

INTRODUCTION TO TRIGONOMETRY

TRIGONOMETRIC RATIOS OF COMPLEMENTARY ANGLES

EXERCISE

Q.1 Without using trigonometric tables evaluate the following :

$$(i) \frac{\sin 20^\circ}{\cos 70^\circ} \quad (ii) \frac{\cos 19^\circ}{\sin 71^\circ} \quad (iii) \frac{\sin 21^\circ}{\cos 69^\circ}$$

$$(iv) \frac{\tan 10^\circ}{\cot 80^\circ} \quad (v) \frac{\sec 1^\circ}{\csc 7^\circ} \quad (vi) \frac{\sin 20^\circ 30'}{\cos 69^\circ 30'}$$

Q.2 Without using trigonometric tables evaluate the following :

$$(i) \left(\frac{\sin 49^\circ}{\cos 41^\circ} \right)^2 + \left(\frac{\cos 41^\circ}{\sin 49^\circ} \right)^2$$

$$(ii) \frac{\cot 40^\circ}{\tan 50^\circ} - \frac{1}{2} \left(\frac{\cot 35^\circ}{\sin 55^\circ} \right)$$

Q.3 Without using trigonometric tables evaluate the following :

$$(i) \frac{\tan 35^\circ}{\cot 55^\circ} + \frac{\cot 78^\circ}{\tan 12^\circ} - 1$$

$$(ii) \operatorname{cosec}^2 67^\circ - \tan^2 23^\circ$$

Q.4 Without using trigonometric tables evaluate the following :

$$(i) \sin^2 20^\circ + \sin^2 70^\circ - \tan^2 45^\circ$$

$$(ii) \sec 50^\circ \sin 40^\circ + \cos 40^\circ \operatorname{cosec} 50^\circ$$

Q.5 Without using trigonometric tables prove the following :

$$(i) \quad \tan 20^\circ \tan 35^\circ \tan 45^\circ \tan 55^\circ \tan 70^\circ = 1$$

$$(ii) \quad \sin 48^\circ \sec 42^\circ + \cos 48^\circ \operatorname{cosec} 42^\circ = 2$$

$$(iii) \quad \sin 63^\circ \cos 27^\circ + \cos 63^\circ \sin 27^\circ = 1$$

$$(iv) \quad \frac{\sin 70^\circ}{\cos 20^\circ} + \frac{\operatorname{cosec} 20^\circ}{\sec 70^\circ} - \cos 70^\circ \operatorname{cosec} 20^\circ = 1$$

$$(v) \quad \frac{\cos 80^\circ}{\sin 10^\circ} + \cos 59^\circ \operatorname{cosec} 31^\circ = 2$$

Q.6 Prove the following :

$$(i) \quad \sin \theta \sin(90^\circ - \theta) - \cos \theta \cos(90^\circ - \theta) = 0$$

$$(ii) \quad \frac{\sin \theta \cos(90^\circ - \theta) \cos \theta}{\sin(90^\circ - \theta)} + \frac{\cos \theta \sin(90^\circ - \theta) \sin \theta}{\sin(90^\circ - \theta)} = 1$$

$$(iii) \quad \frac{\sin \theta}{\sin(90^\circ - \theta)} + \frac{\cos \theta}{\cos(90^\circ - \theta)} = \sec \theta \operatorname{cosec} \theta$$

$$(iv) \quad \sin(90^\circ - \theta) \cos(90^\circ - \theta) = \frac{\tan \theta}{1 + \cot^2(90^\circ - \theta)}$$

$$(v) \quad \frac{\cos(90^\circ - \theta)}{1 + \sin(90^\circ - \theta)} + \frac{1 + \sin(90^\circ - \theta)}{\cos(90^\circ - \theta)} = 2 \operatorname{cosec} \theta$$

$$(vi) \quad \frac{1}{1 + \cos(90^\circ - \theta)} + \frac{1}{1 - \cos(90^\circ - \theta)} = 2 \operatorname{cosec}^2(90^\circ - \theta)$$

$$(vii) \quad \sin^2(90^\circ - \theta)(1 + \cot^2(90^\circ - \theta)) = 1$$

$$(viii) \frac{\cos(90^\circ - \theta) \sec(90^\circ - \theta) \tan \theta}{\operatorname{cosec}(90^\circ - \theta) \sin(90^\circ - \theta) \cot(90^\circ - \theta)} + \frac{\tan(90^\circ - \theta)}{\cot \theta} = 2$$

$$(ix) \frac{\tan(90^\circ - A) \cot A}{\operatorname{cosec}^2 A} - \cos^2 A = 0$$

$$(x) \frac{\cos(90^\circ - A) \sin(90^\circ - A)}{\tan(90^\circ - A)} = \sin^2 A$$

Ex.7 Express each of the following in terms of trigonometric ratios of angles between 0° and 45° ;

$$(i) \operatorname{cosec} 69^\circ + \cot 69^\circ$$

$$(ii) \sin 81^\circ + \tan 81^\circ$$

$$(iii) \sin 72^\circ + \cot 72^\circ$$

Ex.8 If A, B, C are the interior angles of a triangle ABC, prove that $\tan \frac{B+C}{2} = \cot \frac{A}{2}$

Ex.9 If $\tan A = \cot B$, prove that $A + B = 90^\circ$.

Ex.10 Express $\sin 67^\circ + \cos 75^\circ$ in terms of trigonometric ratios of angles between 0° and 45° .

ANSWER KEY

1. (i) 1 (ii) 1 (iii) 1 (iv) 1 (v) 1 (vi) 1

2. (i) 2 (ii) $\frac{1}{2}$

3. (i) 1 (ii) 1

4. (i) 0 (ii) 2

7 (i) $\sec 21^\circ + \tan 21^\circ$

(ii) $\cos 9^\circ + \cot 9^\circ$

(iii) $\cos 18^\circ + \tan 18^\circ$

10 $\cos 23^\circ + \sin 15^\circ$.