

SURFACE AREAS AND VOLUMES

CYLINDER

Right circular cylinder

For a right circular cylinder of base radius r and height h , we have -

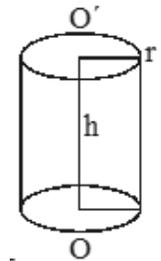
(i) Area of each end = area of base = πr^2

(ii) Curved surface area = $2\pi rh$

(iii) Total surface area = curved surface area + area of circular ends

$$= 2\pi rh + 2\pi r^2$$

$$= 2\pi r (r+h)$$



Right circular hollow cylinder

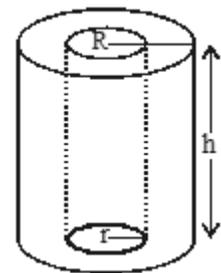
Let R and r be the external and internal radii of a hollow cylinder of height h , then

(i) Area of each end = $\pi (R^2 - r^2)$

(ii) Curved surface area of hollow cylinder

$$= \text{External surface area} + \text{Internal surface area}$$

$$= 2\pi Rh + 2\pi rh = 2\pi h (R + r)$$



(iii) Total surface area

$$= 2 pRh + 2 prh + 2 p(R^2 - r^2)$$

$$= 2 ph (R + r) + 2 p(R+r) (R-r)$$

$$= 2 p (R+r) (R+h-r)$$

(iv) Volume of material = External volume - Internal volume

$$= p R^2 h - p r^2 h$$

$$= p h (R^2 - r^2)$$