CLASS 12

## CONTINUITY AND DIFFERENTIABILITY

## MEAN VALUE THEOREM

## EXERCISE

| Q.1 | Function f should be on [a,b] according to Rolle's theorem                |  |  |  |  |
|-----|---|--|--|--|--|
|     | (a) continuous  | (b) non-continuous<br>(d) non-existent |  |  |  |
|     | (c) integral  |  |  |  |  |
| Q.2 | Function f is differential on (a,b) according to Rolle's theorem.         |  |  |  |  |
|     | (a) True  |  |  |  |  |
|     | (b) False   |  |  |  |  |
| Q.3 | What is the relation between f(a) and f(b) according to Rolle's theor     |  |  |  |  |
|     | (a) Equals to   | (b) Greater than                       |  |  |  |
|     | (c) Less than   | (d) Unequal                            |  |  |  |
| Q.4 | Does Rolle's theorem applicable if f(a) is not equal to f(b)?             |  |  |  |  |
|     | (a) Yes   | (b) No                                 |  |  |  |
|     | (c) Under particular conditions   | (d) May be                             |  |  |  |
| Q.5 | <b>Q.5</b> Another form of Rolle's theorem for the differential condition |  |  |  |  |
|     | (a) f is differentiable on (a,ah)   |  |  |  |  |
|     | (b) f is differentiable on (a,a-h)  |  |  |  |  |
|     | (c) f is differentiable on (a,a/h)  |  |  |  |  |
|     | (d) f is differentiable on (a,a+h)  |  |  |  |  |
| Q.6 | Another form of Rolle's theorem for the continuous condition is           |  |  |  |  |
|     | (a) f is continuous on [a,a-h]  |  |  |  |  |
|     | (b) f is continuous on [a,h]  |  |  |  |  |
|     |   |  |  |  |  |

- (c) f is continuous on [a,a+h]
- (d) f is continuous on [a,ah]
- **Q.7** What is the relation between f(a) and f(h) according to another form of Rolle's theorem?
  - a) f(a) < f(a+h)
  - b) f(a) = f(a+h)
  - c) f(a) = f(a-h)
  - d) f(a) > f(a+h)
- **Q.8** Function f is not continuous on [a,b] to satisfy Lagrange's mean value theorem.
  - (a) False
  - (b) True
- Q.9 What are/is the conditions to satify Lagrange's mean value theorem?
  - (a) f is continuous on [a,b]
  - (b) f is differentiable on (a,b)
  - (c) f is differentiable and continuous on (a,b)
  - (d) f is differentiable and non-continuous on (a,b)
- **Q.10** Function f is differentiable on [a,b] to satisfy Lagrange's mean value theorem.
  - (a) True
  - (b) False
- Q.11 Lagrange's mean value theorem is also called as \_\_\_\_\_
  - (a) Euclid's theorem
  - (b) Rolle's theorem
  - (c) a special case of Rolle's theorem
  - (d) the mean value theorem
- Q.12 Rolle's theorem is a special case of \_\_\_\_\_
  - (a) Euclid's theorem
  - (b) another form of Rolle's theorem

- (c) Lagrange's mean value theorem
- (d) Joule's theorem

**Q.13** Is Rolle's theorem applicable to  $f(x) = \tan x$  on  $\left[\frac{\pi}{4}, \frac{5\pi}{4}\right]$ ?

(a) Yes

(b) No

Q.14 What is the formula for Lagrange's theorem?

(a) 
$$f'(c) = \frac{f(a) + f(b)}{b - a}$$
  
(b)  $f'(c) = \frac{f(b) - f(a)}{b - a}$   
(c)  $f'(c) = \frac{f(a) + f(b)}{b + a}$   
(d)  $f'(c) = \frac{f(a) - f(b)}{b + a}$ 

**Q.15** Find 'C' using Lagranges's mean value theorem, if  $f(x) = e^x$ , a = 0, b = 1.

(a) 
$$e^{e^{-1}}$$
 (b)  $e^{-1}$ 

(c) 
$$\log_e^{e+1}$$
 (d)  $\log_e^{e-1}$ 

## **ANSWER KEY**

- **1.** (a)
- **2.** (a)
- **3.** (a)
- **4.** (b)
- 5. (d)
- **6.** (c)
- **7.** (b)

| CLASS 12 |     | MATHS |  |
|----------|-----|-------|--|
| 8.       | (a) |       |  |
| 9.       | (C) |       |  |
| 10.      | (a) |       |  |
| 11.      | (d) |       |  |
| 12.      | (C) |       |  |
| 13.      | (b) |       |  |
| 14.      | (b) |       |  |
| 15.      | (d) |       |  |