

# **Quadrilaterals**

# In the Chapter

- Sum of the angles of a quadrilateral is 360°.
- A diagonal of a parallelogram divides it into two congruent triangles.
- In a parallelogram,
  - (i) opposite sides are equal
  - (ii) opposite angles are equal
  - (iii) diagonals bisect each other
- A quadrilateral is a parallelogram, if
   (i) opposite sides are equal or
  - (i) opposite sides are equal or
  - (ii) opposite angles are equal or
  - (iii) diagonals bisect each other or
  - (iv) a pair of opposite sides is equal and parallel
- Diagonals of a rectangle bisect each other and are equal and vice-versa.
- Diagonals of a rhombus bisect each other at right angles and vice-versa.
- Diagonals of a square bisect each other at right angles and are equal, and vice-versa.
- The line-segment joining the mid-points of any two sides of a triangle is parallel to the third side and is half of it.
- A line through the mid-point of a side of a triangle parallel to another side bisects the third side.
- The quadrilateral formed by joining the mid-points of the sides of a quadrilateral, in order, is a parallelogram.
- Sides, angles and diagonals of a quadrilateral.
- Different types of quadrilatrals : Trapezium, parallelogram, rectangle, rhombus and square.
- A line drawn through the mid-point of a side of a triangle parallel to another side bisects the third side.

## • Types of Quadrilaterals

Look at the different quadrilaterals drawn below:



#### **Observe that :**

- One pair of opposite sides of quadrilateral ABCD in Fig. (i) namely, AB and CD are parallel. You know that it is called a *trapezium*.
- Both pairs of opposite sides of quadrilaterals given in Fig. (ii), (iii), (iv) and (v) are parallel. Recall that such quadrilaterals are called *parallelograms*. So, quadrilateral PQRS of Fig. 8.5 (ii) is a parallelogram. Similarly, all quadrilaterals given in Fig. (iii), (iv) and (v) are parallelograms.
- In parallelogram MNRS of Fig. 8.5 (iii), note that one of its angles namely ∠M is a right angle. What is this special parallelogram called? Try to recall.
   It is called a *rectangle*.
- The parallelogram DEFG of Fig. (iv) has all sides equal and we know that it is called a *rhombus*.
- The parallelogram ABCD of Fig. (v) has  $\angle A = 90^{\circ}$  and all sides equal; it is called a *square*.
- In quadrilateral ABCD of Fig. (vi), AD = CD and AB = CB i.e., two pairs of adjacent sides are equal. It is not a parallelogram. It is called a *kite*.

## Note that a square, rectangle and rhombus are all parallelograms.

- A square is a rectangle and also a rhombus.
- A parallelogram is a trapezium.
- A kite is not a parallelogram.
- A trapezium is not a parallelogram (as only one pair of opposite sides is parallel in a trapezium and we require both pairs to be parallel in a parallelogram).
- A rectangle or a rhombus is not a square.

# NCERT TEXT BOOK QUESTION (SOLVED)

# EXERCISE 8.1

Q.1. The angles of quadrilateral are in the ratio 3:5:9:13. Find all the angles of the quadrilateral.

## Ans. Let the angles be

2*x*, 5*x*, 9*x* and 13 *x* 

As the sum of the angles of a quadrilaterals is  $360^{\circ}$ ,

 $\therefore \quad 3x + 5x + 9x + 13x = \quad 360^{\circ}$ 

or 
$$30x = 360$$
  
or  $x = \frac{360}{30} = 12$   
 $\therefore 3x = 3 \times 12 = 36^{\circ}$   
 $5x = 5 \times 12 = 60^{\circ}$ 

$$9x = 9 \times 12 = 108^{\circ}$$
  
 $9x = 9 \times 12 = 108^{\circ}$   
 $13x = 13 \times 12 = 156^{\circ}$ 

Hence the angles of the quadrilateral are  $36^{\circ}$ ,  $60^{\circ}$ ,  $108^{\circ}$  and  $156^{\circ}$ .

Q.2. If the diagonals of a parallelogram are equal, then show that it is a rectangle.

**Ans. Given :** A parallelogram ABCD in which diagonal AC = diagonal BD.

To prove : ABCD is a rectangle.

**Proof** : In  $\triangle$ ABC and  $\triangle$ DCB.

$$AC = BD$$
 (given)



 $BC = CB \qquad (Common)$ AB = DC

(Opposite sides of a parallelogram) Therefore,

 $\begin{array}{rcl} \Delta ABC &\cong & \Delta DCB & (SSS Rule) \\ \angle ABC &= & \angle BCD & (CPCT) \end{array}$ 

But 
$$\angle ABC + \angle BCD = 180^{\circ}$$

So

[ Interior angles on the same side of transversal BC and AB  $\parallel$  CD]

$$2\angle ABC = 180^{\circ}$$
$$\angle ABC = 90^{\circ}$$

 $\angle ABC = 90$ 

Hence parallelogram ABCD is a rectangle.

Q.3. Show that if the diagonals of a quadrilateral bisect each other at right angles, then it is a rhombus.

**Ans. Given :** A quadrilateral ABCD in which diagonals AC and BD bisect each other at right angles at O.



**To prove :** Quad. ABCD is a rhombus. **Proof :** In  $\triangle AOD$  and  $\triangle AOB$ ,

OA = OA (common) OD = OB (given)  $\angle AOB = 90^{\circ}$  (given) ∠AOD = Therefore  $\triangle AOD =$  $\triangle AOB$  (SAS rule) AD =So AB (CPCT) Similarly, AB =BC = CD = DAHence, Quadrilateral ABCD is a rhombus.

Q.4. Show that the diagonals of a square are equal and bisect each other at right angles.

**Ans. Given :** ABCD is a square whose diagonals intersect each other at O.



**To prove :** (i) BD = AC(ii) OA = OC, OB = OD(iii)AC⊥BD **Proof**: (i) In  $\Delta$ DAB and  $\Delta$ CBA. AB =BA (Common) (Sides of a square) AD =BC ∠DAB =  $\angle CBA = 90^{\circ}$ [Angle of a square] Therefore  $\Delta DAB \cong \Delta CBA$  (SAS rule) BD = (CPCT) So, AC (ii) In  $\triangle AOB$  and  $\triangle COD$ ∠AOB = ∠COD (Vert. opp. angles) CD (Sides of a square) AB = $\angle OCD$  (Alternate angles) ∠OBA =  $\Delta AOB =$ *.*..  $\Delta COD$ (AAS rule) Hence OA = OC and OB = OD(CPCT) (iii) In  $\triangle AOD$  and  $\triangle COD$ OA =OC (Proved above) AD =(Sides of a square) CD OD =OD (Common) Therefore  $\triangle AOD \cong \triangle COD$  (SSS Rule) Thus  $\angle AOD = \angle COD$  (CPCT)

Also 
$$\angle AOD + \angle COD = 180^{\circ}$$
 (linear pair)  
or  $2\angle AOD = 180^{\circ}$   
or  $\angle AOD = 90^{\circ}$   
Hence AC  $\perp$  BD

Q.5. Show that if the diagonals of a quadrilateral are equal and bisect each other at right angles, then it is a square.



To Prove : ABCD is a square.

**Proof :** Since ABCD is a quadrilateral whose diagonals bisect each other, so it is parallelogram. Also, its diagonals bisect each other at right angles, therefore, ABCD is a rhombus.

 $\Rightarrow$ AB = BC = CD = DA[Sides of a rhombus] In  $\triangle ABC = \triangle BAD$ , we have AB =AB (Common) BC =AD (Sides of a rhombus] AC =BD (Given)  $\therefore \Delta ABC =$ ΔBAD (SSS congruence) ∠ABC = ∠BAD (CPCT) .:. But,  $\angle ABC + \angle BAD = 180^{\circ}$ [Consecutive interior angles]  $\angle ABC =$  $\angle BAD = 90^{\circ}$ ∠A =  $\angle B = \angle C = \angle D = 90^{\circ}$ [Opposite angles of a || gm]  $\Rightarrow$  ABCD is a rhombus whose angles are of 90°

each. Hence, ABCD is a square.

Q.6. Diagonal AC of a parallelogram ABCD bisects  $\angle A$  (see Fig. ). Show that



(i) it bisects ∠C also,
(ii) ABCD is a rhombus.
Ans. Given : A parallelogram ABCD, in which diagonal AC bisects ∠A, i.e., ∠DAC = ∠BAC.

**To Prove :** (i) Diagonal AC bisects  $\angle C$ 

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i.e.,  $\angle DCA = \angle BCA$ (ii) ABCD is a rhombus. Proof: (i) ∠DAC =  $\angle$ BCA [Alternate angles] ∠BAC = ∠DCA [Alternate angles] But,∠DAC = ∠BAC [given]  $\therefore \angle BCA = \angle DCA$ Hence, AC bisects ∠DCB Or, AC bisects  $\angle C$ Proved. (ii) In  $\triangle ABC$  and  $\triangle CDA$ AC =AC [Common] ∠BAC = ∠DAC [Given] ∠BCA = ∠DCA [Proved above] and  $\Delta ABC \cong$ [ASA congruence] ...  $\Delta ADC$ ... BC =DC [CPCT] But AB =DC [Given] AB =BC = DC = ADThus, Hence, ABCD is a rhombus

Q.7. ABCD is a rhombus. Show that diagonal AC bisects  $\angle A$  as well as  $\angle C$  and diagonal BD bisects  $\angle B$  as well as  $\angle D$ .

C

Ans. Given : A rhombus ABCD



To Prove : (i)  $\angle BAC = \angle CAD$ (ii)  $\angle BCA = \angle DCA$ (iii)  $\angle ABD = \angle CBD$ (iv)  $\angle COB = \angle ADB$ **Proof**: In ΔACD, AD =CD ZDAC = **ZDCA** ·•. (Opposite sides of a  $\Delta$ ) Now CD || AB ∠BCA (Alternate angles)  $\therefore$  ZDAC = Therefore  $\angle DCA = \angle BCA$ Hence AC bisects  $\angle C$ . Similarly we can prove AC bisects ∠A and BD

bisects both  $\angle B$  as well as  $\angle D$ .

Q.8. ABCD is a rectangle in which diagonal AC bisects ∠A as well as ∠C. Show that: (i) ABCD is a square

(ii) diagonal BD bisects  $\angle B$  as well as  $\angle D$ . Sol. Given : ABCD is a rectangle in which AC bisects ∠A as well as ∠C.
To prove : (i) ABCD is a square.
(ii) Diagonal BD bisects ∠B as well as ∠D.



[Sides opposite to equal angles] Hence ABCD is a rhombus and it is given that it is a square.

Hence ABCD is a square.

(ii) In a square, diagonals bisect the angles.

Hence BD bisects both  $\angle B$  and  $\angle D$ .

Q.9. In parallelogram ABCD, two points P and Q are taken on diagonal BD such that DP = BQ (see Fig.). Show that:

(i) 
$$\triangle APD \cong \triangle CQB$$
  
(ii)  $AP = CQ$   
(iii)  $\triangle AQB \cong \triangle CPD$   
(iv)  $AQ = CP$   
(v) APCQ is a parallelogram



**Ans. Given :** A parallelogram ABCD. There are two points P and Q on two diagonals BD such that DP=BQ.

To Proof: (i)  $\triangle APD \cong \triangle CQB$ (ii) AB = CQ(iii)  $\triangle AQB \cong \angle CPD$ (iv) AQ = CP

(v) APCQ is a parallelogram

**Proof**: (i) In  $\triangle$ APD and  $\triangle$ CQB, we have AD = BC [Opposite sides of a ||gm] DP =BO [given] ∠ADP = ∠CBQ [Alernate angles] **Δ**APD ≅  $\Delta CQB$  [By SAS Axiom] *.*.. AP =(CPCT) (ii) CO (iii) In  $\triangle$ AOB and  $\triangle$ CPD, AB =CD (Opposite sides of ||gm ABCD) AQ =CD (Opposite sides of ||gm AQCP) ∠CDP (Alternate angles) ZABO = Hence  $\triangle AOB =$ ΔСРО (SAS rule) (iv) AQ =CP (CPCT) (v) Now, AP = CQ (Proved above) AQ =CP (Proved above) and Since in APCQ opposite sides are equal,

therefore it is a parallelogram. Q.10. ABCD is a parallelogram and AP and CQ are perpendiculars from vertices A and C on diagonal BD (see Fig. ). Show that



(i)  $\triangle APB \cong \triangle CQD$ 

(ii) AP = CQ

**Ans.** Given : A parallelogam ABCD in which AP and CQ are perpendiculars from vertices A and C on diagonal BD respectively.

To prove : (i)  $\triangle APB \cong \triangle CQD$ AP = CO(ii) **Proof :** (i) In  $\triangle$ APB and  $\triangle$ CQD  $\angle COD = 90^{\circ}$ ∠APB = (Given) ∠ABP = ∠CDQ (Alternate angles) AB =CD (Opposite sides of a ||gm)  $\therefore \Delta APB =$ **∆**COD (AAS rule) (ii) Thus AP= CO (CPCT) Q.11. In  $\triangle ABC$  and  $\triangle DEF$ , AB = DE,  $AB \parallel DE$ ,

Q.11. In  $\triangle ABC$  and  $\triangle DEF$ , AB = DE,  $AB \parallel DE$ , BC = EF and BC  $\parallel$  EF. Vertices A, B and C are joined to vertices D, E and F respectively (see Fig.). Show that

(i) quadrilateral ABED is a parallelogram(ii) quadrilateral BEFC is a parallelogram

(iii) AD || CF and AD = CF
(iv) quadrilateral ACFD is a parallelogram
(v)AC = DF
(vi) ΔABC ≅ Δ DEF.



**Ans. Given :** In  $\triangle$ ABC and  $\triangle$ DEF, AB= DE, AB || DE, BC = EF and BC || EF. Vertices A, B and C are joined to vertices D, E and F.

To prove: (i) ABED is a parallelogram (ii) BEFC is a parallelogram (iii)  $AD \parallel CF and AD = CF$ (iv) ACFD is a parallelogram (v) AC = DF $(vi) \Delta ABC \cong \Delta DEF$ **Proof :** (i) In quadrilatral ABED, we have  $AB = DE and AB \parallel DE$  [Given] ABED is a parallelogram  $\Rightarrow$ [One pair of opposite sides is parallel and equal] (ii) In quadrilateral BEFC, we have  $BC = EF and BC \parallel EF$ [Given] BEFC is a parallelogram.  $\Rightarrow$ [One pair of opposite sides is parallel and equal] (iii) BE = CF and  $BE \parallel CF$ [BEFC is parallelogram] BE and AD  $\parallel$  BE AD =[ABED is a parallelogram] AD =CF and AD || CF  $\Rightarrow$ (iv) ACFD is a parallelogram. [One pair of opposite sides is parallel and equal] AC = DF(v) [Opposite sides of parallelogram ACFD] (vi) In  $\triangle$ ABC and  $\triangle$ DEF, we have AB =DE [Given] BC =EF [Given] AC =DF [Proved above] ∴ **∆**ABC ≅ **∆**DEF [SSS axiom] Q.12. ABCD is a trapezium in which AB || CD

and AD = BC (see Fig.). Show that

- (i)  $\angle A = \angle B$
- (ii)  $\angle C = \angle D$

(iii)  $\triangle ABC \cong \triangle BAD$ 

[*Hint* : Extend AB and draw a line through C parallel to DA intersecting AB produced at E.]



**Ans. Given :** ABCD is a trapezium in which AB  $\parallel$  CD and AD = BC.

- **To Prove :** (i)  $\angle A = \angle B$
- (ii)  $\angle C = \angle D$

(iii)  $\triangle ABC \cong \triangle BAD$ 

(iv) Diagonal AC = Diagonal BD

**Construction :** Extend AB and draw a line through C parallel to DA intersecting AB produced at E.

**Proof :** (i) In quad. ADCE,

$$AD \parallel CE (By construction)$$

AE || DC (Given)

So AD = EC and AD = BC

$$\therefore BC = EC$$
Therefore
$$\angle CBE = \angle BEC$$
[Angles opposite to equal sides of a  $\Delta$ ]
$$\angle A + \angle E = 180^{\circ}$$
(Interior angles on the same side of transversal
AE where  $AD \parallel EC$ )
and  $\angle E = \angle CBE$ 
Therefore
$$\angle A + \angle CBE = 180^{\circ}$$
But  $\angle ABC + \angle CBE = 180^{\circ}$ 
(linear pair)
So  $\angle A = \angle ABC = \angle B$ ,
Hence  $\angle A = \angle B$ 
(ii)  $\angle A = \angle BCD$  and  $\angle B = \angle D$ 

$$\therefore \angle BCD = \angle D$$
or  $\angle C = \angle D$  in trap  $ABCD$ 
(iii) In  $\triangle ABC$  and  $\triangle BAD$ 

$$BC = AD$$

$$(Given)$$

$$AB = BA$$

$$(Common)$$

$$\angle A = \angle B$$
Therefore
$$\triangle ABC \cong \triangle BAD$$
(SAS rule
(iv)  $\therefore$  Diagonal  $AC =$  Diagonal BD (CPCT)

# EXERCISE 8.2

Q.1. ABCD is a quadrilateral in which P, Q, R and S are mid-points of the sides AB, BC, CD and DA (see Fig). AC is a diagonal. Show that :

(i) SR || AC and SR = 
$$\frac{1}{2}$$
 AC

(ii) PQ = SR

(iii) PQRS is a parallelogram.



**Ans.** Given : ABCD is a quadrilateral in which P, Q, R and S are mid-points of AB, BC, CD and DA. AC is a diagonal.

**To prove :** (i) SR || AC and SR = 
$$\frac{1}{2}$$
 AC

(ii) PQ = SR

(iii) PQRS is a parallelogram

**Proof :** (i) In  $\triangle$ ABC, P is the mid-point of AB and Q is the mid-point of BC.

$$\therefore PQ \parallel AC \text{ and } PQ = \frac{1}{2} AC \qquad \dots(i)$$

[Mid-point theorem]

In  $\triangle$ ADC, R is the mid-point of CD and S is the mid-point of AD.

$$\therefore \quad SR \parallel AC \text{ and } SR = \frac{1}{2} AC \qquad \dots (ii)$$

[Mid-point theorem]

(ii) From (i) and (ii), we get

$$PQ \parallel SR$$
 and  $PQ = SR$ 

(iii) Now in quadrilateral PQRS, its one pair of opposite sides PQ and SR is equal and parallel.

: PQRS is a parallelogram.

Q.2. ABCD is a rhombus and P, Q, R and S are the mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rectangle.



Ans. Given : ABCD is a rhombus and P, Q, R and S are the mid-points of the sides AB, BC, CD and DA respectively.

To Prove : Quadrilateral PQRS is a rectangle. Construction: Join A and C.

**Proof**: In  $\triangle$ ABC, P is the mid-point of AB and Q is the mid-point of BC.

$$\therefore PQ = \frac{1}{2}AC$$

 $PQ \parallel AC$ and

(Mid-point Theorem)

... (i)

Similarly, 
$$SR = \frac{1}{2} AC \text{ and } SR \parallel AC \dots$$
...(ii)

(Mid-point Theorem)

PQ =SR and ... PO || SR. So, PQRS is a parallelogram. SP || Also. DB and RQ || BD And AC  $\perp$ BD [Diagonals of a rhombus bisect each other at right angle] BD || SP ON || MP  $\Rightarrow$ and AC || PQ PN OM ||  $\Rightarrow$ MONP is a ||gm *.*•. ∠MON =  $\angle MPN = 90^{\circ}$  $\Rightarrow$ [opposite angles of a ||gm]

So, PQ ⊥ PS

Hence PQRS is a rectangle.

Q.3. ABCD is a rectangle and P, Q, R and S are mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rhombus.

Ans. Given : ABCD is a rectangle and P, Q, R and S are mid-points of AB, BC, CD and DA respectively.

To prove : PQRS is a rhombus.

Construction : Join AC and BD.

**Proof** : In  $\triangle$ ABC, P is the mid-point of AB and Q



$$\therefore \qquad PQ = \frac{1}{2}AC$$
  
d 
$$PQ \mid \mid AC$$

and

... (i) [Mid-point Theorem]

Also in AACD, R is the mid-point of CD and S is the mid-point of AD.

$$SR = \frac{1}{2} AC \text{ and}$$

$$SR \mid \mid AC \qquad \dots (ii)$$
From (i) and (ii), we get

SR = PQ and PQ || SR

Since a pair of opposite sides are equal and parallel.

Therefore, PQRS is a || gm [SR = PQ and PS = RQ] $\Rightarrow$ ...(iii) Now, in  $\triangle ABD$ 

$$PS = \frac{1}{2}DB \qquad ...(iv)$$

But 
$$AC = DB$$

$$\Rightarrow \frac{1}{2}AC = \frac{1}{2}DB$$

$$PQ = PS \qquad ...(v)$$

$$\Rightarrow From (iii), (iv) and (v)$$

$$PQ = QR = RS = SP$$
Hence, PORS is a rhombus. **Proved.**

Q.4. ABCD is a trapezium in which AB || DC, BD is a diagonal and E is the mid-point of AD. A line is drawn through E parallel to AB intersecting BC at F (see Fig.). Show that F is the mid-point of BC.



**Ans.** ABCD is a trapezium in which AB  $\parallel$  DC, BD is a diagonal and E is the mid-point of AD. A line is a drawn through E, parallel to AB intersecting BC at F.

F is the mid-point of BC.

Let EF intersect BD at G.

In  $\triangle ABD$ , EG is the mid-point of DA and EG ||

AB.

So, G is the mid-point of DB.

Again in  $\Delta DBA$ ,

G is the mid-point of DB and GF  $|\,|\,\text{CD}.$ 

 $\therefore$  F is the mid-point of BC.

Q.5. In a parallelogram ABCD, E and F are the mid-points of sides AB and CD respectively (see Fig.). Show that the line segments AF and EC trisect the diagonal BD.



**Ans.** A parallelogram ABCD. E and F are midpoints of sides AB and CD respectively. The line segments AF and EC trisect the diagonal BD or DP PQ=QB.

$$AE = \frac{1}{2} AB \text{ and } FC = \frac{1}{2} CD$$

But  $AB \parallel CD$  and AB = CD,

(Opposite sides of parallelogram)

 $\therefore \qquad AE = FC \text{ and } AE = FC$ 

Thus, AECF is a paralleogram.

Now, F is the mid-point of DC and FP || CQ.

 $\therefore$  P is the mid-point of DQ.

(Mid-point theorem)

Similarly, Q is the mid-points of BP. Thus, DP = PQ = OB. (Proved)

Q.6. Show that the line segments joining the mid-points of the opposite sides of a quadrilateral

**bisect each other.** Ans. Given : A quadrilateral ABCD in which P, Q, R and S are the mid-points of AB, BC, CD and DA, PR and SQ intersect each other.

To prove : PR and SQ bisect each other.

**Proof :** In  $\triangle ABC$ , P is the mid-point of AB and Q is the mid-point of BC.



Similarly, SR | | AC and SR  $\frac{1}{2}$  AC ...(ii)

From Equation (i) and (ii), we get

PQRS is a parallelogram.

We know that diagonals of a parallelogram bisect each other.

Hence, PR and SQ bisect each other.

Q.7. ABC is a triangle right angled at C. A line through the mid-point M of hypotenuse AB and parallel to BC intersects AC at D. Show that

(i) D is the mid-point of AC

(ii)  $MD \perp AC$ 

(iii) 
$$CM = MA = \frac{1}{2}AB$$

**Ans. Given :** ABC is a right angled triangle at C. A line through the mid-point M of hypotenuse AB and parallel to BC intersects AC at D.

**To prove :** (i) D is the mid-point of AC (ii)  $MD \perp AC$ 

(iii) 
$$CM = MA = \frac{1}{2}AB.$$



**Proof :** (i) In  $\triangle$ ABC, M is the mid-point of AB and MD || BC. So, D is the mid-point of AC.

(ii)	MD	BC		
<i>.</i> .	∠BCD =	∠MDA		
But	∠BCD =	rt. angle		
<i>.</i> .	∠MDA =	rt. angle		
Hence,	$MD \perp$	AC.		
(iii) A and M is the mid-point of AB.				
<i>.</i>	AM =	MB		

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In  $\triangle$ ADM and  $\triangle$ CDM ; DM = DM  $\angle$ ADM =  $\angle$ CDM (Proved above each = 90°) AD = CD, (Proved above)  $\therefore \quad \Delta ADM = \quad \Delta CDM \quad (SAS rule)$ So,  $AM = \quad CM \quad (CPCT)$ Hence,  $CM = \quad AM = \frac{1}{2} AB. (Proved)$ 

# **Additional Questions**

*.*..

Q.1. Diagonals of a rectangle are equal and perpendicular. Is this statement true? Give reason for your answer.

**Ans.** No. Diagonals of a rectangle are equal but need not be perpendicular.

Q.2. All the angles of a quadrilateral are equal. What special name is given to this quadrilateral?

Ans. In rectangle all angles are equal.

Q.3. In quadrilateral ABCD,  $\angle A + \angle D = 180^{\circ}$ . What special name can be given to this quadrilateral?

**Ans.** It is a trapezium because sum of interior angles is 180°.

Q.4. Diagonals of a parallelogram are perpendicular to each other. Is this statement true? Give reason for your answer.

**Ans.** No. Diagonals of a parallelogram are not perpendicular to each other. They only bisect each other.

Q.5. Can the angles  $110^{\circ}$ ,  $80^{\circ}$ ,  $70^{\circ}$  and  $95^{\circ}$  be the angles of a quadrilateral? Why or why not?

**Ans.** No. We know that, sum of the angles of a quadrillateral is  $360^{\circ}$ .

Here, sum of the angles =  $110^{\circ} + 80^{\circ} + 70^{\circ} + 95^{\circ} = 355^{\circ}$ .

So, these angles cannot be the angles of a quadrilateral.

Q.6. Can all the angles of a quadrilatral be acute angles? Give reason for your answer.

**Ans.** No. All the angles of a quadrilateral cannot be acute angles. Since, sum of the angles of a quadrilateral is 360°.

Q.7. Can all the angles of a quadrilateral be right angles ? Give reason for your answer.

**Ans.** Yes, all the angles of a quadrilatral be right angles. In this case, the quadrilateral becomes rectangle or square.

#### Q.8. Opposite angles of a quadrilatral ABCD

are equal. If AB = 4 cm, determine CD.

**Ans.** Given, opposite angles of a quadrilateral are equal. So, ABCD is a parallelogram and we know that in a parallelogram opposite sides are also equal.

$$CD = AB = 4 cm$$

Q.9. One angle of a quadrilateral is of  $180^{\circ}$  and the remaining three angles are equal. Find each of the three equal angles.

**Ans.** Let each of the three equal angles is of  $x^{\circ}$ . Now, sum of angles of a quadrilateral =  $360^{\circ}$ 

$$\Rightarrow 108^{\circ} + x^{\circ} + x^{\circ} + x^{\circ} = 360^{\circ}$$

$$\Rightarrow 3x^{\circ} = 360^{\circ} - 108^{\circ}$$

$$\Rightarrow x^{\circ} = \frac{252^{\circ}}{3}$$

$$\Rightarrow x^{\circ} = 84^{\circ}$$

Hence, each of the three equal angles =  $84^{\circ}$ .

Q.10. Show that each angle of a rectangle is a right angle.

Ans. We have ABCD as a rectangle

 $\Rightarrow$  ABCD is a parallelogram

$$\Rightarrow$$
 AD || BC

Now, AD || BC and AB intersects them at A and B.

 $\therefore \quad \angle A + \angle B = 180^{\circ}$ 

[Sum of the interior angles on the same side of a transversal is 180°]

$$\Rightarrow 90^\circ + \angle B = 180^\circ [\angle A = 90^\circ (given)]$$



Similarly, we can show that  $\angle C = 90^{\circ}$  and  $\angle 90^{\circ}$ . Hence,  $\angle A = \angle B = \angle C = \angle D = 90^{\circ}$ 

# **Multiple Choice Questions**

Q.1. In a quadrilateral, if one of angle is 90° and opposite sides are equal, then it is a:		Q.6. In a parallelogram, if the adjacent angles are $(3x+10)^{\circ}$ and $(5x+30)^{\circ}$ , then value of x is:		
(a) rhombus	(b) trapezium	(a) 20°	(b) 25°	
(c) rectangle	(d) square	(c)30°	(d) 40°	
Ans. (c) rectangle		<b>Ans.</b> (b) 25°		
Q.2. The bisectors of the angles of parallelogram		Q.7. If an angle of a parallelogram is two third of its		
form a:		adjacent angle, the smallest angle of the		
(a) trapezium	(b) paralleogram	parallelogram is:		
(c) rectangle	(d) square	(a) 108°	(b) 72°	
Ans. (c) rectangle	· · · •	(c) 54°	(d) 126°	
Q.3. When each angle of a rhombus is of 90°, it is		<b>Ans.</b> (b) 72°		
called a:		Q.8. If the diagonals of a parallelogram are equal,		
(a) square	(b) paralleogram	then it is a:		
(c) rectangle	(d) trapezium	(a) rhombus	(b) trapezium	
Ans. (a) square		(c) rectangle	(d) square	
<b>O.4.</b> If the diagonals of a quadrilateral bisect each		Ans. (c) rectangle		
other at right angles, then it is a:		Q.9. If the diagonals of a quadrilateral bisect the		
(a) trapezium	(b) rectangle	opposite angle, then it is a:		
(c) rhombus	(d) paralleogram	(a) square	(b) paralleogram	
Ans. (c) rhombus		(c) rectangle	(d) trapezium	
O.5. The perimeter of a parallelogram is 28 cm. if		Ans. (a) square		
shorter sides measure 4.5 cm, then measure of		Q.10. If ABCD is a paralleogram, then $\angle A - \angle C$ is		
the longer side is:	,	equal to:		
(a) 9.5 cm	$(b)9 \mathrm{cm}$	(a) 90°	(b) 45°	
(c) $6.5 \mathrm{cm}$	(d) $7.5 \mathrm{cm}$	(c) 180°	(d) 0°	
<b>Ans.</b> 9.5 cm	· /	<b>Ans.</b> (d) 0°		