

9.



$$1. \quad j = \frac{I}{A} = nev_d$$

$$\frac{4 I}{\pi d^2} = nev ...(i)$$
  $\frac{16 I}{\pi d^2} = nev' ...(ii)$ 

From equation (i) & (ii)  $\frac{4I}{16I} = \frac{v}{v'} \implies v' = 4v$ 

2.  $j \rightarrow Current density \quad n \rightarrow Charge density$ 

$$j = -nev_{d} \qquad v_{d_{1}} = \frac{j}{n_{1}e}$$
$$v_{d_{2}} = \frac{j}{n_{2}e}, \ \frac{n_{1}}{n_{2}} = \frac{1}{4} \Longrightarrow n_{2} = 4n_{1}$$
$$\frac{v_{d_{1}}}{v_{d_{2}}} = \frac{n_{2}}{n_{1}} = \frac{4n_{1}}{n_{1}} = 4:1$$

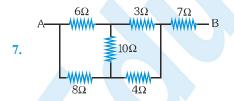
3. 
$$i = nev_d A; I = \frac{2envA}{4} - (-nevA) = \frac{3}{2}nevA$$

4. 
$$v_d = \frac{1}{Ane}$$
 As  $A \uparrow$  so  $v_d \downarrow \Rightarrow v_p > v_q$ 

- 5.  $R = \frac{\rho L}{A} \frac{L}{L} = \frac{\rho L^2}{V} \implies R \propto L^2$
- 6.  $R = \frac{\rho L}{A} \frac{L}{L} = \frac{\rho L^2}{AL} = \frac{\rho L^2}{V} = \frac{\rho L^2 d}{m}$

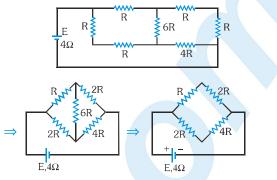
 $d, \rho \rightarrow$  same for all as the material is same for all.

$$\Rightarrow R_1: R_2: R_3 = \frac{25}{1}: \frac{9}{3}: \frac{1}{5} = 125: 15: 1$$



Balanced Wheatstone Bridge

As 
$$\frac{1}{9} + \frac{1}{12} = \frac{7}{36} = \frac{36}{7}$$
 So  $R_{AB} = \frac{36}{7} + 7 = \frac{85\Omega}{7}$ 



This is balanced wheat stone bridge From maximum power transfer theorem Internal resistance = External resistance

$$\Rightarrow 4 = \frac{3R \times 6R}{3R + 6R} \Rightarrow 4 = 2R \Rightarrow R = 2\Omega$$

$$V = IR \implies 2 = (I)(20) \implies I = \frac{1}{10}A$$

**10.** 
$$P = I^2 R = \left(\frac{V}{R}\right)^2 R = \frac{\varepsilon^2}{(R+r)^2} R$$

 $\varepsilon$  is constant and (R+ r) increases rapidly Then P $\downarrow$ 

11. 
$$P = \frac{V^2}{R}$$
 Initially,  $I = \frac{V}{2R}$   
Power across  $P_x = P_y = \left(\frac{\epsilon^2}{4R}\right)R$ 

Finally, I =  $\frac{2V}{3R}$ , Power P<sub>X</sub> =  $\frac{4V^2}{9R}$ , P<sub>y</sub> = P<sub>z</sub> =  $\frac{2V^2}{9R}$ 

Hence  $P_x$  increases,  $P_y$  decreases. Alternative method :

Brightness  $\propto i^2 R$  when S is closed current drawn from battery increases because  $R_{eq}$  decreases. i.e. current in X increases. So brightness of X increases and current in Y decreases. So brightness of Y decreases.

12. 
$$R_1 = \frac{\rho l}{A_1}$$
,  $R_2 = \frac{\rho l}{A_2}$  As  $A_1 < A_2$  So  $R_1 > R_2$   
In series  $H = I^2 Rt$   $H \propto R$ ;  $H_1 > H_2$   
In parallel  $H = \frac{V^2}{R}t$   $H \propto \frac{1}{R}$ ;  $H_1 < H_2$ 



# CURRENT ELECTRICITY

...**(i)** 

...(ii)

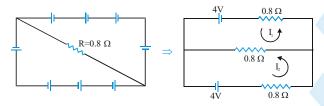
13. 
$$P = i^2 R \implies 10 = i^2 5 \implies i^2 = \frac{10}{5} = 2 \implies i = \sqrt{2}$$
  
 $i_4 = \frac{i_5}{2} \implies P_4 = \left(\frac{i}{2}\right)^2 4$ ,  $P_5 = (i^2)5$   
 $\frac{P_4}{P_5} = \frac{1}{5} \implies P_4 = \frac{P_5}{5}$ ,  $P_4 = \frac{10}{5} = 2$  cal/s

14. 
$$V = \varepsilon + i(r) \Rightarrow 12.5 = \varepsilon + \frac{1}{2}(1) \Rightarrow \varepsilon = 12 V$$

(As the battery is a storage battery it is getting charged)

- 15.  $V = IR \Rightarrow 0.2 = I(20)$   $I_g = 0.01A$  (through the galvanometer)  $I_g G = (i - i_g)S \Rightarrow (0.01)(20) = (10 - 0.01)S$  $\Rightarrow S = 0.020 \Omega$
- **16.** The correct answer is R = 0

#### 17.



1.6  $I_1 - 0.8 I_2 = 4 ...(i)$ 1.6  $I_2 - 0.8 I_1 = 4 ...(ii)$ from eq.  $I_1 = I_2 = 5$ voltage difference across any of the battery.

$$V_{a} = \begin{bmatrix} 0.2 \ \Omega & I \\ 1V \\ V_{a} - 1 + 0.2 \times 5 - V_{b} = 0 \\ V_{a} - V_{b} = 0 \text{ Volt} \end{bmatrix} V_{b}$$

18. 
$$R_v = \frac{V}{i_g} - G \implies 910 = \frac{V}{10 \times 10^{-3}} - 90$$

$$\Rightarrow$$
 V = 10  $\Rightarrow$  No. of divisions =  $\frac{10}{0.1} = 100$ 

**19.** I =  $\frac{12}{4+2+\infty}$  = 0. If i=0,

potential difference is equal of EMF of cell. = 12V

20. 
$$20 + R = \frac{12}{0.1} \Rightarrow R = 100\Omega$$
  
21.  $E = \left(\frac{V}{1}\right) \times \frac{1}{3}$  &  $E = \left(\frac{V}{31/2}\right)(1') \Rightarrow 1' = \frac{1}{2}$ 

22. 
$$\frac{P}{S} = \frac{Q}{625} \implies \frac{P}{Q} = \frac{S}{625}$$
$$\frac{Q}{S} = \frac{P}{676} \implies \frac{P}{Q} = \frac{676}{S}$$
From (i) & (ii)  $\frac{676}{S} = \frac{S}{625}$ 

$$(676)(625) = S^2 \implies S = 650\Omega$$

23. Potential gradient

I.

$$\mathbf{x} = \left(\frac{12}{8+16}\right) \times 4 = 2 \,\mathrm{Vm}^{-1}$$

Effective emf of  $E_1$  and  $E_2$ 

$$E = E = \frac{\frac{E_2}{r_2} - \frac{E_2}{r_1}}{1 / r_1 + 1 / r_2} = \frac{1}{2} \text{ volt}$$

Balancing length AN = 
$$\left(\frac{1}{2}\right)\left(\frac{1}{2}\right) = \frac{1}{4}$$
 m = 25 cm

24. Potential gradient

x = 
$$\left(\frac{5}{0.5 + 4.5}\right)\left(\frac{4.5}{3}\right) = 1.5$$
 Vm<sup>-1</sup>  
Here (x) (AC)=3 ⇒ AC =  $\frac{3}{1.5} = 2$  m

25. Potential gradient  $x = \left(\frac{E}{10r}\right) \left(\frac{9r}{L}\right)$ According to question

$$\frac{E}{2} = \left(\frac{E}{10r}\right) \left(\frac{9r}{L}\right) (1) \implies 1 = \frac{5L}{9}$$

26. (25W-220V)

$$P_1 = \frac{V_1^2}{R_1}$$
,  $R_1 = \frac{(220)^2}{25} = 1936\Omega$ 

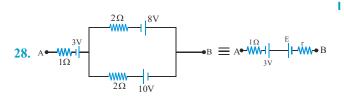
$$(100W-220V)$$

$$P_2 = \frac{V_2^2}{R_2}, R_2 = \frac{(220)^2}{100} = 484 \,\Omega$$

In Series (I same) H=I<sup>2</sup>Rt, H  $\propto$  R so if R<sub>1</sub>>R<sub>2</sub> then H<sub>1</sub> > H<sub>2</sub> R<sub>1</sub> is likely to fuse

27. 
$$P = \frac{V^2}{R} = \frac{V^2 A}{\rho l} \alpha \frac{r^2}{l} [V \rightarrow same]$$





$$E = \frac{\frac{E_1}{r_1} + \frac{E_2}{r_2}}{\frac{1}{r_1} + \frac{1}{r_2}} = \frac{\frac{10}{2} + \frac{(-8)}{2}}{\frac{1}{2} + \frac{1}{2}} = 1 \text{ volt and}$$

$$r = \frac{r_1 r_2}{r_1 + r_2} = 1\Omega$$
. Therefore  $A = 2\Omega$   $_{2V} = B$ 

**29.** 
$$P \Rightarrow \frac{V^2}{R} \Rightarrow \frac{V^2 A}{L\rho}$$
 ...(i)

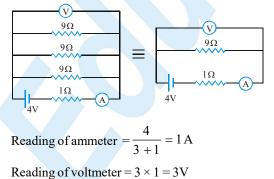
$$P' = \frac{V^2 A}{\left(L - \frac{L}{10}\right)} \rho \implies \frac{10 V^2 A}{9 L \rho} \qquad \dots (ii)$$

from eq. (i) & (ii)  $P' = \frac{10}{9}P$ 

$$\frac{\Delta P}{P} \times 100 \implies \frac{\left(\frac{10}{9}P - P\right)}{P} \times 100$$

 $\Rightarrow \frac{1}{9} \times 100 \Rightarrow 11.11\%$ 

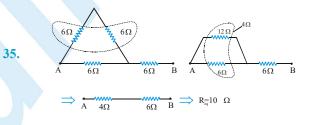
- **30.** In parallel combination the equivalent resistance is less than the two individual resistance connected and in series combination equivalent resistance is more than the two individual components.
- **31.** Given circuit can be reduced to

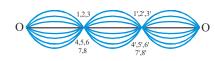


34. Total length of wire = 90 + 90 = 180 m; Total resistance of wire =  $180/5 = 12 \Omega$ .

As I = 
$$\frac{nE}{R+nr}$$
  $\Rightarrow$  0.25 =  $\frac{n \times 1.4}{12+5+n \times 2}$   $\Rightarrow$  n = 4.7

$$\Rightarrow$$
 Total number of cells required = 5





Points 1, 2, 3......8 are of same potential and 1', 2', 3'.....8' are of same potential.

$$R_{eq} = \frac{3R}{8}$$

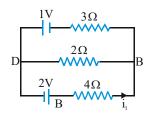
36.



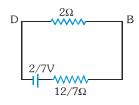
# CURRENT ELECTRICITY

# EXERCISE - 2 Part # I : Multiple Choice

1.  $E_{eq} = \frac{E_1 r_2 - E_2 r_1}{r_1 + r_2} = \frac{2 \times 3 - 1 \times 4}{3 + 4} = \frac{2}{7}$ 



$$r_{eq} = \frac{3 \times 4}{3 + 4} = \frac{12}{7}; i = \frac{2/7}{2 + \frac{12}{7}} = \frac{1}{13}A$$



$$V_{\rm B} > V_{\rm D} = 2\left(\frac{1}{13}\right); V_{\rm D} = V_{\rm B} = -\frac{2}{13}V_{\rm D}$$

From Figure 1:

$$V_{B} + 4i_{1} - 2 - V_{D} = 0; \frac{2}{13} - 2 + 4i = 0$$

$$i = \frac{6}{13} \text{ A}; V_{\text{G}} = 3 - 3 \times \frac{6}{13}$$
$$V_{\text{G}} = \frac{21}{13} \text{ V}, V_{\text{H}} = 1 + 1 \times \frac{6}{13} = V_{\text{H}} = \frac{19}{13}$$

2. 
$$_{28V}$$
  $\downarrow$   $_{4\Omega}$   $\stackrel{3\Omega}{=}$   $_{2\Omega}$   $\stackrel{3\Omega}{=}$   $_{4\Omega}$   $\stackrel{3\Omega}{=}$   $\stackrel{4\Omega}{=}$   $\stackrel{2}{=}$   $\stackrel{5\Omega}{=}$   $\stackrel{3\Omega}{=}$   $\stackrel{3\Omega}{=}$   $\stackrel{A}{=}$   $\stackrel{A}{=}$   $\stackrel{10\Omega}{=}$   $\stackrel{I}{=}$   $\stackrel{I=2A}{=}$   $\stackrel{V_{AB}}{=}$   $\stackrel{I=7 \text{ volt}}{=}$ 

3. Free–electron density and the total current passing through wire does not depend on 'n'.

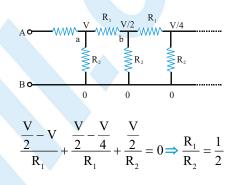
4.  $I = \frac{dq}{dt} = 2 - 16 t$ Power:  $P = I^2 R = (2 - 16t)^2 R$ 

L

Heat produced = 
$$\int P dt = \int_{1}^{\frac{1}{8}} (4 - 256t^2 - 64t) R dt$$

$$= \left[ \left( 4t - \frac{256t^3}{3} - \frac{64t^2}{2} \right) R \right]_{0}^{1/8} = \frac{R}{6} \text{ joules}$$

- 5. Both ' $4\Omega$ ' and ' $6\Omega$ ' resistors are short circuited therefore R<sub>eq</sub> of the circuit in  $2\Omega$  is 10 A. Power = VI = 200 watt Potential difference across both 'A' and 'B' = 0
- 6. It is the concept of potentiometer.
- 7. By applying node analysis at point b



- 8. For wheat stone Bridge condition is  $\frac{R_1}{R_2} = \frac{R_3}{R_4}$ Therefore null point is independent of the battery voltage.
- 9.  $\Delta V = E + ir$  and in charging current flows from positive terminal to negative terminal.
- 10.  $V = E ir \Rightarrow V = -ri + E$ Slope of graph 'V' and 'i' gives 'r' intercept of graph 'V'

and 'i' gives 
$$E \Longrightarrow \tan \theta = \frac{y}{y} = r$$
.

11. 
$$R_{AB} = \frac{11R}{18}$$

12. If n batteries are in series than the circuit can be made as

$$i = \frac{nE}{nr} \Rightarrow \frac{E}{r}$$
  $i.e.$  independent of n.



13. If n batteries are in parallel than the circuit can be made

as 
$$i = \frac{nE}{r}$$

i is directly proportional to n.

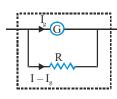
14. Slope of 'V' vs 'i' graph give internal resistance

 $\therefore r=5\Omega$ 

Intercept gives the value of e.m.f. E = 10 volt

Maximum current is  $i_{max} = \frac{E}{r} \implies 2A$ 

- 15. In parallel combination current gets divided therefore parallel combination supports  $i = i_1 + i_2$  is 20A in series current remain same therefore the series combination supports i = 10A.
- **16.** For Ammeter  $I_g G = (I I_g) R$

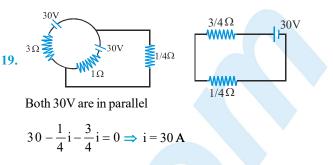


$$50 \times 10^{-6} \times 100 = 5 \times 10^{-3} \times (R) \Rightarrow R \cong 1\Omega$$
  
For voltmeter I<sub>g</sub>(R+G) = V  
$$\Rightarrow 50 \,\mu A \,(R+G) = 10V$$
$$\Rightarrow R + G = 200 \,k\Omega$$

- $\Rightarrow$  R  $\cong$  200k $\Omega$
- 17. As power in 2Ω is maximum when the current in it is maximum. Current in it will maximum when the value of R<sub>eq</sub> is minimum. ∴ R = 0 Heat =i<sup>2</sup>RT ⇒ (36)(2) = 72 W

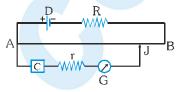
**18.** 
$$i_{min} = \frac{20}{R_{min}} = \frac{20}{200} = \frac{1}{10} A$$
  
 $i_{max} = \frac{20}{R_{max}} = \frac{20}{250} = \frac{2}{25} Amp$ 

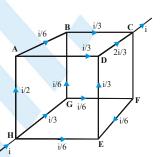
Potential =  $i_{min}R_{PM} = \frac{1}{10} \times 75 = 7.5 \text{ V}$ Across potentiometer V =  $i_{max}R_{PM} = \frac{2}{25} \times 75 = 6 \text{ V}$ 



20. If e.m.f of c is greater than the e.m.f. of the 'D'  $I_r = 0$ 

So r does not play any role of zero deflection in galvanometer.





So current in FC=0

21.

22. Assume  $DE \Rightarrow R_1\Omega$   $EC \Rightarrow R_2\Omega$   $R_1 + R_2 = 1\Omega$   $V_B = V_E$   $R_1 + R_2 = 1\Omega$   $R_2 + R_2 = 1\Omega$   $R_1 + R_2 = 1\Omega$   $R_2 + R_2 = 1\Omega$   $R_1 + R_2 = 1\Omega$   $R_2 + R_2 = 1\Omega$   $R_1 + R_2 = 1\Omega$   $R_2 + R_2 = 10$   $R_2 + R_2 = 10$  $R_2 + R_2 = 10$ 

10

Means balance wheat stone bridge

$$\frac{P}{Q} = \frac{R}{S}; \frac{1}{1} = \frac{\frac{R_{1} + 1}{R_{1} + 2}}{R_{2}}$$

$$R_{2} = \frac{R_{1} + 1}{R_{1} + 2} = 1 - R_{1}$$

$$R_{1} + 1 = R_{1} + 2 - R_{1}^{2} - 2R_{1}$$

$$R_{1}^{2} + 2R_{1} - 1 = 0 \Rightarrow R_{1} = -1 + \sqrt{2} \Rightarrow R_{2} = 2 - \sqrt{2}$$

$$\frac{CE}{ED} = \frac{R_{2}}{R_{1}} = \frac{2 - \sqrt{2}}{\sqrt{2} - 1} = \sqrt{2}$$

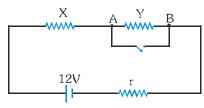


# CURRENT ELECTRICITY

23. 
$$\frac{E_1 + E_2}{r_1 + r_2 + R} < \frac{E_1}{r_1 + R}; (E_1 + E_2)(r_1 + R) < E_1(r_1 + r_2 + R)$$

 $E_1R + E_2R + E_1R < E_1r_2 + E_1R; R(E_1 + E_2) < E_1r_2$ On solving we get  $E_1r_2 > E_2(R + r_1)$ 

24.

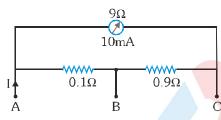


$$\frac{12}{X+Y+r} = 1 A \implies V_x = 1 = 1 \times X \implies X = 1\Omega$$

When Y shorted I =  $\frac{12}{1+r}$ 

$$10=12 - \mathrm{Ir} \Longrightarrow 10 = 12 - \frac{12}{(1+r)}\mathrm{r}$$
$$\Longrightarrow 10+10 \mathrm{r} = 12 + 12 - 12\mathrm{r} \Longrightarrow 10\mathrm{r} = 2 \Longrightarrow \mathrm{r} = 0.2 \Omega$$





Between A and B

- $(9+0.9) \times 10 \times 10^{-3} = (I-10mA) \times 0.1$
- $\Rightarrow$  990 mA = I 10mA
- $\Rightarrow$  I = 1000 mA = 1A
- 26. If all were in series all of them would have being getting discharged. But since, 2 are in opposite polarity, they will be getting charged.

V = E+iR getting charged  $i = \frac{V}{R} = \frac{(nE-4)}{nR}$ 

as (nE-4) as 4 batteries will be cancelled out

$$= \mathbf{E} + \left(\frac{\mathbf{n}\mathbf{E} - 4}{\mathbf{n}\mathbf{R}}\right)\mathbf{R}, = \mathbf{E} + \left(\mathbf{E} - \frac{4}{\mathbf{n}}\right) = 2\left(1 - \frac{2}{\mathbf{n}}\right)\mathbf{E}$$

27. 
$$V = \frac{V}{I} = \text{slope} \uparrow$$

$$P = I^{2}R$$

$$R = \frac{V}{I} = \text{slope} \uparrow$$

$$P = I^{2}R$$

$$R \uparrow P \uparrow$$

$$P \propto I^{2}$$

28. When  $S_2$  open Assume resistance of AB = RResistance of wire per unit length.

L

$$x = \frac{R}{L} \qquad I = \frac{E}{R}$$
Now in AC
$$\frac{E}{R} \times \frac{R}{L} \times \frac{L}{2} = 6$$

$$E = 12V$$
When S<sub>2</sub> closed
$$V_1 = \frac{E}{R} \times \frac{R}{L} \times \frac{5L}{12} = \frac{5E}{12} = \frac{5 \times 12}{12} = 5V$$

$$\Rightarrow 6 - I_1 r = 5 \Rightarrow 6 - \left(\frac{5}{10}\right)r = 5 \Rightarrow r = 2 \Omega$$

29. Rearranged circuit between A & B is :

$$A \xrightarrow{B} A \xrightarrow{B} A \xrightarrow{T} \Omega$$

(due to symmetry) Total resistance of circuit

$$=\frac{7}{3}+\frac{2}{3}=3\ \Omega \cdot i=\frac{9}{3}=3\ A$$

Heat produced in cell

$$= \mathrm{I}^2 \mathrm{r} = (3)^2 \times \left(\frac{2}{3}\right) = 6\mathrm{W}$$

Current in resistance connected directly between

A & B = 
$$\frac{7}{15} \times 3 = \frac{7}{5} = 1.4$$
 A  
=  $\frac{7}{15} \times 3 = \frac{7}{5} = 1.4$  A)



$$\Rightarrow I_1 R = 12 - 2 R, E - I_2 (4R) = 4R, I_1 + I_2 = 2$$
$$\Rightarrow E = 20R - 48$$

31.

$$2r \bigcirc 4r \bigcirc 4r$$

$$r_x = r + rx = r(1 + x) \Longrightarrow dR_x = \frac{\rho dx}{\pi r_x^2} = \frac{\rho dx}{\pi r^2 (1 + x)^2}$$

$$R_{1} = \int_{0}^{1} \frac{\rho dx}{\pi r_{x}^{2} (1+x)^{2}} = \frac{\rho}{\pi r^{2}} \left[ 1 - \frac{1}{1+1} \right],$$
$$R_{2} = \int_{1}^{1} \frac{\rho dx}{\pi r^{2} (1+x)^{2}} = \frac{\rho}{\pi r^{2}} \left[ \frac{1}{1+1} - \frac{1}{1+1} \right]$$

For null point

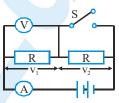
$$\frac{R_1}{R_2} = \frac{10}{10} \Longrightarrow R_1 = R_2$$
$$\implies 1 - \frac{1}{1+1} = \frac{1}{1+1} - \frac{1}{2} \Longrightarrow \frac{3}{2} = \frac{2}{1+1}$$
$$\implies 3+3 \bullet = 4 \Longrightarrow \bullet = \frac{1}{3} m$$

#### Part # II : Assertion & Reason

1. C 2. B 3. E 5. A 6. A 7. B 8. A 9. C 10. D

#### EXERCISE - 3 Part # I : Matrix Match Type

- 1.  $A \rightarrow P; B \rightarrow Q, S; C \rightarrow S; D \rightarrow P, R, S$
- 2.  $A \rightarrow Q; B \rightarrow P; C \rightarrow P; D \rightarrow Q$
- 3. After closing the switch net resistance decreases therefore there will be increases in the current. After closing the switch  $V_2$  becomes zero hence  $V = V_1$ .



- After short circuiting current in the resistance becomes zero therefore power become zero.
- 4. For potentiometer short circuit =  $x \bullet_1$ x Depends only on primary circuit
- x Depends only on primary circuit
- (A)  $E_1 \uparrow \Rightarrow x \uparrow \Rightarrow \bullet_1 \downarrow$  if secondary circuit remain same (B)  $R \uparrow \Rightarrow x \downarrow \Rightarrow \bullet_1 \uparrow$  if secondary circuit remain same
- (C) S.C $\uparrow = \bullet_1 \uparrow$  if x remain same

#### Part # II : Comprehension

Comprehension-1

Т

1. (A) 2. (D) 3. (D) Comprehension–2

1. (B) 2. (B) 3. (D)

**Comprehension-3** 

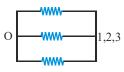
**1.** (C) **2.** (B)

#### **Comprehension**-4

1. As potential of 1, 2 and 3 are same potential difference across them 'zero'.



2. As 1, 2 and 3 are having same potential therefore we can draw it.



 $R_{01} = R/3$ ;  $R_{02} = R/3$ ;  $R_{03} = R/3$ 

3. As point 1,2,3 are equipotential  $\Delta V = I R_{12}$  $\Rightarrow \Delta V = 0$  therefore I = 0 for  $R_{12}, R_{23}, R_{31}$ 

#### **Comprehension-5**

- 1. Power through fuse
  - $\mathbf{P} = \mathbf{I}^2 \mathbf{R} = \mathbf{h} \times 2\pi \mathbf{r} \bullet$

h = heat energy lost per unit area per unit time I = current.

$$I^{2} = \frac{h \times 2\pi r l}{\frac{\rho l}{\pi r^{2}}} \propto r^{3} \implies I \propto r^{3/2}$$

$$\left(\frac{I_1}{I_2}\right) = \left(\frac{r_1}{r_2}\right)^{3/2} = \left(\frac{4}{1}\right)^{3/2} = \frac{8}{1}$$

2. 
$$P = VI$$
 20kw  $\Rightarrow$  2000  $= \frac{V^2}{20}$   
 $\Rightarrow V = 200 \text{ volt} \Rightarrow V < 200 \text{ volt}$ 

3. At maximum power delivery R = r, so  $\eta = 50\%$ 



# CURRENT ELECTRICITY

## **Comprehension-6**

- In balancing condition, current in the circuit should be 1. zero which happens at  $\bullet=20$  cm according to graph.
- At balance point  $\varepsilon = \frac{1}{100} V = \frac{20}{100} \times 6 = 1.2 V$ 2.
- 3. At  $\bullet$  = 0, applying kirchhoff's 2<sup>nd</sup> law in the circuit containing cell,  $\varepsilon = IR$

where I is the current at  $\bullet = 0, \& \varepsilon$  is the emf of the cell.

$$\Rightarrow R = \frac{\varepsilon}{I} = \frac{1.2}{40 \times 10^{-3}} = 30\Omega$$

#### **Comprehension**-7

- 1. Current is maximum when resistance in the circuit is minimum. i.e. when  $S_1, S_3, S_5$  are closed because then all
  - resistances will be short circuited  $I_{max} = \frac{V_0}{R}$ .
- 2. After regular closing of switches, total resistance decreases gradually.

**3.** 
$$P_1 = \frac{V_0^2}{R}$$
,  $P_2 = \frac{V_0^2}{\frac{37}{7}R}$  So  $\frac{P_1}{P_2} = \frac{7}{37}$ 

## **Comprehension-8**

1. 
$$I_1 = \frac{E_1 - E_2}{R_1}, I_1 + I_2 = \frac{E_2}{R_2} \Rightarrow I_2 = \frac{E_2}{R_2} - \frac{E_1 - E_2}{R_1}$$
  
 $E_2 = \frac{I_1 - I_2}{I_1 + I_2} \Rightarrow I_1 = \left(\frac{-1}{R_1}\right) E_2 + \frac{E_1}{R_1} & I_2 = \left(\frac{1}{R_1} + \frac{1}{R_2}\right) E_2 - \frac{E_1}{R_1}$   
 $\Rightarrow \frac{1}{R_1} = \frac{0.3}{6} \Rightarrow R_1 = 20\Omega$   
and  $\frac{1}{R_1} + \frac{1}{R_2} = \frac{0.3}{4} \Rightarrow R_2 = 40\Omega$   
Now as  $\frac{E_1}{R_1} = 0.3 \Rightarrow E_1 = 0.3 \times 20 = 6V$   
Comprehension-9  
1.  $V = E + ir$ 

- - = 12 + (0.04)(50) $= 12 + 2 \implies 14 \text{ V}$

 $=i^{2}r=(50)^{2}(.04)=100$  W

3. Total input - Loss in power = Useful power Input power = 14(50) = 700 w Loss in power = 100 w, Rate of conversion = 600 watt

1. 31 C, 
$$\frac{31}{3}$$
 A

2. 
$$\frac{1.5 \times 63.5 \times 10^{-3}}{1.6 \times 6 \times 9} = 1.1 \times 10^{-3} \,\mathrm{ms}^{-1}$$

(i) 
$$Q = 1200 C$$
 (ii)  $n = 75 \times 10^{20}$ 

Section (B)

4. (a) 
$$n = \frac{2}{1.6} \times 10^{17} = 1.25 \times 10^{17}$$
  
(b)  $\frac{1}{2\pi} \times 10^{6} \text{ A/m}^{2}$ .  
5. 10 A. 6. (i) 41°C (ii)  $\frac{1 n 2}{273}$  °C<sup>-1</sup>.  
7. T<sub>2</sub> 8. 0.2%

9. (i) 
$$R = \frac{0.35}{2} = 0.175 \Omega$$
 (ii)  $R = 7 \times 10^{-5} \Omega$ 

#### Section (C)

- **10.** (a) E = 10 V each
  - (b) (A) act as a source and (B) act as load (c)  $V_{A} = 9V, V_{B} = 11V$ (d)  $P_A = 9 W, P_B = 11 W$
  - (e) Heat rate = 1 W each
  - (f) 10 W each
  - (g) 9V, 11V
  - **(h)** –9W, 11 W



#### PART # I : AIEEE/JEE-MAIN

# PHYSICS FOR JEE MAIN & ADVANCED

**11.** 
$$\frac{125}{9}$$
 V

- 12. (a) all equal (b) b, then a and c equal(c) a, c equal, b
- **13.** (a) 7.5 V, (b) 24 mA (c) greater than 12 V.
- **14.** (a)  $\frac{50}{11} = 4.55 \text{ A}$  (b)  $\frac{22 \times 11}{5} = 48.4 \Omega$ (c) 1000 W (d) 240 cal s<sup>-1</sup> (e) 80/3 gm
- **15.**  $\frac{125}{4} = 31.25$  watt
- 16.  $P_A = 8 W \& P_B = 32 W$ , A is more likely to fail his examinations
- 17. (a)  $V_A = V_B = V_C = V_D = 0 V$ ,  $V_E = V_F = V_G = V_H = 10 V$ ,  $V_I = V_J = V_K = 15 V$ (b)  $V_I = 15 V$ ,  $V_2 = 5V$ ,  $V_3 = 15 V$ 
  - (c) each act as a source
  - (d)  $17.5 A(\uparrow), 15A(\downarrow) 2.5 A(\uparrow), 5A(\downarrow)$  from left to right in given circuit.
  - (e) 1  $\Omega$  resistance
  - (f) left most battery.

**18.** 
$$\frac{25}{9}$$
 V=2.78 V,  $\frac{5}{18}$  A=0.278 A

**19.** 19V

- **20.** (a) 10 Ω. (b) 3200 J
- 21. 5 A,74 V,49 V(+ve terminal is connected at point B)

#### Section (D)

**22.**  $R_f = 2\Omega$ .

- **23.** (a)  $R = 10 \Omega$  (b) 1A in each
  - (c)  $V_3 = 3V$ ,  $V_2 = 2V$ ,  $V_4 = 4V$  (d) 10 W (e) 1 W (f) 9W (g) 9V (h) 4  $\Omega$  resistance (i) 3 W.

24. (a) 
$$R = 3 \Omega$$
 (b)  $i = 2A$ ,  $i_1 = \frac{1}{2}A$ ,  $i_2 = 1A$ ,  $i_3 = \frac{1}{2}A$   
(c)  $V = 4V$  in each (d)  $12 W$  (e)  $4W$  (f)  $8 W$   
(g)  $4\Omega$  (h)  $4W$   
25. (a)  $3.7 V$  (b)  $3.7 V$ 

**26.** (i)  $R_{AB} = 5/6 \Omega$  (ii)  $R_{CD} = 1.5 \Omega$ (iii)  $R_{EF} = 1.5 \Omega$  (iv)  $R_{AF} = 5/6 \Omega$ (v)  $R_{AC} = 4/3 \Omega$ **27.** (ii) 1.5 A

**28.** (i) 
$$\frac{150}{7} = 21.43$$
 V, (ii)  $1600 \Omega$ 

29. CE: ED =  $\sqrt{2}$  : 1 30. 12.5  $\Omega$ , 170  $\Omega$ . 31. (a) 1 A (b) 2/3 A (c) 1/3 A 32. (a) 0.1 A (b) 0.3 A

Section (E)

**33.** (i) 
$$\frac{12}{8.59} = 1.4 \text{ A}$$
, (ii)  $\frac{12 \times 8.5}{8.59} = 11.9 \text{ V}$ 

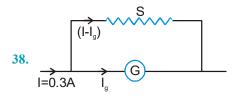
**34.** (i) 
$$\frac{1}{2} = 0.5 \,\mathrm{A}$$
 (ii)  $\frac{1}{12} = 0.0833 \,\mathrm{A}$ 

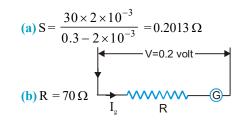
(iii) 
$$1.5 + \frac{1}{2} \times 0.4 = 1.7 \text{ V}$$
  
35.  $V_{\rm B} - V_{\rm A} = 21/5 = 4.2 \text{ V}, \text{ I} = 35/2 \text{ mA} = 17.5 \text{ mA}$   
(B to A)

**36.** zero in the upper 4  $\Omega$  resistor and 0.2 A in the rest two.

**37.** (a) 
$$\frac{1.2}{2.1} = 0.57$$
 (b) 1 (c)  $\frac{10.5}{6} = 1.75$ 

Section (F)

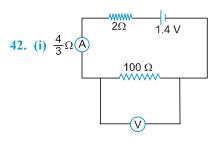




**39.** (a) 24 V, (b) 28 V  
**40.** 
$$V = \epsilon / (\eta + 1) = 2.0$$
 V.



**41.** 
$$\frac{20}{3}$$
V



(ii) 200 Ω

(iii) 
$$1.1 - \frac{4}{3} = -0.23 \text{ V}$$

**43.** 
$$\left(\frac{70}{60} - 1\right) \times 9.5 = \frac{9.5}{6}$$
 ohm

44. (a) 1.25 V, (b) saving of galvanometer from damage and to prevent the cell discharging fast

(c) No, (d) Yes, (e) No, (f) No

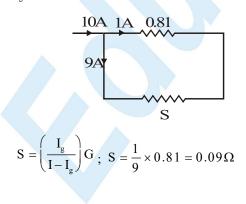
**45.** 
$$x = \frac{20}{7} \Omega$$
,  $Y = \frac{20}{3} \Omega$ 

# EXERCISE - 5 Part # I : AIEEE/JEE-MAIN

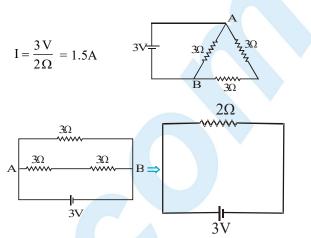
- 1. In order to convert an ammeter into a voltmeter, one has to connect a high resistance in series with it.
- The emf of the standard cell E ∞100
   The emf of the secondary cell e ∞30

$$\frac{E}{e} = \frac{100}{30} \implies e = \frac{30E}{100}$$

4.  $I_g = 1A; G = 0.81\Omega; I = 10A$ 



**5.** On redrawing the circuit between A and B we get

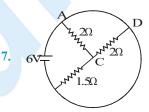


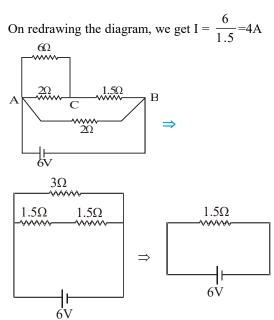
6. For a given volume, the resistance of the wire is expressed as

$$\mathbf{R} = \frac{\rho l^2}{\text{Volume}} \Longrightarrow \mathbf{R} \propto l^2$$

$$\frac{\mathbf{R}_2}{\mathbf{R}_1} = \left(\frac{21}{1}\right)^2 = 4 \implies \frac{\mathbf{R}_2 - \mathbf{R}_1}{\mathbf{R}_1} = 3$$

So, the change in resistance of wire will be 300%







# PHYSICS FOR JEE MAIN & ADVANCED

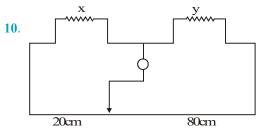
8. Let resistances be  $R_1$  and  $R_2$ 

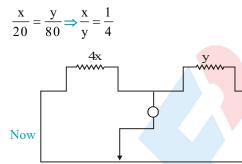
then S = R<sub>1</sub> + R<sub>2</sub> and P = 
$$\frac{R_1R_2}{R_1 + R_2}$$
  
n =  $\frac{S}{P} = \frac{(R_1 + R_2)^2}{R_1R_2} = \frac{R_1}{R_2} + \frac{R_1}{R_2} + 2$ 

$$= \left(\sqrt{\frac{R_1}{R_1}} - \sqrt{\frac{R_2}{R_1}}\right)^2 + 4 \implies n_{\min} = 4$$

9. Given that  $\frac{l_1}{l_2} = \frac{4}{3}$  &  $\frac{r_1}{r_2} = \frac{2}{3} \Rightarrow \frac{A_1}{A_2} = \frac{r_1^2}{r_2^2} = \frac{4}{9}$ In parallel :  $I_1R_2 = I_2R_2$ 

hence 
$$\frac{I_1}{I_2} = \frac{R_2}{R_1} = \frac{I_2}{A_2} \times \frac{A_1}{I_1} = \frac{3}{4} \times \frac{4}{9} = \frac{1}{3}$$

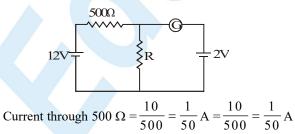




 $\frac{4x}{a} = \frac{y}{100 - a} \implies a = 50 \text{ cm}$ 

а

**12.** Voltage across R=2V Hence, voltage across 500Ω=10V

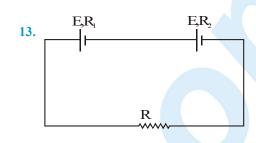


100-a

As 500 and R are in series value of

$$R = \frac{V_{R}}{I_{R}} = \frac{2}{1 / 50} = 100\Omega$$

I



Current in the circuit  $= \frac{2E}{R_1 + R_2 + R}$ 

potential difference across cell with R2 resistance

$$= \mathbf{E} - \mathbf{IR}_2 = \mathbf{E} - \frac{2\mathbf{E}}{\mathbf{R}_1 + \mathbf{R}_2 + \mathbf{R}} \times \mathbf{R}_2$$

But potential difference = 0

$$E = \frac{2E}{R_1 + R_2 + R} \times R_2 \Longrightarrow R = R_2 - R_1$$

14. Current supplied by the source to the external resistance

$$I = \frac{E}{R+r}$$

If r >>R;  $I = \frac{E}{r}$ 

which will be constant

15. The internal resistance of a cell

$$r = \left(\frac{e}{v_{T}} - 1\right)R = \left(\frac{l_{1}}{l_{2}} - 1\right)R = \left(\frac{240}{120} - 1\right)2 = 2\Omega$$

- **16**. Kirchoff's first law is based on law of conservation of charge.Kirchoff's second law is based on law of conservation of energy.
- 17. Specific resistance ( $\rho_B$ )=2 $\rho_A$ ; diameter  $d_B$ =2 $d_A$

$$\frac{1}{l_{A}} = ? \text{ for } \frac{(\text{Resistance})_{\text{B}}}{(\text{Resistance})_{\text{A}}} = 1$$
$$\frac{\rho_{\text{B}}l_{\text{B}}}{A_{\text{B}}} = \frac{\rho_{\text{A}}l_{\text{A}}}{A_{\text{A}}} - \frac{1}{l_{\text{B}}} = \frac{\rho_{\text{A}}}{\rho_{\text{B}}}\frac{A_{\text{B}}}{A_{\text{A}}}$$

$$\frac{l_{B}}{l_{A}} = \frac{\rho_{A}}{\rho_{B}} \frac{\left(dia_{B}\right)^{2}}{\left(dia_{A}\right)^{2}} = \frac{1}{2} \times 2^{2} = 2$$



**18.** Given that

 $\begin{aligned} R_{100^{\circ}C} &= 100\Omega \\ R_{T^{\circ}C} &= 200\Omega \\ T &=? \\ R_{100} &= R_0 [1 + \alpha (100)] & ...(i) \\ R_T &= R_0 [1 + \alpha T] & ...(ii) \\ On dividing eq. (ii) by eq. (i), we get \end{aligned}$ 

$$\frac{R_{\rm T}}{R_{\rm 100}} = \frac{1 + \alpha T}{1 + 100\alpha}$$

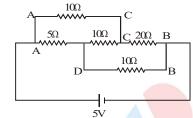
On solving, we get T=400°C

$$19. \underbrace{ \begin{array}{c} P_{r}r^{r} & \gamma_{r} \\ \gamma_{r} & S_{1} \\ Q_{1} \\ Q_{1} \\ Q_{1} \\ \gamma_{r} \\ r^{r} \\ r^{r} \\ S_{2} \\ r^{r} \\ s_{2} \\ r^{r} \\ s_{2} \\ s_{$$

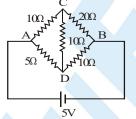
Under balanced condition

$$\frac{P}{Q} = \frac{R}{\frac{S_1 S_2}{S_1 + S_2}} \implies \frac{P}{Q} = \frac{R(S_1 + S_2)}{S_1 S_2}$$

20.



On redrawing the circuit, we get



It is a balanced Whetstone bridge having R<sub>eff</sub> as

$$R_{eff} = \frac{30 \times 15}{45} = 10\Omega$$

$$\Rightarrow \begin{bmatrix} 100 \\ 150 \\$$

$$I = \frac{V}{R} = \frac{5}{10} = 0.5 A$$

21. Let the resistance of the wire at 0°C is  $R_0$  also let the temperature coefficient of resistance is  $\alpha$ .

$$R_{50} = R_0 [1 + \alpha(50 - 0)] \qquad \dots (i)$$
  
Similarly  $R_{100} = R_0 [1 + \alpha(100 - 0)] \qquad \dots (ii)$ 

$$\frac{R_{100}}{R_{50}} = \frac{1+100\alpha}{1+50\alpha}; \ \frac{6}{5} = \frac{1+100\alpha}{1+50\alpha}$$

$$\Rightarrow$$
 6 + 300 $\alpha$  = 5 + 500 $\alpha$   $\Rightarrow$  1 = 200 $\alpha$ 

$$\alpha = \frac{1}{200} / \circ C$$

н

On replacing  $\alpha = \frac{1}{200}$  / °C in equation (i), we get

$$5 = R_0 \left[ 1 + \frac{1}{200} 50 \right] \Longrightarrow 5 = R_0 \left[ 1 + \frac{1}{4} \right]$$
$$\implies 5 = R_0 \left[ \frac{5}{4} \right] \implies R_0 = 4\Omega$$

22. 
$$\frac{55}{20} = \frac{R}{80} \implies R = \frac{55 \times 8}{2} = 220\Omega$$

24. Choosing A as origin,

$$E = \rho j = \rho \frac{I}{2\pi r^2}$$

- 25.  $V_{\rm C} V_{\rm B} = -\frac{\rho I}{2\pi} \int_{a}^{(a+b)} \frac{1}{r^2} dr = \frac{\rho I}{2\pi} \left[ \frac{1}{(a+b)} \frac{1}{a} \right]$  $V_{\rm B} - V_{\rm C} = -\frac{\rho I}{2\pi} \left[ \frac{1}{a} - \frac{1}{(a+b)} \right]$
- 27. For series combination

$$\alpha_{s} = \frac{\alpha_{1}R_{01} + \alpha_{2}R_{02}}{R_{01} + R_{02}}$$

$$R_{01} = R_{02} = R_{0} \text{ (given)}$$

$$\alpha_{s} = \frac{\alpha_{1} + \alpha_{2}}{2}$$
For parallel combination
$$\frac{1}{R} = \frac{1}{R_{1}} + \frac{1}{R_{2}}$$

$$1 \qquad 1$$

$$\frac{1}{R_{eq}} = \frac{1}{R_0(1+\alpha_1 t)} + \frac{1}{R_0(1+\alpha_2 t)}$$



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 $\Rightarrow$ 

$$\frac{1}{\frac{R_0}{2}(1+\alpha_p t)} = \frac{1}{R_0(1+\alpha_1 t)} + \frac{1}{R_0(1+\alpha_2 t)}$$

$$2 (1 + \alpha_{p}t)^{-1} = (1 + \alpha_{1}t)^{-1} + (1 + \alpha_{2}t)^{-1}$$

using binomial expansion

$$2 - 2\alpha_{p}t = 1 - \alpha_{1}t + 1 - \alpha_{2}t \Longrightarrow \alpha_{p} = \frac{\alpha_{1} + \alpha_{2}}{2}$$

**28.**  $R = \rho \frac{1}{A} \Rightarrow R \alpha \bullet^2$ 

$$\frac{\Delta R}{R} = \frac{\Delta R}{R} = \frac{2\Delta l}{l} = 2[0.1] = 0.2\%$$
 increase.

**29.** 
$$R = R_1 + R_2 + R_3 + R_4 \implies \Delta R = \frac{5}{100} \times 100 = 5\Omega$$

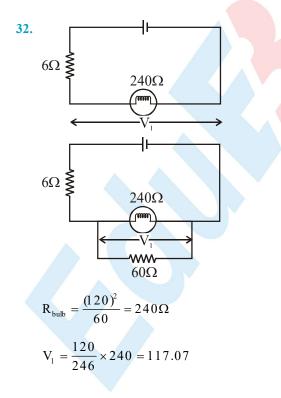
$$\Delta \mathbf{R} = \Delta \mathbf{R}_1 + \Delta \mathbf{R}_2 + \Delta \mathbf{R}_3 + \Delta \mathbf{R}_4 = 20$$

For combination  $\frac{\Delta R}{R} \times 100 = \frac{20}{400} \times 100 = 5\%$ 

**30.** 
$$i = 0.2 \text{ A}, \ \rho = 4 \times 10^{-7} \ \Omega\text{-m}, A = 8 \times 10^{-7} \ \text{m}^2$$

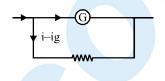
$$x = \frac{i\rho}{A} = \frac{0.02 \times 4 \times 10^{-7}}{8 \times 10^{-7}} = 0.1 \text{ V/m}$$

**31.** Due to greater heating as  $H = I^2 R$ 25W get fused.



$$R_{heater} = \frac{(120)^2}{240} = 60\Omega$$
  
V<sub>2</sub> =  $\frac{120}{54} \times 48 = 106.6$   
So change in voltage = V<sub>1</sub> - V<sub>2</sub> ≈ 10.4 Volt

**33**. To increase the range of ammeter, resistance should be decreased (So additional shunt connected in parallel) so total resistance to ammeter decreases.



**Single Choice** 

1

1. Net resistance of the circuit is  $9\Omega$ .

: current drawn from the battery,

$$i = \frac{9}{9} = 1A = current through 3\Omega resistor$$

$$9V \xrightarrow{3\Omega}_{1A} \xrightarrow{2\Omega}_{i_2} \xrightarrow{C}_{2\Omega}$$
$$8\Omega \xrightarrow{i_1}_{i_2} \xrightarrow{i_3}$$
$$4\Omega$$

Potential difference between A and B is

$$V_{A} - V_{B} = 9 - (3+2) = 4V = 8i_{1}$$
  
∴  $i_{1} = 0.5 \text{ A}$  ∴  $i_{2} = 1 - i_{1} = 0.5 \text{ A}$   
Similarly, potential difference between C and D  

$$V_{C} - V_{D} = (V_{A} - V_{B}) - i_{2}(2+2) = 4 - 4i_{2} = 4 - 4(0.5) = 2V = 8i_{3}$$
  
∴  $i_{3} = 0.25 \text{ A}$ 

Therefore, 
$$i_4 = i_2 - i_3 = 0.5 - 0.25$$
  
 $\Rightarrow i_4 = 0.25 A$ 

2. As there is no change in the reading of galvanometer with switch S open or closed. It implies that bridge is balanced. Current through S is zero and

$$\mathbf{I}_{\mathrm{R}} = \mathbf{I}_{\mathrm{G}}, \mathbf{I}_{\mathrm{P}} = \mathbf{I}_{\mathrm{Q}}.$$

3. Current I can be independent of  $R_6$  only when  $R_1$ ,  $R_2$ ,  $R_3$ ,  $R_4$  and  $R_6$  form a balanced wheatstone's bridge.

Therefore, 
$$\frac{R_1}{R_2} = \frac{R_3}{R_4} \implies R_1 R_4 = R_2 R_3$$



4. In the first case  $\frac{(3E)^2}{R} t = ms\Delta T$  ...(i)  $\left[H = \frac{V^2}{R}t\right]$ 

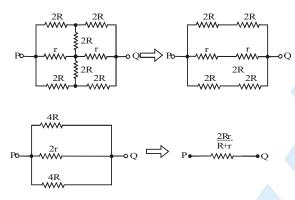
When length of the wire is doubled, resistance and mass both are doubled. Therefore, in the second case

$$\frac{(NE)^2}{2R}$$
.t=(2m)s\Delta T ....(ii)

Dividing eq. (ii) by (i), we get

$$\frac{N^2}{18} = 2 \Longrightarrow N^2 = 36 \Longrightarrow N = 6$$

5. The circuit can be redrawn as follows



6. 
$$P = \frac{V^2}{R}$$
 so,  $R = \frac{V^2}{P}$ 

: 
$$R_1 = \frac{V^2}{100} \& R_2 = R_3 = \frac{V^2}{60}$$

Now, 
$$W_1 = \frac{(250)^2}{(R_1 + R_2)^2} \cdot R_1$$

and 
$$W_2 = \frac{(250)^2}{(R_1 + R_2)^2} \cdot R_2$$
 and  $W_3 = \frac{(250)^2}{R_3}$ 

$$W_1: W_2: W_3 = 15:25:64 \implies W_1 < W_2 < W_3$$

- 7. Ammeter is always connected in series and voltmeter in parallel.
- 8. The ratio  $\frac{AC}{CB}$  will remain unchanged.

9. P=i<sup>2</sup>R Current is same, so P∝R.
In the first case it is 3r, in second case it is (2/3)r, in III

case it is 
$$\frac{r}{3}$$
 & in IV case the net resistance is  $\frac{3r}{2}$   
 $R_{III} < R_{II} < R_{IV} < R_{1}$   $\therefore$   $P_{III} < P_{II} < P_{IV} < P_{1}$   
10.  $R_{PQ} = \frac{5}{11}r$ ,  $R_{QR} = \frac{4}{11}r$  and  $R_{PR} = \frac{3}{11}r$   
 $\therefore$   $R_{PQ}$  is maximum

11. BC, CD and BA are known resistance. The unknown resistance is connected between A and D.

12. 
$$V_{ab} = i_g \cdot G = (i - i_g)S$$
  $\therefore i = \left(1 + \frac{G}{S}\right)i_g$ 

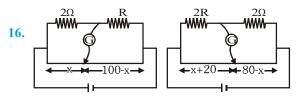
Substituting the values, we get i=100.1 mA

- 13. W=0. Therefore, from first law of thermodynamics,  $\Delta U = \Delta Q = i^2 Rt = (1)^2 (100) (5 \times 60) J = 30 \text{ kJ}$
- 14. Current in the respective loop will remain confined in the loop itself. Therefore, current through  $2\Omega$  resistance = 0. Current always flow in closed path.

**5.** 
$$H = I^2 Rt$$
  $I \rightarrow same$ 

So H 
$$\propto$$
 R =  $\frac{\rho l}{\pi r^2} \rho$ ,  $\bullet$  same.

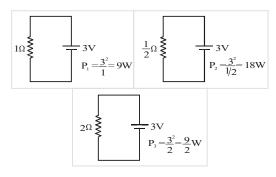
So H 
$$\propto$$
 R  $\propto \frac{1}{r^2}$  H<sub>BC</sub> = 4H<sub>AB</sub>





# **PHYSICS FOR JEE MAIN & ADVANCED**

- $R > 2\Omega \quad \therefore 100 x > x$ Applying  $\frac{P}{Q} = \frac{R}{S}$ We have  $\frac{2}{R} = \frac{x}{100 x}$ ...(i)  $\frac{R}{2} = \frac{x + 20}{80 x}$ ...(ii)
  Solving eq. (i) and (ii) we get  $R=3\Omega$
- 17. Given circuits can be reduced to



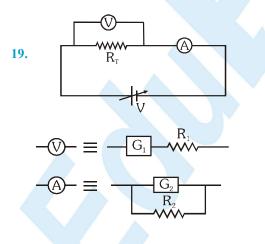
**18.** P = 
$$\frac{V^2}{R}$$
 and 100W > 60W > 40W

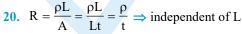
$$\Rightarrow \frac{V^2}{R_{100}} > \frac{V^2}{R_{60}} > \frac{V^2}{R_{40}} \Rightarrow \frac{1}{R_{100}} > \frac{1}{R_{60}} > \frac{1}{R_{40}}$$

[Note : Although 100 = 60 + 40 so at room tempeature

 $\frac{\mathbf{V}^2}{\mathbf{R}_{100}} = \frac{\mathbf{V}^2}{\mathbf{R}_{60}} + \frac{\mathbf{V}^2}{\mathbf{R}_{40}} \implies \frac{1}{\mathbf{R}_{100}} = \frac{1}{\mathbf{R}_{60}} + \frac{1}{\mathbf{R}_{40}}$ 

(Applicable Only at room temperature)]





#### I Multiple Choice

$$I = \frac{240}{32} \implies \frac{60}{8} = 7.5 \text{ mA}$$

- (A) Current I is 7.5 mA
- (B) Voltage drop across R<sub>L</sub> is 9 volt

(C) 
$$\frac{P_1}{P_2} = \frac{V_1^2}{R_1} \times \frac{R_2}{v_2^2} = \frac{225 \times 1.2}{2 \times 81} \implies 1.6$$

**(D)** After interchanging the two resistor  $R_1$  and  $R_2$ 

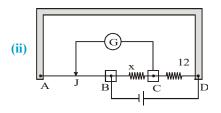
$$\Rightarrow \left\lfloor \frac{9}{3} \right\rfloor^2 = 9$$

**Assertion - Reason** 

1. Ans. D

#### **Subjective Problems**

 (i) There are no positive and negative terminals on the galvanometer because only zero deflection is needed.



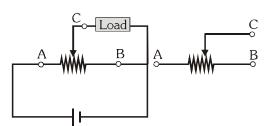


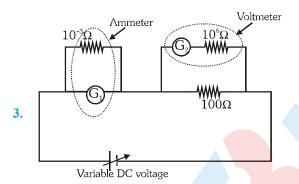
#### (iii) AJ = 60 cm $\therefore BJ = 40 \text{ cm}$

If no deflection is taking place. Then, the Wheatstone's bridge is said to be balanced,

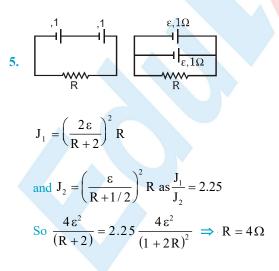
Hence, 
$$\frac{X}{12} = \frac{R_{BJ}}{R_{AJ}} \Rightarrow \frac{X}{12} = \frac{40}{60} = \frac{2}{3}$$
  
 $\Rightarrow x = 8\Omega$ 

2. The rheostat is as shown in figure. Battery should be connected between A and B and the load between C and B





4. Slide wire bridge is most sensitive when the resistance of all the four arms of bridge is same. Hence, B is the most accurate answer.



MOCK TEST

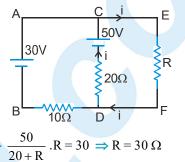
$$i = \frac{7 V}{7 \Omega} = 1 A.$$
  
Current flows in a:

Current flows in anticolockwise direction in the loop. Therefore  $0 - 1 \times 2 - 1 \times 2 - 5 = V_1$  $V_1 = -9 V.$ 

2.  $i = \frac{50}{20 + R}$ 

1.

Potential drop across 
$$R =$$
 Potential drop across AB



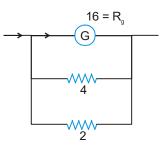
- 3.  $I_G = 10 \text{ mA} \Rightarrow G = 10\Omega$   $S(I-I_G) = I_G G$  where S is shunt is parallel  $S = 0.1\Omega$
- 4. Case I

$$R_{g} \times \frac{I}{5} = \left(I - \frac{I}{5}\right) \times 4 \implies R_{g} = 16 \Omega$$

Case II

$$16 I_1 = \frac{4 \times 2}{6} (I - I_1) \implies I_1 = I/13$$

S = 4

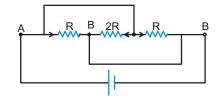


so decrease in current to previous current

$$=\frac{I/5-I/13}{I/5}=\frac{8}{13}$$
 Ans.

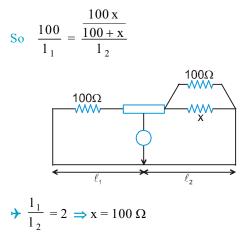


5. In figure all resistance are connected in parallel.



So  $R_{eq} = \frac{2R \times R/2}{2R + R/2}$  and current in all resistance flow from positive terminal of battery (means A end) to negative terminal of battery (means B end).

6.  $\Rightarrow$  wheat stone bridge is in balanced condition



- P
- 7. r = RPower maximum when r = R.

So, power consumed by it will decrease. for R > r.

- 8.  $V = E ir = -\frac{Er}{R+r} = E\left[\frac{R+r-r}{R+r}\right]$   $V = \frac{ER}{(R+r)} \implies V = 0 \text{ at } R = 0$   $V = E \text{ at } R = \infty$ So (B) is correct option.
- 9. Voltage across each bulb will be

$$V_1 = iR = \frac{V}{nR} \cdot R = (V/n)$$

so power developed by each bulb =

$$iV_1 = \frac{V}{nR} \cdot \frac{V}{n} = \frac{V^2}{n^2 R} \& P = \frac{V^2}{R}$$

So power consumed by one bulb =  $\frac{P}{n^2}$ 

10. For maximum current, net resistance of cells must be equal to  $2.5\Omega$ 

i.e. 
$$\frac{n (0.5)}{m} = 2.5$$
 .....(1)  
&  $m \times n = 45$  .....(2)  
solving we get  $n = 15$   $m = 3$ 

**11.** From the figure.

$$AC_1 = AC_2 = C_1C_2 = radius$$

 $\therefore \angle AC_1B = 120^{\circ}$ 

Hence the resistance of four sections are Hence equivalent resistance R across AB is

$$\frac{1}{R} = \frac{1}{24} + \frac{1}{12} + \frac{1}{12} + \frac{1}{24}$$
 or  $R = 4\Omega$ 

: Power = 
$$\frac{V^2}{R} = \frac{(20)^2}{4} = 100$$
 watt

**12.** In potentiometer wire potential difference is directly proportional to length

Let potential drop per unit length a potentiometer wire be K.

For zero deflection the current will flow independently in two closed circuits

$$IR = K \times 10 \qquad .... (1)$$
  

$$IR + IX = K \times 30 \qquad .... (2)$$

(2) - (1)  $\Rightarrow IX = k \times 20 \qquad \dots (3)$ Divide (1) & (3)

 $\frac{R}{x} = \frac{1}{2} \implies x = 2R$ 

13.  $E = \frac{\lambda}{2\pi\epsilon_0 r}$ ,

where  $\boldsymbol{\lambda}$  is the linear charge density on the inner cylinder.

and 
$$V = \int_{a}^{b} E.dl = \frac{\lambda}{2\pi\varepsilon_0} l n\left(\frac{b}{a}\right) \dots (1)$$



Now; 
$$I = \int_{J}^{r} \frac{du}{dA} = \sigma \int_{E}^{r} \frac{du}{dA} = \sigma \frac{\lambda}{2\pi\varepsilon_0 r} \cdot 2\pi r l$$

aa

b

Current per unti length will be :

$$I = \frac{\sigma\lambda}{\varepsilon_0} \qquad \dots (2)$$
  
From (1)  
$$I = \frac{2\sigma\pi\varepsilon_0}{\varepsilon_0 \ln(b/a)} V$$
$$= \frac{2\pi\sigma}{\ln(b/a)} V$$
  
Alternate

 $I_{b} = \frac{V}{R}$ 

1

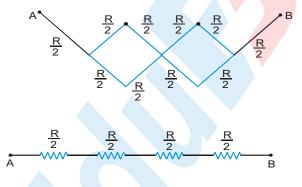
$$R = \int_{x=a}^{b} \frac{1}{\sigma} \frac{dx}{2\pi x \cdot l} = \frac{1}{2\pi\sigma} l n \left(\frac{b}{a}\right) \qquad \therefore \quad I = \frac{2\pi\sigma V}{l n (b/a)}$$

4. 
$$50 = 10 [R + r]$$
  
 $R + r = 5 \Omega$   
 $\eta = \frac{R}{R + r} \implies 0.25 = \frac{R}{R + r}$   
 $R + r = 4R$   
 $r = 3R$   
then  $R = \frac{5}{4} = 1.25 \Omega$ , and  $r = 3.75 \Omega$ .

**15.** 
$$P = VI$$
,  $50 = 5 \times I$   
 $I = 10 A$ 

Power lost in cable =  $I^2 R = 10 \times 10 \times 0.02 = 2 W$ Power supplied to T.R. = 50 W - 2 W = 48 W

16. The circuit can be folded about B and redrawn as



Hence equivalent resistance between A and B is 2R.

17.  $R = \frac{1}{\sigma} \times \frac{t}{4\pi r^2}$ Using values  $R = 5 \times 10^{-11} \Omega$ 

 $R = 5 \ge 10^{-11} \Omega$ 

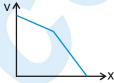
**18.** Since current  $I = neAv_d$  through both rods is same

$$2(n) e A v_L = n e (2A) v_R$$
 or  $\frac{v_L}{v_R} =$ 

**19.**  $i = \frac{dq}{dt}$  = slope of q - t graph

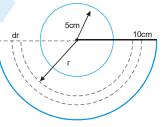
= -5 (which is constant) Amount of heat generated in time t H = i<sup>2</sup>RT H  $\propto$  t.

20. From relation  $E = \rho J$ , the magnitude of electric field is greater in right rod as compared to left rod. There fore magnitude of potential gradient in the right rod is greater. (remember potential is continuous).



Therefore the variation is shown by figure.

**21.** The arrangement is shown in figure. Consider the hemispherical shell of radius r and thickness dr as shown. Resistance of this shell is :



$$dR = \frac{dr}{\sigma \times 2\pi r^2}$$

$$R = \frac{1}{2\pi\sigma} \times \int_{r=5cm}^{r=10cm} \frac{dr}{r^2} = 1591.6\,\Omega$$

22. Redrawing the given circuit diagram as shown below: Using point potential theory,

$$\frac{V-E}{r} + \frac{V-E}{r} + \frac{V-E}{R} = 0$$

$$\Rightarrow (V-E)\left(\frac{2}{r} + \frac{1}{R}\right) = 0$$

$$F = 0$$

$$V = E$$

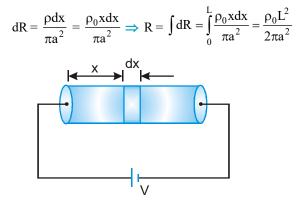
$$V = E$$

So, current through R,  $i = \frac{v - E}{R} = 0$ whatever be the value of R.



23. Consider an elemental part of solid at a distance x from left end of width dx.

Resistance of this elemental part is,



Current through cylinder is,  $I = \frac{V}{R} = \frac{V \times 2\pi a^2}{\rho_0 L^2}$ 

Potential drop across element is,  $dV = IdR = \frac{2V}{L^2} x dx$ 

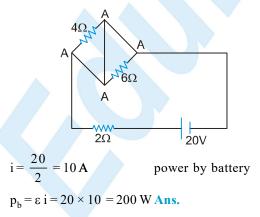
$$E(x) = \frac{dV}{dx} = \frac{2V}{L^2}x.$$

24. (A) p.d. across each cell =  $V_p - V_0$ 

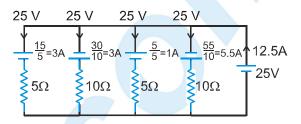
- (B) If i is clockwise then  $E_2$  is source and for anticlockwise current  $E_1$  is source.
- (C) P.D. = E ir (when battery supplies energy) = E + ir (when battery consumes energy).

By KVL 
$$i = \frac{E_1 - E_2}{r_1 + r_2}$$
 (Anticlockwise)  
 $V_p - V_Q = E_1 - i r_1 = \frac{E_1 r_2 + E_2 r_1}{r_1 + r_2}$ 

**25.** there is zero potential difference across 4  $\Omega$  and 6  $\Omega$  resistance.



26. The area of cross-section of conductor at point A is less than that at point B. So current density at A is higher. Hence, the electric field at A is more than at B and the thermal power generated at A is more than at B in an element of small same width. since resistance at A is greater



Power supplied by 20 V cell = (-1)(20) = -20 W as the cell is not supplying the power, it is eating the power (getting charged)

**28.** As the length is doubled, the cross section area of the wire becomes half. Thus the resistance of the

wire  $R = \rho \frac{L}{A}$  becomes four times the previous value.

Hence after the wire is elongated the current becomes one fourth. Electric field is potential difference per unit length and hence becomes half the initial value.

The power delivered to resistance is  $P = \frac{V^2}{R}$  and

hence becomes one fourth.

9. Total charge = 
$$\int Idt$$
 = Area under the curve  
= 10 C

Average current = 
$$\frac{\int Idt}{\int dt} = 5A$$

Total heat produced =  $\int I^2 R dt = \int_0^2 (-5t+10)^2 .1$ 

$$dt = \frac{200}{3}$$

Maximum Power =  $I^2 R$  when I is maximum current. = 100 x 1 = 100 W

**30.** Let a be the radius of left end side cross-section, then radius of cross-section at distance x from left end is a + bx where b is a constant.

From  $J = \sigma E \Rightarrow \frac{i}{A} = \sigma E \Rightarrow E = \frac{i}{A} \times \frac{1}{\sigma}$  as i and  $\sigma$  are same for all cross-section

$$E \propto \frac{1}{A} = \frac{1}{\pi (a+bx)^2}$$



...

Rate of heat generation per unit length,  $H = \frac{i^2 \rho}{A}$ ,

So 
$$H \propto \frac{1}{A} \implies \frac{H}{E} = \frac{i^2 \rho}{A} \times \frac{A}{i\rho} = i = \text{constant}$$

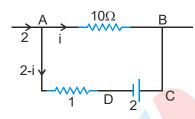
$$dV = -\vec{E} \cdot d\vec{x} \implies \int_{\mathcal{E}}^{V} dV = \int_{0}^{X} \frac{\rho \ i \ dx}{\pi (a+bx)^{2}}$$

$$\Rightarrow V = \epsilon + \frac{\rho i}{\pi b} \left[ \frac{1}{a + bx} - \frac{1}{a} \right] = \epsilon - \frac{\rho i}{\pi a b} \left( \frac{bx}{a + bx} \right).$$

31. Resistance absorbs energy at the rate of 2W. Potential difference across AB  $\Rightarrow$  V<sub>AB</sub>.I = 50 W V<sub>AB</sub>=50 V

Drop across resistor is 2V, therefore EMF of E is 48 V. As AB is absorbing energy at the rate of 50 W, 48 W is being absorbed by E. Thus E is on charging mode i.e. current is entering from +ve terminal of E.

32. Let the currents be as shown in the figure KVL along ABCDA



 $\Rightarrow -10 \text{ i} - 2 + (2 - i)1 = 0$ Potential difference across S =  $(2 - i)1 = 2 \times 1 = 2 \text{ V}$ .

- 33. Both statements 1 and 2 are true. In statement-1 R is varied while in statement-2 R is kept constant. Hence both statements are independent.
- 34. From relation  $\overset{1}{J} = \sigma \overset{1}{E}$ , the current density  $\overset{1}{J}$  at any point

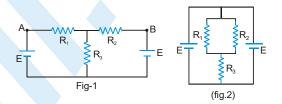
in ohmic resistor is in direction of electric field  $\dot{E}$  at that point. In space having non-uniform electric field, charges released from rest may not move along ELOF. Hence statement 1 is true while statement 2 is false.

35. As the length of wire is doubled, the cross-section area of wire becomes half. Therefore resistance of wire becomes four times and current becomes  $\frac{1}{4}$  th of the initial value.

also  $v_d = \frac{I}{neA}$ 

Since current becomes one fourth and cross-section area of wire becomes half, therefore from above equation the drift velocity of electron becomes half. Hence statement I is false.

- **36.** The potential difference across the resistance is always  $|E_1 E_2|$  in magnitude. Hence statement 1 and 2 are true and statement 2 is correct explanation of statement 1.
- 37. Just after switching ON the bulb, the filament of bulb is cold and its resistance is low. But after some time as filament gets hot, its resistance increases and hence withdraws less power from the source as compared to initial duration.
- 38. The points A and B are at same potential, then under given conditions points A and B on the circuit can be connected by a conducting wire. Hence the circuit can be redrawn as shown in figure 2.



Therefore statement 1 is true. Statement 2 is obviously false.

$$\mathbf{P}_{\mathrm{A}} = \frac{\mathbf{R} \cdot \mathbf{R}_{\mathrm{V}}}{\mathbf{R} + \mathbf{R}_{\mathrm{V}}} < \mathbf{R}$$

3

**40.**  $R_{B} = R + R_{G} > R$ 

**41.** % error in case A.

$$\frac{\mathbf{R}_{\mathrm{A}} - \mathbf{R}}{\mathbf{R}} \times 100 = \left(\frac{\mathbf{R}_{\mathrm{V}}}{\mathbf{R} + \mathbf{R}_{\mathrm{V}}} - 1\right) \times 100$$

$$= \frac{-R}{R+R_{\rm V}} \times 100 \approx -1\%$$

% error in case B

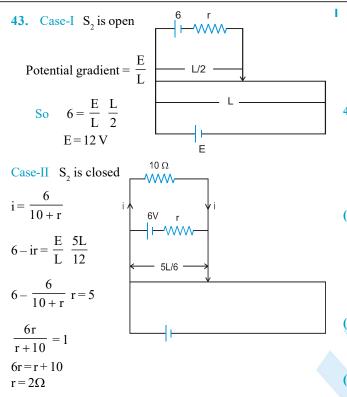
$$\frac{R_{\rm B} - R}{R} \times 100 = \frac{R_{\rm G}}{R} \times 100 \approx 10\%$$

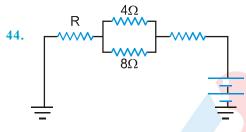
Hence percentage error in circuit B is more than that in A.

#### 42. (C)



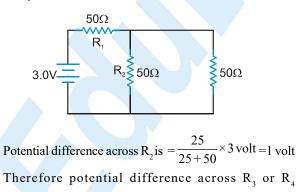
# **PHYSICS FOR JEE MAIN & ADVANCED**





Current in  $4\Omega$  resistance = 4ATotal current = 4 + 2 = 6A

**45.** The equivalent circuit can be redrawn as shown in figure 1. From figure 1 it is obivious that power dissipated by R<sub>1</sub> is maximum.



$$=\frac{20}{20+30} \times 1$$
 volt =0.4 volt

The equivalent resistance of circuit across the cell is 50+25=75 ohms

Therefore current drawn through cell is  $\frac{3}{3}$  1000 to  $\frac{1}{3}$ 

$$\frac{1000 \text{ mA}}{75}$$
 = 40 mA.

**48.** (A) Since current in both rods is same.

$$\mathbf{n}_1 \mathbf{e} \mathbf{v}_1 \mathbf{A}_1 = \mathbf{n}_2 \mathbf{e} \mathbf{v}_2 \mathbf{A}_2$$

$$\therefore \quad \frac{\mathbf{v}_1}{\mathbf{v}_2} = \frac{\mathbf{n}_2 \,\mathbf{A}_2}{\mathbf{n}_1 \,\mathbf{A}_1} = \frac{1}{2} \times \frac{2}{1} = 1$$

**B)** 
$$\Rightarrow$$
  $E = \rho J = \rho \frac{1}{A}$ 

$$\frac{E_1}{E_2} = \frac{\rho_1}{\rho_2} \times \frac{A_2}{A_1} = \frac{2}{1} \times \frac{2}{1} = 4$$

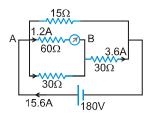
(C)  $\frac{\text{p.d. across rod I}}{\text{p.d. across rod II}} = \frac{\text{E}_1 \times \text{AB}}{\text{E}_2 \times \text{BC}} = 4$ 

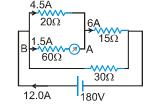
(D)  $\frac{\text{Average time taken by free electron to move from A to B}}{\text{Average time taken by free electron to move from B to C}}$ 

$$=\frac{AB}{v_1} \times \frac{v_2}{BC} = 1$$

**49.** When switch S is opened then right side resistance R which was short circuited earlier contributes to equivalent resistance. Hence, equivalent resistance across the battery increases, power dissipated by left resistance R decreases, voltmeter reading decreases and ammeter reading decreases.

**50.** When switch  $S_1$  is closed

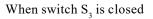


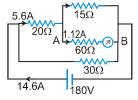


When switch  $S_2$  is closed

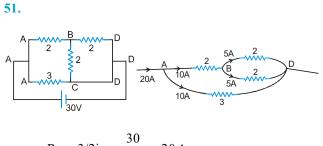
20Ω 3.6A 30Ω 12.6A 30Ω 12.6A 1.2A 60Ω 2.4A 30Ω 12.6A 1.80V

When switch S4 is closed



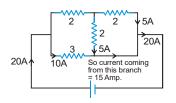




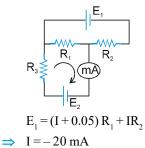


$$\Rightarrow R_{eq} = 3/2i = \frac{30}{3/2} = 20 \text{ Amp.}$$

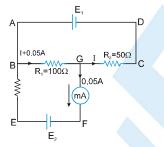
From figure current through  $B \rightarrow D$  branch = 5 Amp.



52. Applying KVL in loop ABCD

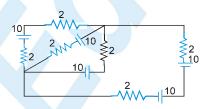


 $\therefore$  Current through R<sub>1</sub> = 30 mA towards right



Current through  $R_2 = 20$  mA towards left Applying KVL in loop BGFE  $E_2 = (I + 0.05) 100 + (0.05)20 = 4$  volts

**53.** The simplified circuit is.



We have to find I.



55.

Let potential of point 'P' be '0'. Potential at other points are shown in the figure apply kirchoff's current law at point x.

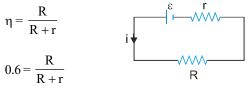
L

$$\frac{x-10}{4} + \frac{x-10}{2} + \frac{x-20}{4} + \frac{(x-10)-0}{2} = 0$$
  

$$\Rightarrow x - 10 + 2x - 20 + x - 20 + 2x - 20 = 0$$
  

$$\therefore 6x = 70 \Rightarrow x = \frac{35}{3} \text{ volt.}$$
  

$$10 \int_{0}^{10} \int_{0}^{4} \frac{x \text{ (assume)}}{10 \sqrt{10}} \int_{20}^{11} \int_{20}^{120 \sqrt{10}} \int_{20}^{4} \int_{20}^{4} \int_{20}^{120 \sqrt{10}} \int_{20}^{10} \int_{20}$$



# **PHYSICS FOR JEE MAIN & ADVANCED**

- $\Rightarrow$  3R+3r=5R or 2R=3r
- $\therefore$  new efficiency  $\eta = \frac{6R}{6R+r} = 0.9 = 90\%$  Ans.
- 56. V = Potential difference across the cell = Electric field × width of the cell
  - $= 8 \times 0.1 = 0.8$  volt ....Ans.

 $\epsilon = \text{emf of the cell} = 10 \times 0.1 = 1.0 \text{ volt } \dots \text{Ans.}$ 

Also r is the internal resistance and i is the current drawn from the cell

 $V = \varepsilon - ir \text{ or } 0.8 = 1 - 1r \implies r = 0.2 \Omega$  ....Ans.

**57.** (a) When Jockey is not connected.

Resistance per unit length

$$\lambda = \frac{12\,\mathrm{r}}{300} \,\,\Omega/\mathrm{cm}$$

 $\therefore$  Let  $\bullet$  be the length when we get zero deflection.

$$\therefore \left(\frac{E}{2}\right) = (\lambda \bullet) \Longrightarrow \frac{E}{2} = \frac{E}{13r} \times \frac{12r}{300} \times 1$$

 $\therefore = 157.5 \text{ cm}$ 

(b) Let potential at C is zero

Then apply Kirchoff's Ist law

$$\frac{x-0}{11r} + \frac{x-\frac{E}{2}-0}{2r} + \frac{(x-E-0)}{2r} = 0$$

$$\Rightarrow x = \frac{11E}{16}$$

$$x \xrightarrow{E} x \xrightarrow{E} r$$

$$I_{g} = \frac{x - \frac{E}{2}}{2r} = \frac{\left(\frac{11\epsilon}{16}\right) - \frac{E}{2}}{2r} = \frac{3E}{32r}$$

#### | Alternate method

●=300 cm : 
$$r'=(275) \times \frac{12 r}{300}$$
  
r'=11r  
Using KVL in loop (i)  
E-I<sub>1</sub>.11r-Ir-Ir=0 .....(i)  
and in loop (ii)

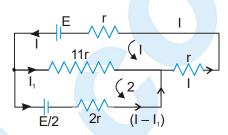
$$I_1 11r + (I - I_1)2r + \frac{L}{2} = 0$$
 .....

10

.(ii)

οA

οB



Solving equation (i) and (ii) we have

$$I_1 = \frac{E}{16 r}$$
 and  $I = \frac{5 E}{32 r}$ 

So current in galvanometer

Branch = 
$$(I - I_1) = \frac{5E}{32r} - \frac{E}{16r} = \frac{3E}{32r}$$

$$\Rightarrow I_g = \frac{3E}{32r}$$

(a) 157.5 cm (b) 
$$\frac{3E}{32r}$$

58.  $R = 100 \Omega$ ,  $\varepsilon = 3V$ In open circuit

$$i = \frac{3+3-3}{5 \times 200} \text{ So } V_{AB} = \varepsilon + ir$$

$$=3+\frac{3}{5\times200}\times400$$

 $V_{AB} = 4.2 V$  Ans. In short circuit

