

# TRIGONOMETRIC FUNCTIONS

# Fundamental trigonometrical ratios and functions

1. If  $5 \tan \theta = 4$ , then  $\frac{5 \sin \theta - 3 \cos \theta}{5 \sin \theta + 2 \cos \theta} =$   
 (A) 0 (B) 1  
 (C) 1/6 (D) 6

2. If  $\tan \theta = \frac{x \sin \varphi}{1 - x \cos \varphi}$  and  $\tan \varphi = \frac{y \sin \theta}{1 - y \cos \theta}$ ,  
 then  $\frac{x}{y} =$   
 (A)  $\frac{\sin \varphi}{\sin \theta}$  (B)  $\frac{\sin \theta}{\sin \varphi}$   
 (C)  $\frac{\sin \varphi}{1 - \cos \theta}$  (D)  $\frac{\sin \theta}{1 - \cos \varphi}$

3. If  $p = \frac{2 \sin \theta}{1 + \cos \theta + \sin \theta}$ , and  $q = \frac{\cos \theta}{1 + \sin \theta}$ , then  
 (A)  $pq = 1$  (B)  $\frac{q}{p} = 1$   
 (C)  $q - p = 1$  (D)  $q + p = 1$

4. If  $\tan \theta + \sin \theta = m$  and  $\tan \theta - \sin \theta = n$ , then  
 (A)  $m^2 - n^2 = 4mn$  (B)  $m^2 + n^2 = 4mn$   
 (C)  $m^2 - n^2 = m^2 + n^2$  (D)  $m^2 - n^2 = 4\sqrt{mn}$

5. If  $\tan \theta = \frac{a}{b}$ , then  $\frac{\sin \theta}{\cos^8 \theta} + \frac{\cos \theta}{\sin^8 \theta} =$   
 (A)  $\pm \frac{(a^2 + b^2)^4}{\sqrt{a^2 + b^2}} \left( \frac{a}{b^8} + \frac{b}{a^8} \right)$  (B)  $\pm \frac{(a^2 + b^2)^4}{\sqrt{a^2 + b^2}} \left( \frac{a}{b^8} - \frac{b}{a^8} \right)$   
 (C)  $\pm \frac{(a^2 - b^2)^4}{\sqrt{a^2 + b^2}} \left( \frac{a}{b^8} + \frac{b}{a^8} \right)$  (D)  $\pm \frac{(a^2 - b^2)^4}{\sqrt{a^2 - b^2}} \left( \frac{a}{b^8} - \frac{b}{a^8} \right)$

6. If  $a \cos \theta + b \sin \theta = m$  and  $a \sin \theta - b \cos \theta = n$ ,  
 then  $a^2 + b^2 =$   
 (A)  $m + n$  (B)  $m^2 - n^2$   
 (C)  $m^2 + n^2$  (D) None of these

7. The value of  
 $6(\sin^6 \theta + \cos^6 \theta) - 9(\sin^4 \theta + \cos^4 \theta) + 4$  is  
 (A) -3 (B) 0  
 (C) 1 (D) 3

## **Sign & trigonometric ratio of allied angles**

## Trigonometrical ratios of sum and difference of two and three angles

- 30.**  $\cos^2\left(\frac{\pi}{4} - \beta\right) - \sin^2\left(\alpha - \frac{\pi}{4}\right) =$
- (A)  $\sin(\alpha + \beta)\sin(\alpha - \beta)$   
 (B)  $\cos(\alpha + \beta)\cos(\alpha - \beta)$   
 (C)  $\sin(\alpha - \beta)\cos(\alpha + \beta)$   
 (D)  $\sin(\alpha + \beta)\cos(\alpha - \beta)$
- 31.**  $1 - 2\sin^2\left(\frac{\pi}{4} + \theta\right) =$
- (A)  $\cos 2\theta$   
 (B)  $-\cos 2\theta$   
 (C)  $\sin 2\theta$   
 (D)  $-\sin 2\theta$
- 32.**  $\frac{\sin 3A - \cos\left(\frac{\pi}{2} - A\right)}{\cos A + \cos(\pi + 3A)} =$
- (A)  $\tan A$   
 (B)  $\cot A$   
 (C)  $\tan 2A$   
 (D)  $\cot 2A$
- 33.** If  $\tan A = \frac{1}{2}$ , then  $\tan 3A =$
- (A)  $\frac{9}{2}$   
 (B)  $\frac{11}{2}$   
 (C)  $\frac{7}{2}$   
 (D)  $-\frac{1}{2}$
- 34.**  $\frac{\sqrt{1+\sin x} + \sqrt{1-\sin x}}{\sqrt{1+\sin x} - \sqrt{1-\sin x}} =$  (when  $x$  lies in II<sup>nd</sup> quadrant)
- (A)  $\sin \frac{x}{2}$   
 (B)  $\tan \frac{x}{2}$   
 (C)  $\sec \frac{x}{2}$   
 (D)  $\operatorname{cosec} \frac{x}{2}$
- 35.**  $(\sec 2A + 1)\sec^2 A =$
- (A)  $r + R$   
 (B)  $2\sec A$   
 (C)  $\sec 2A$   
 (D)  $2\sec 2A$
- 36.**  $\frac{\cos A}{1 - \sin A} =$
- (A)  $\sec A - \tan A$   
 (B)  $\operatorname{cosec} A + \cot A$   
 (C)  $\tan\left(\frac{\pi}{4} - \frac{A}{2}\right)$   
 (D)  $\tan\left(\frac{\pi}{4} + \frac{A}{2}\right)$
- 37.**  $\tan \frac{A}{2}$  is equal to
- (A)  $\pm \sqrt{\frac{1-\sin A}{1+\sin A}}$   
 (B)  $\pm \sqrt{\frac{1+\sin A}{1-\sin A}}$   
 (C)  $\pm \sqrt{\frac{1-\cos A}{1+\cos A}}$   
 (D)  $\pm \sqrt{\frac{1+\cos A}{1-\cos A}}$
- 38.** If  $\sin \alpha = \frac{-3}{5}$ , where  $\pi < \alpha < \frac{3\pi}{2}$ , then  $\cos \frac{1}{2}\alpha =$
- (A)  $\frac{-1}{\sqrt{10}}$   
 (B)  $\frac{1}{\sqrt{10}}$   
 (C)  $\frac{3}{\sqrt{10}}$   
 (D)  $\frac{-3}{\sqrt{10}}$
- 39.** Let  $0 < x < \frac{\pi}{4}$ . Then  $\sec 2x - \tan 2x =$
- (A)  $\tan\left(x - \frac{\pi}{4}\right)$   
 (B)  $\tan\left(\frac{\pi}{4} - x\right)$   
 (C)  $\tan\left(x + \frac{\pi}{4}\right)$   
 (D)  $\tan^2\left(x + \frac{\pi}{4}\right)$
- 40.** If  $\sin \theta + \cos \theta = x$ , then
- $\sin^6 \theta + \cos^6 \theta = \frac{1}{4}[4 - 3(x^2 - 1)^2]$  for
- (A) All real  $x$   
 (B)  $x^2 \leq 2$   
 (C)  $x^2 \geq 2$   
 (D) None of these
- 41.**  $2\cos^2 \theta - 2\sin^2 \theta = 1$ , then  $\theta =$
- (A)  $15^\circ$   
 (B)  $30^\circ$   
 (C)  $45^\circ$   
 (D)  $60^\circ$
- 42.** If  $\sin \alpha = \frac{336}{625}$  and  $450^\circ < \alpha < 540^\circ$ , then  $\sin\left(\frac{\alpha}{4}\right) =$
- (A)  $\frac{1}{5\sqrt{2}}$   
 (B)  $\frac{7}{25}$   
 (C)  $\frac{4}{5}$   
 (D)  $\frac{3}{5}$
- 43.** If  $\tan^2 \theta = 2\tan^2 \varphi + 1$ , then  $\cos 2\theta + \sin^2 \varphi$  equals
- (A)  $-1$   
 (B)  $0$   
 (C)  $1$   
 (D) None of these

$$44. \cos^4 \frac{\pi}{8} + \cos^4 \frac{3\pi}{8} + \cos^4 \frac{5\pi}{8} + \cos^4 \frac{7\pi}{8} =$$

- (A)  $\frac{1}{2}$       (B)  $\frac{1}{4}$   
(C)  $\frac{3}{2}$       (D)  $\frac{3}{4}$

**45.** If  $\sin x + \cos x = \frac{1}{5}$ , then  $\tan 2x$  is

- (A)  $\frac{25}{17}$       (B)  $\frac{7}{25}$   
 (C)  $\frac{25}{7}$       (D)  $\frac{24}{7}$

## **Maximum & minimum values of trigonometrical functions, conditional trigonometrical identities**

**46.** If  $x + y + z = 180^\circ$ ,

then  $\cos 2x + \cos 2y - \cos 2z$  is equal to

- (A)  $4 \sin x \cdot \sin y \cdot \sin z$   
 (B)  $1 - 4 \sin x \cdot \sin y \cdot \cos z$   
 (C)  $3 \cos \theta - 4 \sin \theta$   
 (D)  $\cos A \cdot \cos B \cdot \cos C$

47. If  $\alpha + \beta + \gamma = 2\pi$ , then

- (A)  $\tan \frac{\alpha}{2} + \tan \frac{\beta}{2} + \tan \frac{\gamma}{2} = \tan \frac{\alpha}{2} \tan \frac{\beta}{2} \tan \frac{\gamma}{2}$

(B)  $\tan \frac{\alpha}{2} \tan \frac{\beta}{2} + \tan \frac{\beta}{2} \tan \frac{\gamma}{2} + \tan \frac{\gamma}{2} \tan \frac{\alpha}{2} = 1$

(C)  $\tan \frac{\alpha}{2} + \tan \frac{\beta}{2} + \tan \frac{\gamma}{2} = -\tan \frac{\alpha}{2} \tan \frac{\beta}{2} \tan \frac{\gamma}{2}$

(D) None of these

**48.** If  $A + B + C = \pi$ ,

then  $\cos 2A + \cos 2B + \cos 2C = -\frac{1}{2}$ .

- (A)  $1 + 4 \cos A \cos B \sin C$   
(B)  $-1 + 4 \sin A \sin B \cos C$   
(C)  $-1 - 4 \cos A \cos B \cos C$   
(D) None of these

**49.** If  $A + B + C = 180^\circ$ ,

$$\text{then } \frac{\sin 2A + \sin 2B + \sin 2C}{\cos A + \cos B + \cos C - 1} =$$

- (A)  $8 \sin \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2}$    (B)  $8 \cos \frac{A}{2} \cos \frac{B}{2} \cos \frac{C}{2}$   
 (C)  $8 \sin \frac{A}{2} \cos \frac{B}{2} \cos \frac{C}{2}$    (D)  $8 \cos \frac{A}{2} \sin \frac{B}{2} \sin \frac{C}{2}$

**50.**  $A, B, C$  are the angles of a triangle, then  $\sin^2 A + \sin^2 B + \sin^2 C - 2 \cos A \cos B \cos C =$



51. If  $\cos A = \cos B \cos C$  and  $A + B + C = \pi$ , then the value of  $\cot B \cot C$  is



**52.** If  $A + B + C = 180^\circ$ , then the value of  $(\cot B + \cot C)(\cot C + \cot A)(\cot A + \cot B)$  will be

- (A)  $\sec A \sec B \sec C$
  - (B)  $\operatorname{cosec} A \operatorname{cosec} B \operatorname{cosec} C$
  - (C)  $\tan A \tan B \tan C$
  - (D) 1

53. If  $A + B + C = 180^\circ$ , then the value of  $\cot \frac{A}{2} + \cot \frac{B}{2} + \cot \frac{C}{2}$  will be

- (A)  $2 \cot \frac{A}{2} \cot \frac{B}{2} \cot \frac{C}{2}$    (B)  $4 \cot \frac{A}{2} \cot \frac{B}{2} \cot \frac{C}{2}$   
 (C)  $\cot \frac{A}{2} \cot \frac{B}{2} \cot \frac{C}{2}$    (D)  $8 \cot \frac{A}{2} \cot \frac{B}{2} \cot \frac{C}{2}$

**54.** If  $A + B + C = 270^\circ$ , then

$$\cos 2A + \cos 2B + \cos 2C + 4 \sin A \sin B \sin C =$$



**55.** If  $A + B + C = 180^\circ$ , then  $\sum \tan \frac{A}{2} \tan \frac{B}{2} =$

56. If  $A + B + C = \pi$  ( $A, B, C > 0$ ) and the angle  $C$  is obtuse then

(A)  $\tan A \tan B > 1$       (B)  $\tan A \tan B < 1$   
 (C)  $\tan A \tan B = 1$       (D) None of these

57. If  $A, B, C$  are acute positive angles such that  $A + B + C = \pi$  and  $\cot A \cot B \cot C = K$ , then

(A)  $K \leq \frac{1}{3\sqrt{3}}$       (B)  $K \geq \frac{1}{3\sqrt{3}}$   
 (C)  $K < \frac{1}{9}$       (D)  $K > \frac{1}{3}$

### General Solution of Standard Trigonometrical Equations

58. If  $\tan 2\theta \tan \theta = 1$ , then the general value of  $\theta$  is

(A)  $\left(n + \frac{1}{2}\right)\frac{\pi}{3}$       (B)  $\left(n + \frac{1}{2}\right)\pi$   
 (C)  $\left(2n \pm \frac{1}{2}\right)\frac{\pi}{3}$       (D) None of these

59. If  $1 + \cot \theta = \operatorname{cosec} \theta$ , then the general value of  $\theta$  is

(A)  $n\pi + \frac{\pi}{2}$       (B)  $2n\pi - \frac{\pi}{2}$   
 (C)  $2n\pi + \frac{\pi}{2}$       (D) None of these

60. If  $\cos 7\theta = \cos \theta - \sin 4\theta$ , then the general value of  $\theta$  is

(A)  $\frac{n\pi}{4}, \frac{n\pi}{3} + \frac{\pi}{18}$       (B)  $\frac{n\pi}{3}, \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$   
 (C)  $\frac{n\pi}{4}, \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$       (D)  $\frac{n\pi}{6}, \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$

61. If  $\frac{1 - \tan^2 \theta}{\sec^2 \theta} = \frac{1}{2}$ , then the general value of  $\theta$  is

(A)  $n\pi \pm \frac{\pi}{6}$       (B)  $n\pi + \frac{\pi}{6}$   
 (C)  $2n\pi \pm \frac{\pi}{6}$       (D) None of these

62. If  $\cos \theta + \sec \theta = \frac{5}{2}$ , then the general value of  $\theta$  is

(A)  $n\pi \pm \frac{\pi}{3}$       (B)  $2n\pi \pm \frac{\pi}{6}$   
 (C)  $n\pi \pm \frac{\pi}{6}$       (D)  $2n\pi \pm \frac{\pi}{3}$

63. If  $\cot \theta + \tan \theta = 2 \operatorname{cosec} \theta$ , the general value of  $\theta$  is

(A)  $n\pi \pm \frac{\pi}{3}$       (B)  $n\pi \pm \frac{\pi}{6}$   
 (C)  $2n\pi \pm \frac{\pi}{3}$       (D)  $2n\pi \pm \frac{\pi}{6}$

64. The most general value of  $\theta$  satisfying the equations  $\sin \theta = \sin \alpha$  and  $\cos \theta = \cos \alpha$  is

(A)  $2n\pi + \alpha$       (B)  $2n\pi - \alpha$   
 (C)  $n\pi + \alpha$       (D)  $n\pi - \alpha$

65. The solution of the equation

$$\begin{vmatrix} \cos \theta & \sin \theta & \cos \theta \\ -\sin \theta & \cos \theta & \sin \theta \\ -\cos \theta & -\sin \theta & \cos \theta \end{vmatrix} = 0, \text{ is}$$

(A)  $\theta = n\pi$       (B)  $\theta = 2n\pi \pm \frac{\pi}{2}$   
 (C)  $\theta = n\pi \pm (-1)^n \frac{\pi}{4}$       (D)  $\theta = 2n\pi \pm \frac{\pi}{4}$

66. The set of values of  $x$  for which the expression

$$\frac{\tan 3x - \tan 2x}{1 + \tan 3x \tan 2x} = 1, \text{ is}$$

(A)  $\varphi$

(B)  $\frac{\pi}{4}$

(C)  $\left\{ n\pi + \frac{\pi}{4} : n = 1, 2, 3, \dots \right\}$

(D)  $\left\{ 2n\pi + \frac{\pi}{4} : n = 1, 2, 3, \dots \right\}$

67. If  $\tan \theta + \tan 2\theta + \sqrt{3} \tan \theta \tan 2\theta = \sqrt{3}$ , then

- (A)  $\theta = (6n+1)\pi/18, \forall n \in I$   
(B)  $\theta = (6n+1)\pi/9, \forall n \in I$   
(C)  $\theta = (3n+1)\pi/9, \forall n \in I$   
(D) None of these

### General Solution of Square of Trigonometric Equations

68. If  $\frac{1-\cos 2\theta}{1+\cos 2\theta} = 3$ , then the general value of  $\theta$  is

- (A)  $2n\pi \pm \frac{\pi}{6}$       (B)  $n\pi \pm \frac{\pi}{6}$   
(C)  $2n\pi \pm \frac{\pi}{3}$       (D)  $n\pi \pm \frac{\pi}{3}$

69. If  $\tan^2 \theta - (1 + \sqrt{3}) \tan \theta + \sqrt{3} = 0$ , then the general value of  $\theta$  is

- (A)  $n\pi + \frac{\pi}{4}, n\pi + \frac{\pi}{3}$       (B)  $n\pi - \frac{\pi}{4}, n\pi + \frac{\pi}{3}$   
(C)  $n\pi + \frac{\pi}{4}, n\pi - \frac{\pi}{3}$       (D)  $n\pi - \frac{\pi}{4}, n\pi - \frac{\pi}{3}$

70. If  $4\sin^4 x + \cos^4 x = 1$ , then  $x =$

- (A)  $n\pi$       (B)  $n\pi \pm \sin^{-1} \frac{2}{5}$   
(C)  $n\pi + \frac{\pi}{6}$       (D) None of these

71. If  $\cos 3x + \sin \left(2x - \frac{7\pi}{6}\right) = -2$ ,

then  $x =$  (where  $k \in Z$ )

- (A)  $\frac{\pi}{3}(6k+1)$       (B)  $\frac{\pi}{3}(4k+1)$   
(C)  $\frac{\pi}{3}(2k+1)$       (D) None of these

72.  $2\sin^2 x + \sin^2 2x = 2, -\pi < x < \pi$ , then  $x =$

- (A)  $\pm \frac{\pi}{6}$       (B)  $\pm \frac{\pi}{4}$   
(C)  $\frac{3\pi}{2}$       (D) None of these

73. The values of  $\theta$  satisfying

$$\sin 7\theta = \sin 4\theta - \sin \theta \text{ and } 0 < \theta < \frac{\pi}{2} \text{ are}$$

- (A)  $\frac{\pi}{9}, \frac{\pi}{4}$       (B)  $\frac{\pi}{3}, \frac{\pi}{9}$   
(C)  $\frac{\pi}{6}, \frac{\pi}{9}$       (D)  $\frac{\pi}{3}, \frac{\pi}{4}$

74. The expression  $(1 + \tan x + \tan^2 x)(1 - \cot x + \cot^2 x)$  has the positive values for  $x$ , given by

- (A)  $0 \leq x \leq \frac{\pi}{2}$       (B)  $0 \leq x \leq \pi$   
(C) For all  $x \in R$       (D)  $x \geq 0$

75. If  $5\cos 2\theta + 2\cos^2 \frac{\theta}{2} + 1 = 0, -\pi < \theta < \pi$ , then  $\theta =$

- (A)  $\frac{\pi}{3}$       (B)  $\frac{\pi}{3}, \cos^{-1} \frac{3}{5}$   
(C)  $\cos^{-1} \frac{3}{5}$       (D)  $\frac{\pi}{3}, \pi - \cos^{-1} \frac{3}{5}$

76. If  $\cos \theta = \frac{-1}{2}$  and  $0^\circ < \theta < 360^\circ$ , then the values of  $\theta$  are

- (A)  $120^\circ$  and  $300^\circ$       (B)  $60^\circ$  and  $120^\circ$   
(C)  $120^\circ$  and  $240^\circ$       (D)  $60^\circ$  and  $240^\circ$

### General Solution of Trigonometric Equation

$$a\cos \theta + b\sin \theta = c$$

77. The equation  $a \sin x + b \cos x = c$ , where  $|c| > \sqrt{a^2 + b^2}$  has-

- (A) A unique solution  
(B) Infinite no. of solutions  
(C) No solution  
(D) None of these

78. General solution of  $\sin^3 x + \cos^3 x + \frac{3}{2} \sin 2x = 1$

  - $x = n\pi$  when  $n$  is even integer
  - $x = n\pi +$  when  $n$  is odd integer
  - $x = 2n\pi$  when  $n$  is odd integer
  - $x = n\pi -$  when  $n$  is even integer

79. The smallest angle of the triangle whose sides are  $6 + \sqrt{12}, \sqrt{48}, \sqrt{24}$

  - $\frac{\pi}{4}$
  - $\frac{\pi}{6}$
  - $\frac{\pi}{3}$
  - $\frac{\pi}{2}$

80. In a  $\Delta ABC$ ,  $2s =$  perimeter and  $R$  circumradius. Then  $s/R$  is equal to-

  - $\sin A + \sin B + \sin C$
  - $\cos A + \cos B + \cos C$
  - $\sin \frac{A}{2} + \sin \frac{B}{2} + \sin \frac{C}{2}$
  - none of these

81. If  $R$  denotes circumradius then in a  $\Delta ABC$ ,  $\frac{b^2 - c^2}{2aR}$  is equal to-

  - $\cos(B - C)$
  - $\sin(B - C)$
  - $\cos B - \cos C$
  - none of these

82. The ratio of the circumradius and inradius of an equilateral triangle is-

  - $3 : 1$
  - $1 : 2$
  - $2 : \sqrt{3}$
  - $2 : 1$

83. In an equilateral triangle, the in radius, circum-radius and one of the ex-radii are in the ratio-

  - $2 : 3 : 5$
  - $1 : 2 : 3$
  - $3 : 7 : 9$
  - $3 : 7 : 9$

84. If the exradii of a triangle are in HP the corresponding sides are in-

  - A.P.
  - G.P.
  - H.P.
  - none of these

85. In triangle ABC, if  $\frac{\cos A}{a} = \frac{\cos B}{b} = \frac{\cos C}{c}$  and  $a = 2$ , then area of this triangle is-

  - 1
  - 2
  - $\sqrt{3}/2$
  - $\sqrt{3}$

86. In triangle ABC, if  $b = 3$ ,  $c = 4$  and  $\angle B = \pi/3$ , then number of such triangles is-

  - 1
  - 2
  - 0
  - infinte

87. Radius of the incircle of the triangle with side 18, 24, 30 cms is-

  - 2
  - 4
  - 6
  - 9

88. In triangle ABC, with general notions  $r_1 + r_2 + r_3 - r$  is equal to

  - $4R$
  - $\Delta^2$
  - $\Delta$
  - $2R$

89. In triangle ABC,  $\cos A + \cos B + \cos C$  is equal to-

  - $1 + R/r$
  - $1 + r/R$
  - $1 - R/r$
  - $1 - r/R$

90. In triangle ABC if  $a, b, c$  are in AP, then  $\tan \frac{A}{2}, \tan \frac{B}{2}, \tan \frac{C}{2}$  will be in

  - A.P.
  - G.P.
  - H.P.
  - none of these