## **Criteria for Congruence of Triangles**

1. Given below, each pair of triangles has markings indicating equal parts. Name the congruence condition (SAS, ASA, SSS, RHS), if any, that will establish the two triangles of a pair to be congruent.



D.



2. Given below, lengths of the sides of the triangles are indicated. By applying the SSS congruence rule, state which pairs of triangles are congruent. In case of congruent triangles write the result in symbolic form.



- 3. In the given figure, PQ = PR and S is the midpoint of QR.
  - A. State the three pairs of equal parts in  $\Delta PQS$  and  $\Delta PRS$
  - B. Is  $\triangle$  PQS  $\cong$  PRS? Give reasons.
  - C. Is  $\angle Q = \angle R$ ?



 ΔABC and ΔDBC are both isosceles on a common base BC such that A and D lie on the same side of BC. Are triangles ADB and ADC congruent? Which condition do you use? If ∠BAC = 40° and ∠BDC = 100°, then find ∠ABD. 5. In the given figure, AB = CD and AD = BC. Prove that  $\triangle$ ADC  $\cong \triangle$ CBA.



- 6. In the given figure, PQ || SR and PS = QR.
  - A. State the three measurements of  $\Delta$ SRQ. Which are equal to the three measurements of  $\Delta$ SPQ.
  - B. Is  $\Delta$  SRQ  $\cong \Delta$ SPQ?
  - C. Is  $\Delta$  SRQ  $\cong \Delta$ SQP?



- In the given figure, ΔABC is shown as an isosceles triangle with AB = AC and AD is the bisector of ∠A.
  - A. Name the two triangles which are congruent.
  - B. Is AD = DC?



- 8. Prove that in an isosceles triangle, the angles opposite to the equal sides are equal.
- 9. In  $\triangle PQR$ , A and B are two points on QR. Such that  $\angle PAB = \angle PBA$  and QA = BR. Prove that  $\triangle PQA \cong \triangle PRB$



- 10. Show that the bisector of the vertical angle of an isosceles triangle bisects the base at right angles.
- 11. In the given figure,  $\Delta PQR$  and  $\Delta SQR$  are on the same base QR. Also, PQ = SR and PR = SQ. Is  $\triangle PQR \cong \triangle SQR$ ?

12. In the given figure, PQ = QR, BQ = QC, QP  $\perp$  AB, QR  $\perp$  AC. Prove that AB = AC

13. In the given figure, PQ  $\perp$  BA and PR  $\perp$  BC, such that PQ = PR. Show that BP bisects ∠ABC.

14. In the given figure,  $\triangle$ ABC and  $\triangle$ DCB are right angled at A and D respectively and AC = DB. Prove that  $\triangle ABC \cong \triangle DCB$ .







S



15. In the given figure, AB || CD and AB = CD. Prove that  $\triangle ABC \cong \triangle CDA$ .



16. In the given figure, AX is the  $\angle$ BAD and  $\angle$ BAD and  $\angle$ BCD. Prove that AB = AD.



17. In the given figure,  $\Delta PQR \cong \Delta LMN$ . Find the value of a and b.

