y(x + c)$$

$$6. \quad x^2 - 4xy - y^2 + 10x + 2y = c' \quad \text{Where } c' = -2c$$